

# Tutorial outline

- Overview (this)
- Image representation (60 mins, 9:15 - 10:30)
  - motivation, local features, global features, break
- Learning (90 mins, 10:30 - 12:30)
  - discriminative models, tea-break, generative models, break
- Object detection and recognition (90 mins, 12:30 - 2:00)
  - Dalal & Triggs, lunch-break, PASCAL challenge, *poselets* and their applications, tea-break
- Cross-modal search (60 mins, 2:30 - 3:30)

**lunch-break** 60 mins, **break** 15 mins, **tea-break** 20-30 mins

# ICVGIP 2012, IIT Bombay

The eight Indian Conference on Computer Vision, Graphics and  
Image Processing

## Tutorial

# Histogram of Oriented Gradients

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Slides courtesy Ross Girshick

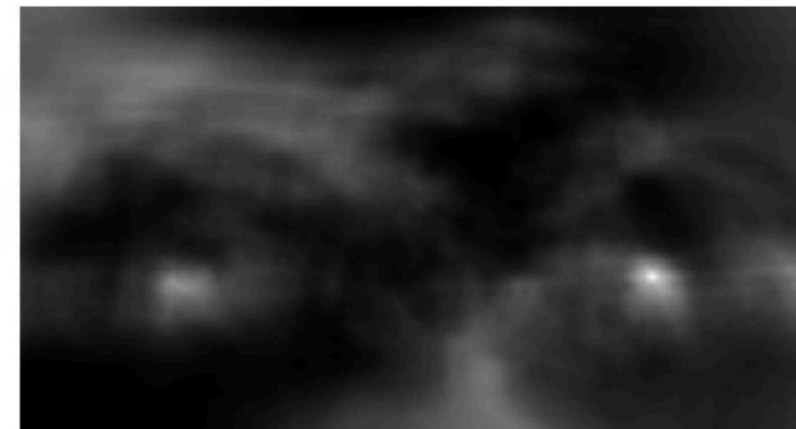
# (Review?) Template matching

- Consider matching with image patches
  - What could go wrong?

template



image



match quality  
e.g., cross correlation

# What is a feature map?

- Any transformation of an image into a new representation
- Example: transform an image into a binary edge map

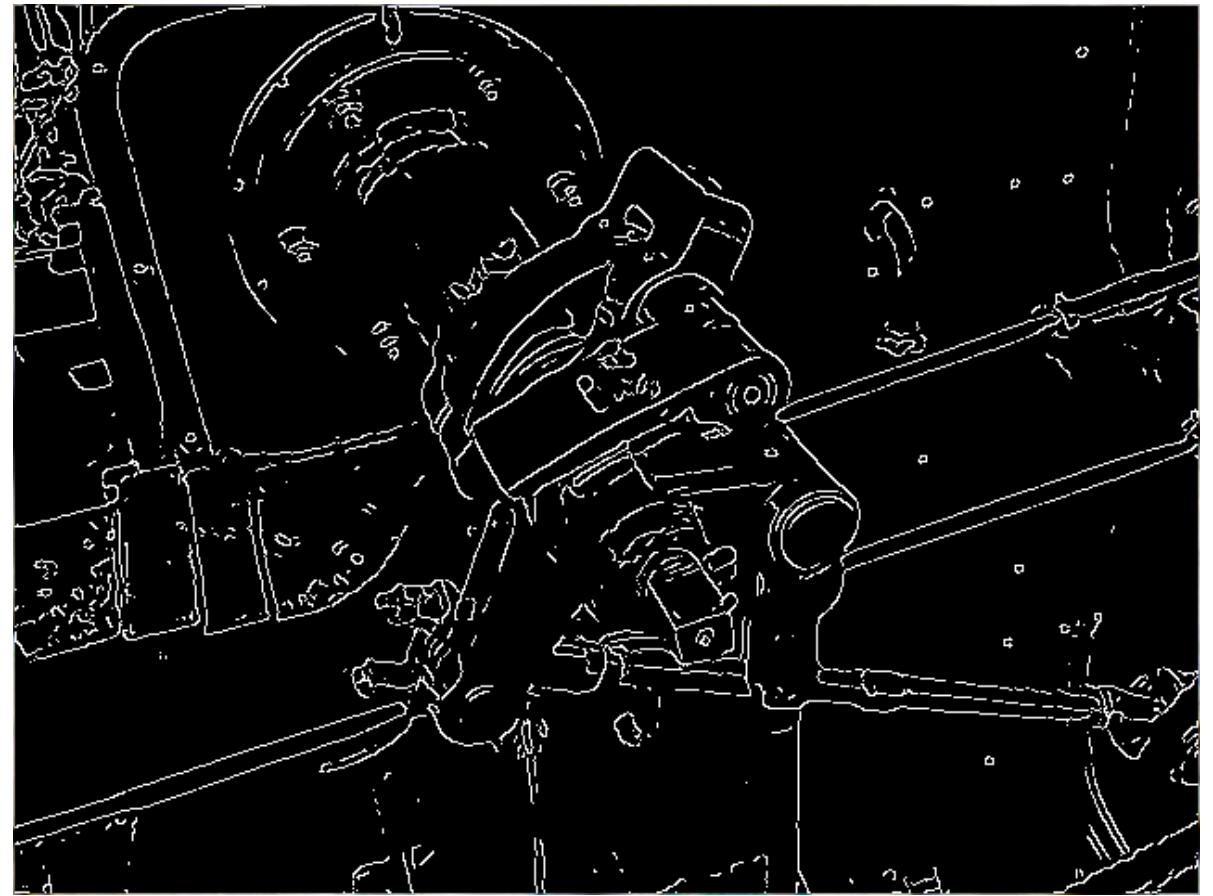
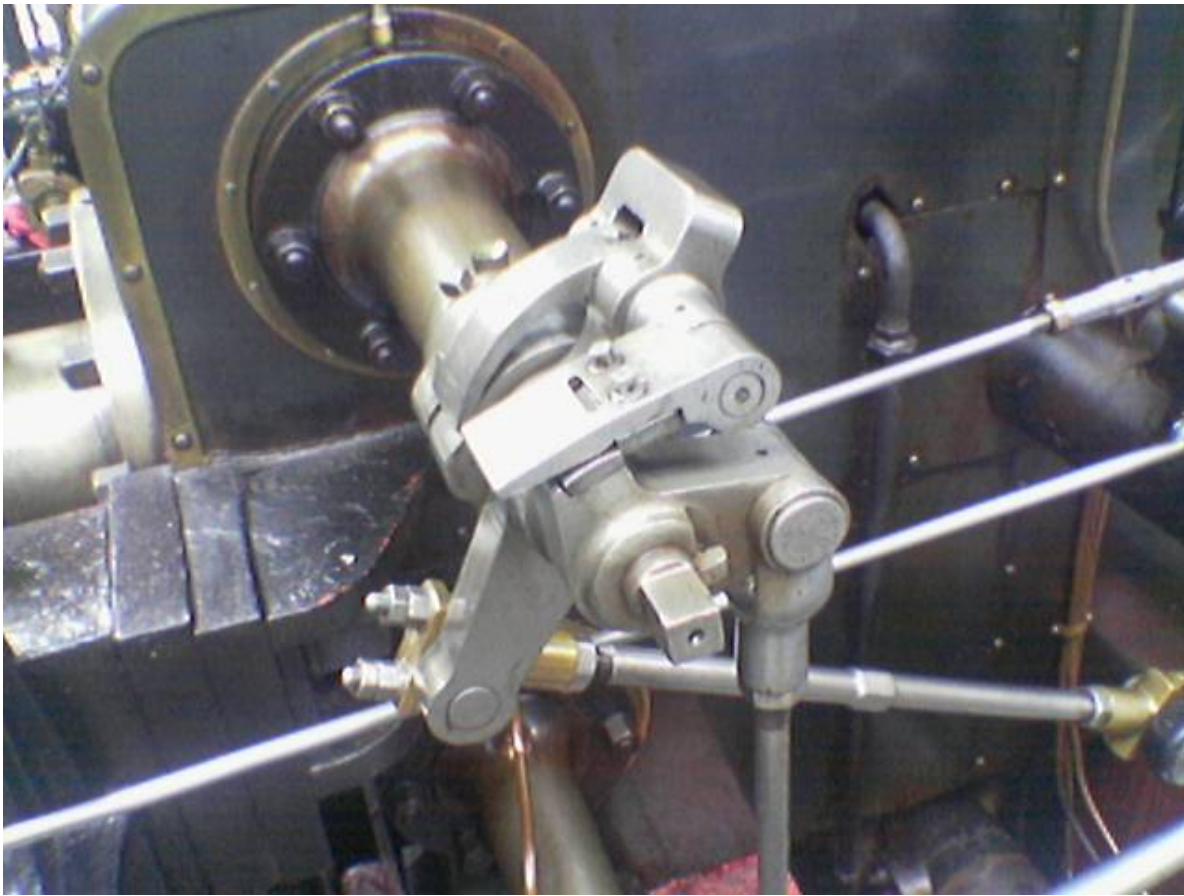


Image source: wikipedia



# Feature map goals

- Introduce invariance
  - Bias, gain, nonlinear transformations
  - Small deformations



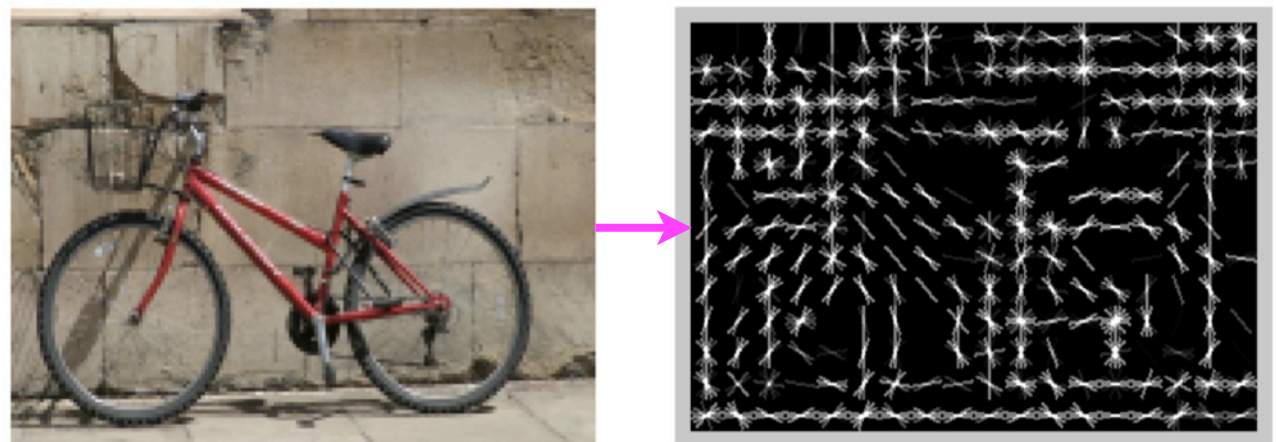
Figure 1.3: Variation in appearance due to a change in illumination

- Preserve larger scale spatial structure

Image: [Fergus05]

# Histograms of Oriented Gradients (HOG)

- Introduce invariance
  - Bias / gain / nonlinear transformations
    - bias: gradients / gain: local normalization
    - nonlinearity: clamping magnitude, orientations
- Small deformations
  - spatial subsampling
  - local “bag” models



- References
  - “Histograms of oriented gradients for human detection.” N. Dalal and B. Triggs, CVPR 2005.
  - “Finding people in images and videos.” N. Dalal, Ph.D. Thesis, Institut National Polytechnique de Grenoble, 2006.

# HOG feature computation

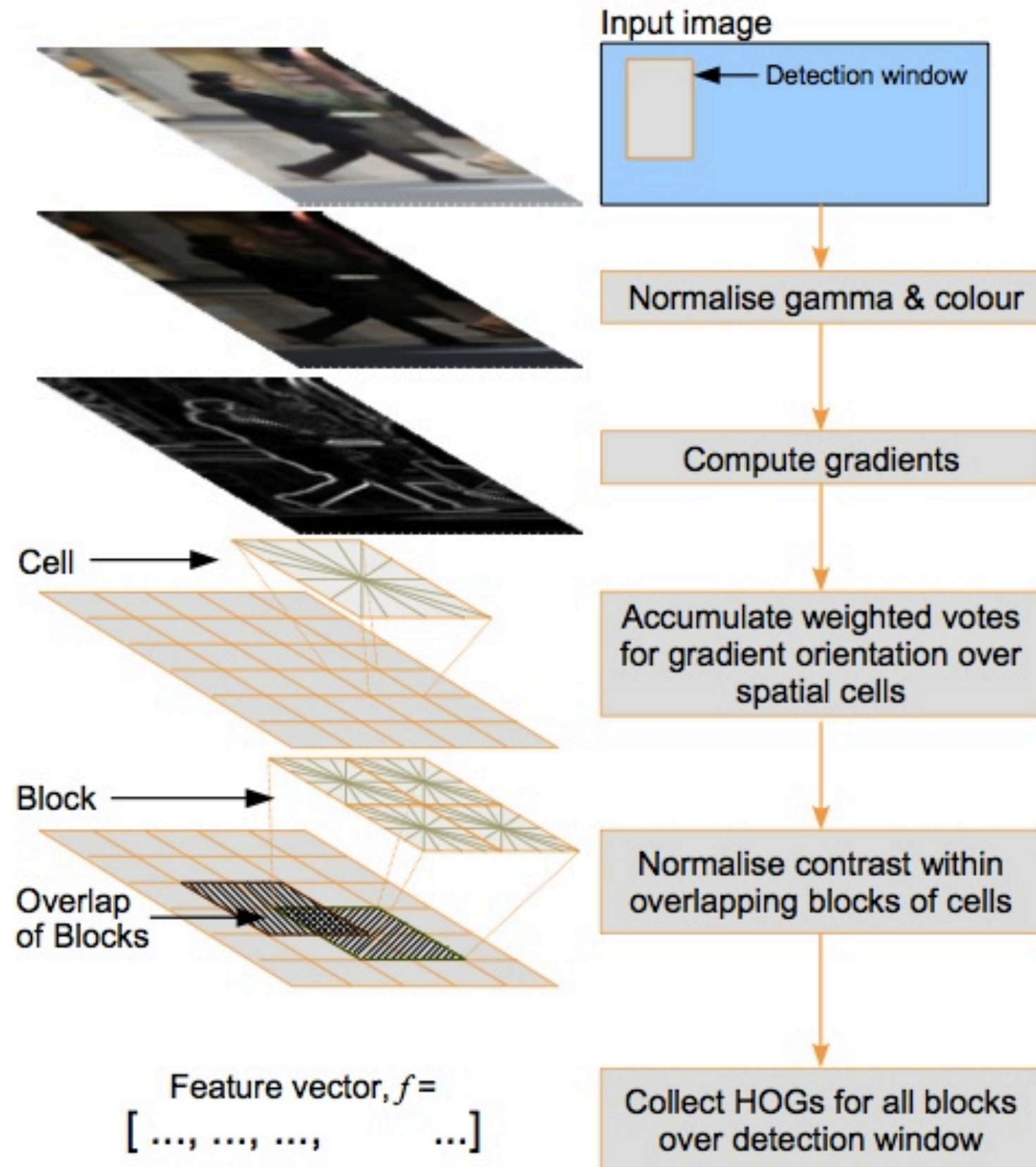
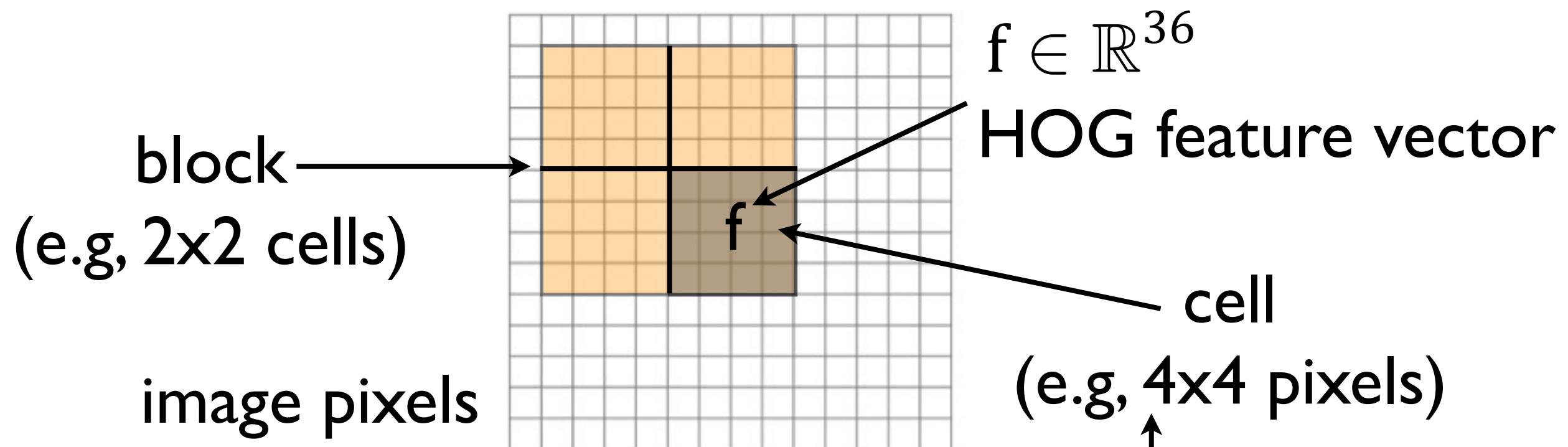


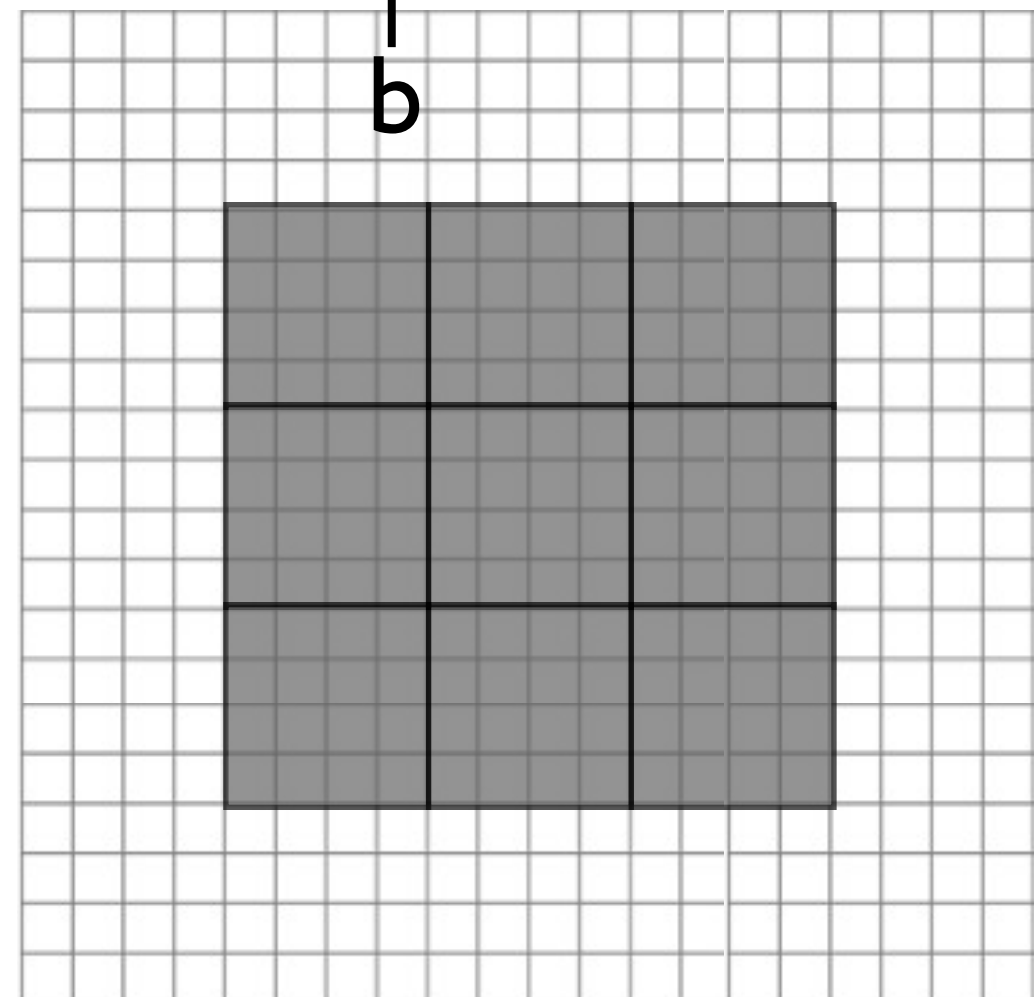
Image: [Dalal06]



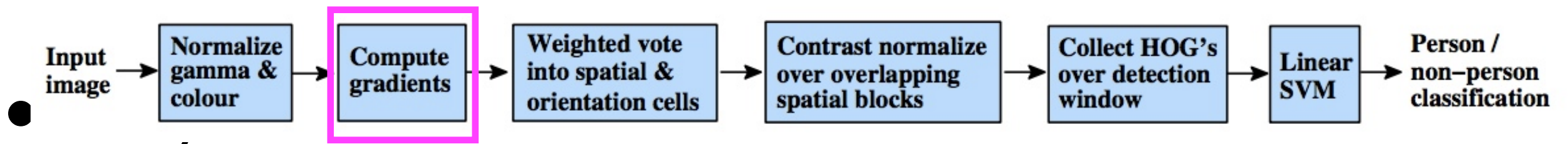
# HOG terminology



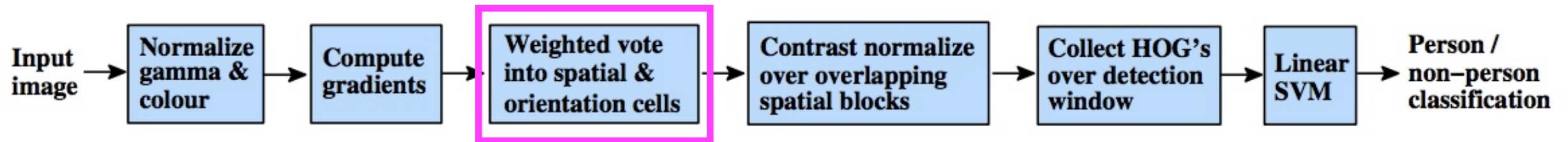
- Original image:  $H \times W \times 3$
- Feature map:  $H' \times W' \times D$
- For example
  - $H' = \text{floor}(H/b) - 2$
  - $W' = \text{floor}(W/b) - 2$
  - $D = 36$



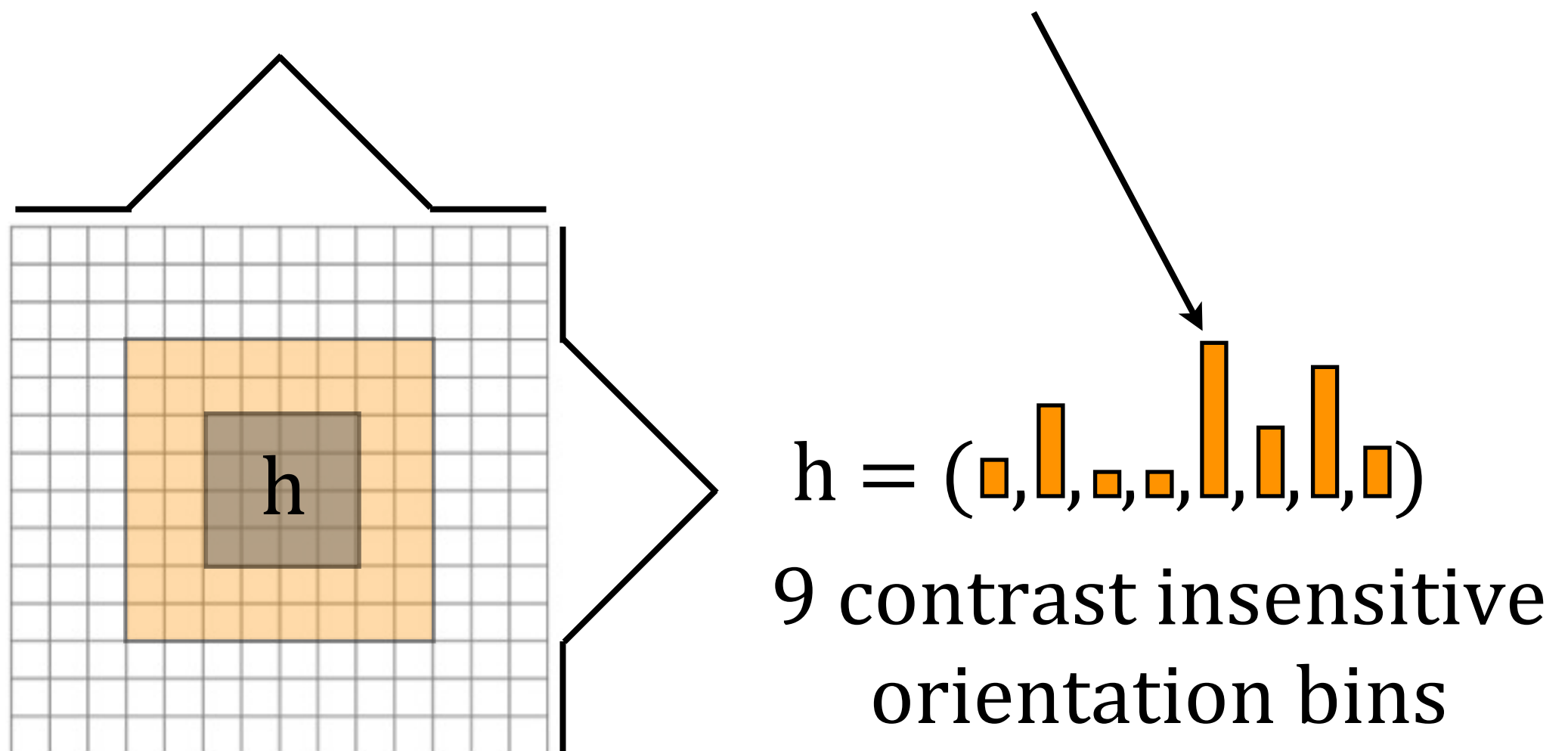


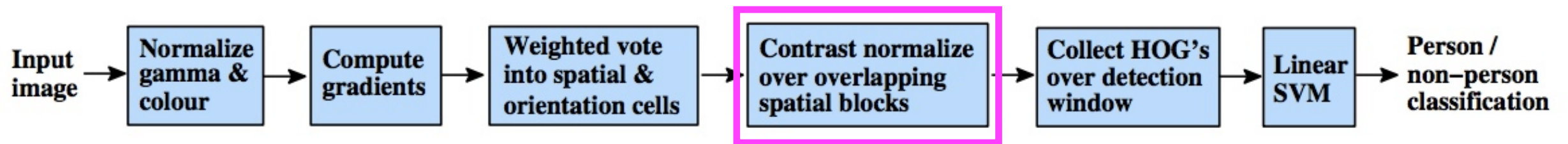


- $(1, 0, -1)$  centered filter works best
- Alternatives: uncentered, cubic corrected, Sobel, etc.
- Discrete approx. to partial derivatives
  - $I_x = I[x+1, y] - I[x-1, y]$
  - $I_y = I[x, y+1] - I[x, y-1]$

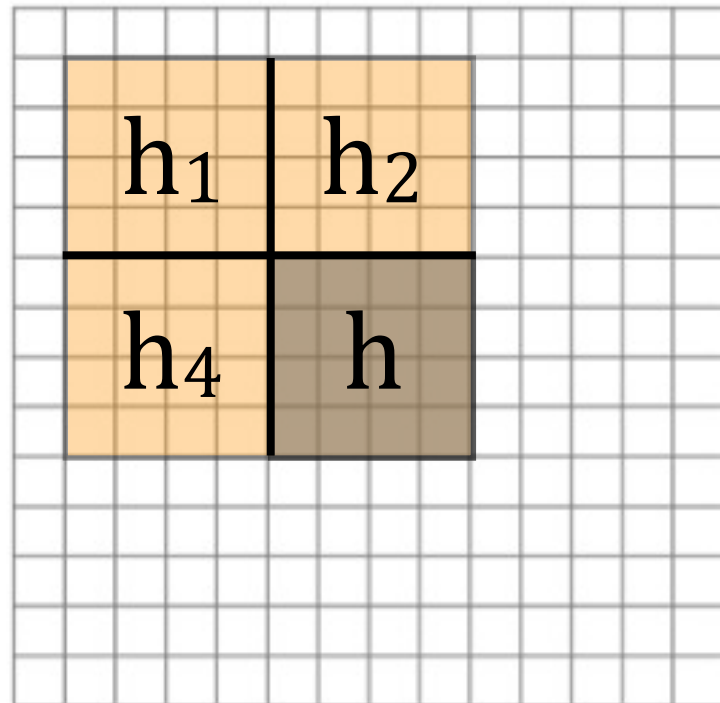


- Gradient magnitude:  $m = || (I_x, I_y) ||$
- Gradient orientation:  $\theta = \tan^{-1}(I_y / I_x)$
- Quantize orientation; vote into bin (weighted)





- Local contrast normalization and clipping



$$h^1 = \max[0.2, h / ||(h; h_1; h_2; h_4)||]$$

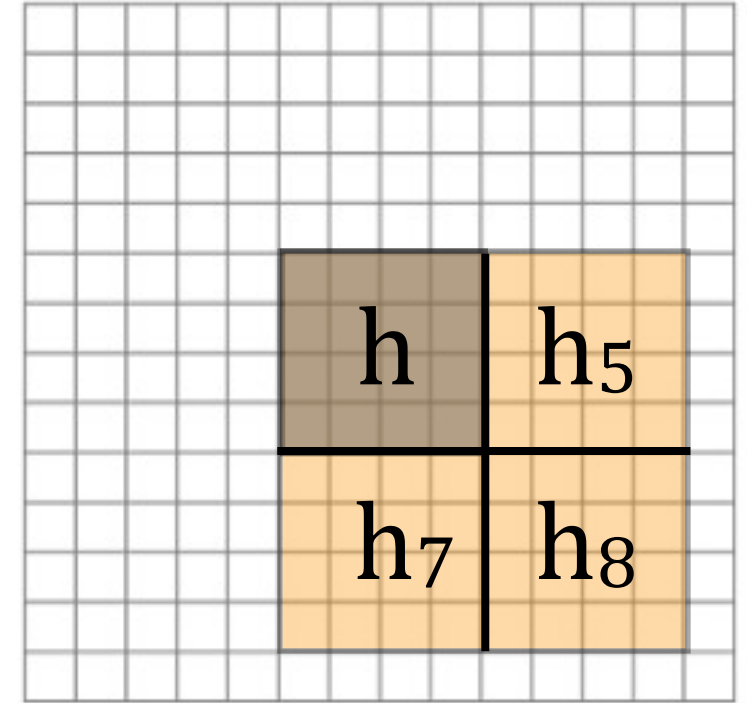
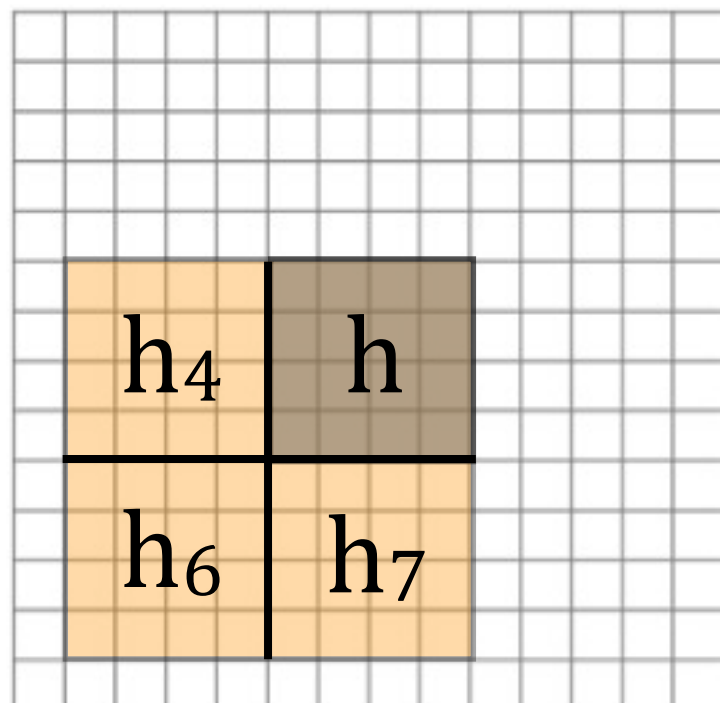
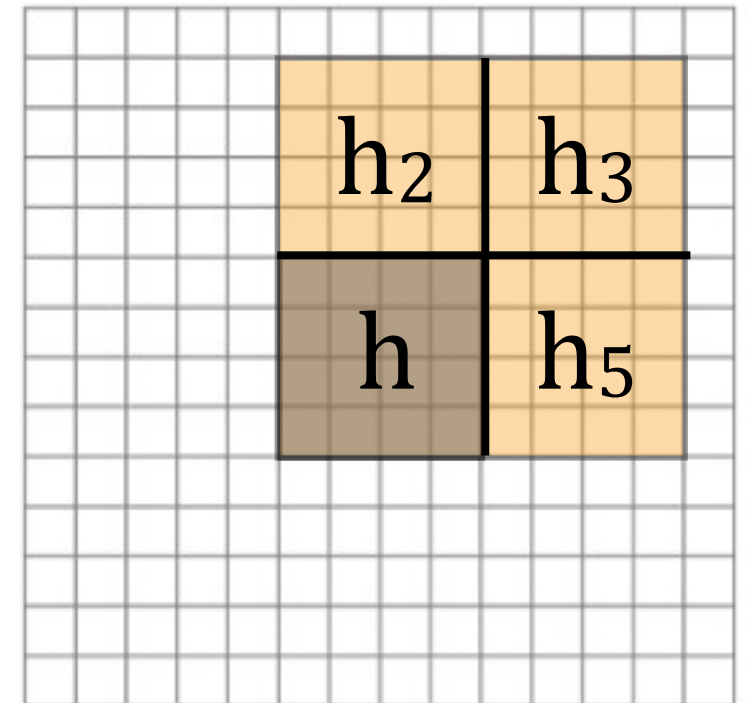
$$h^2 = \max[0.2, h / ||(h; h_2; h_3; h_5)||]$$

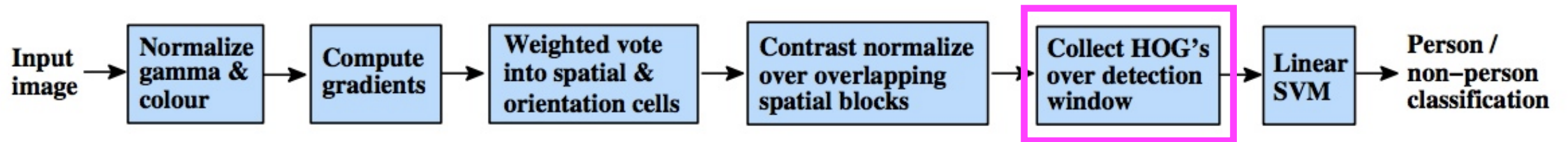
$$h^3 = \max[0.2, h / ||(h; h_4; h_6; h_7)||]$$

$$h^4 = \max[0.2, h / ||(h; h_5; h_7; h_8)||]$$

$$f = (h^1; h^2; h^3; h^4)$$

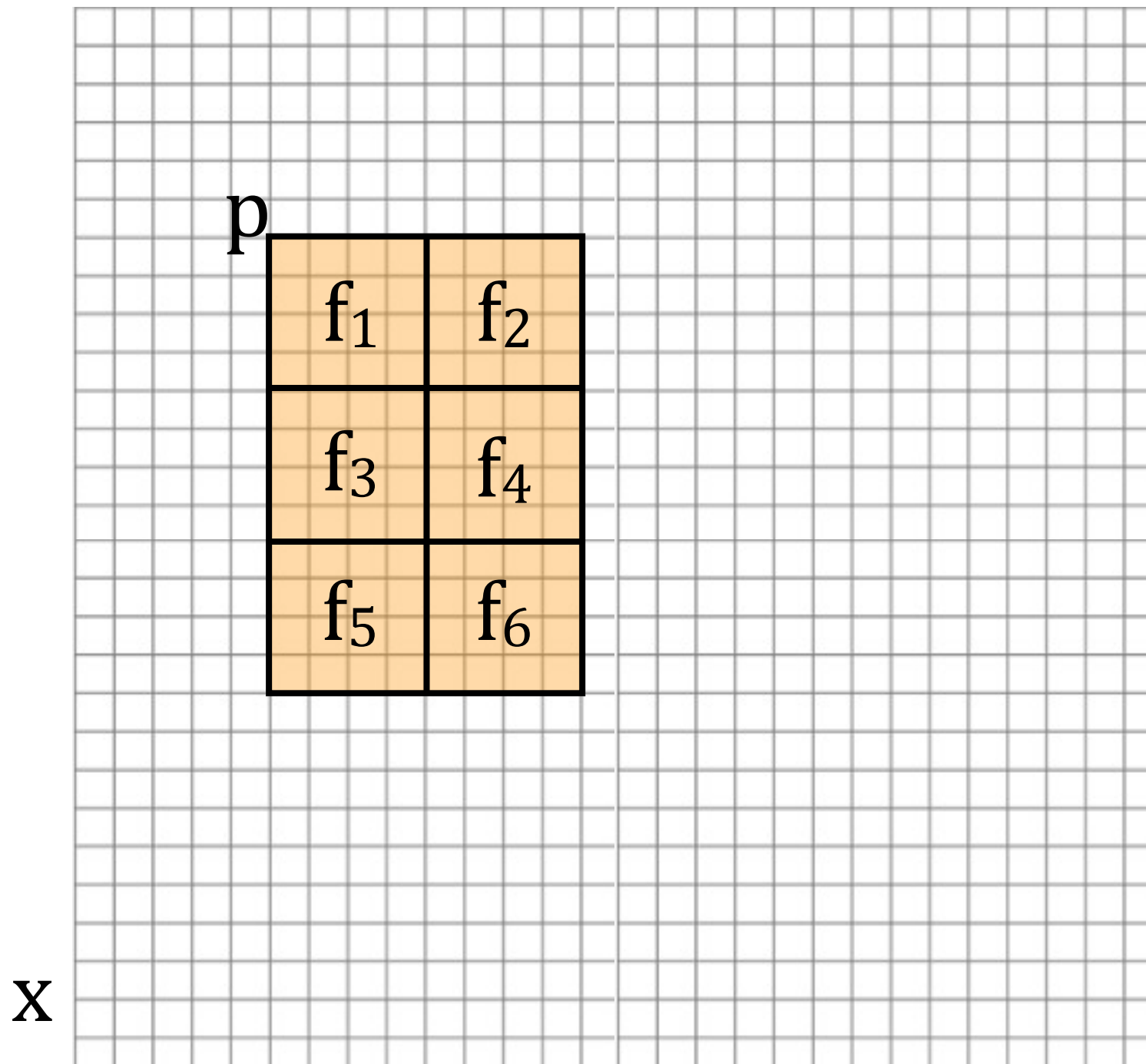
Final dimensionality  
per cell: 36





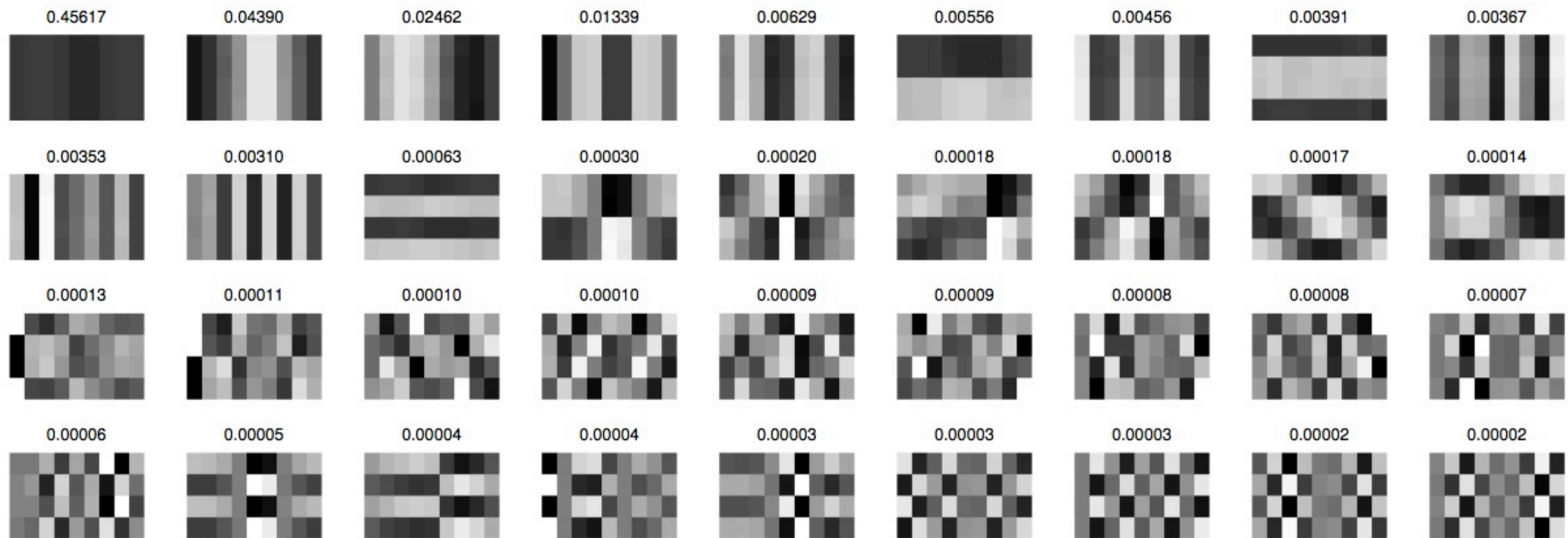
- Sliding window feature vector

- $\Phi(x, p) = (f_1; f_2; f_3; f_4; f_5; f_6)$



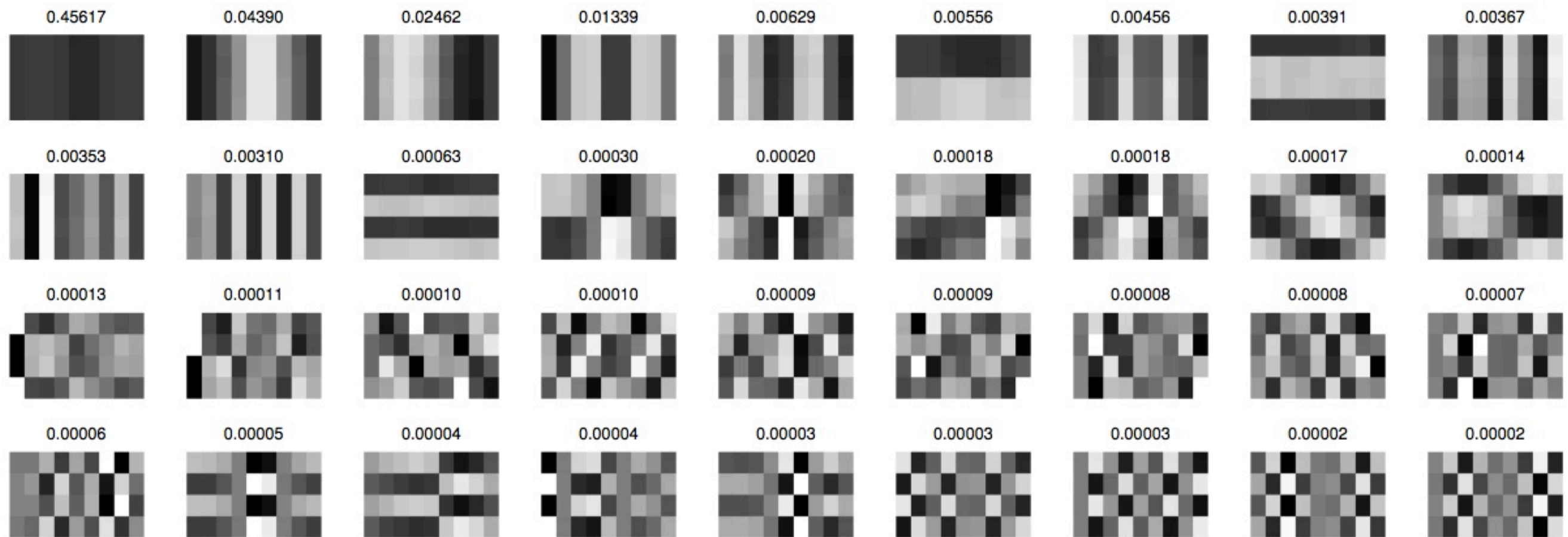


# HOG reformulation



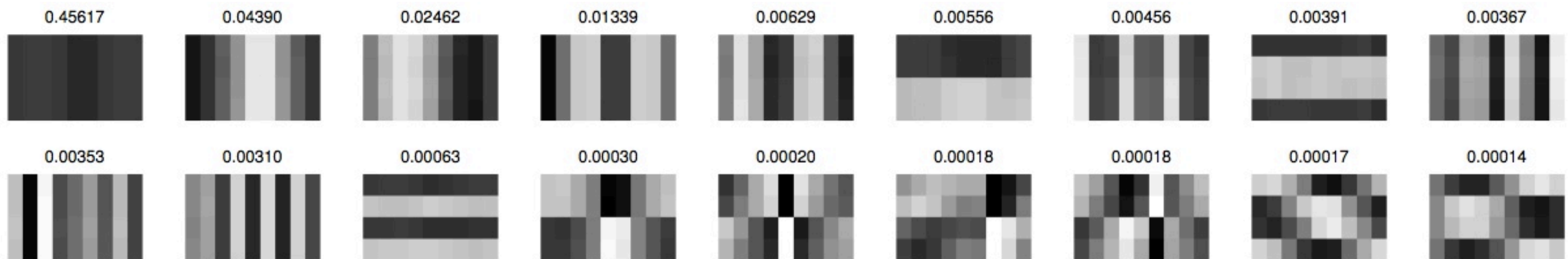
- PCA of HOG features
  - Eigenvectors have a strong structure
  - Dim. reduction to top 12 with no loss in performance

# HOG PCA eigenvectors



- Eigenvector structure
  - All rows or columns are (approximately) constant in the top 12 eigenvectors
  - Suggests a different basis

# V, a sparse basis for HOG



1	0	0	0	0	0	0	0	0
1	0	0	0	0	0	0	0	0
1	0	0	0	0	0	0	0	0
1	0	0	0	0	0	0	0	0

$u_1$

0	1	0	0	0	0	0	0	0
0	1	0	0	0	0	0	0	0
0	1	0	0	0	0	0	0	0
0	1	0	0	0	0	0	0	0

$u_2$

...

0	0	0	0	0	0	0	0	1
0	0	0	0	0	0	0	0	1
0	0	0	0	0	0	0	0	1
0	0	0	0	0	0	0	0	1

$u_9$

1	1	1	1	1	1	1	1	1
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0

$v_1$

...

0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
1	1	1	1	1	1	1	1	1

$v_4$

New basis  $V = \{u_1, \dots, u_9\} \cup \{v_1, v_2, v_3, v_4\}$

# Interpretation of V

Original HOG

$$f = (h^1; h^2; h^3; h^4)$$

Final dimensionality  
per cell: 36

Analytic projection

$$f = (h^1 + h^2 + h^3 + h^4; 1 \cdot h^1; 1 \cdot h^2; 1 \cdot h^3; 1 \cdot h^4)$$

Final dimensionality  
per cell: 13



# HOG summary

- There's no one true HOG feature
  - Large number of parameters and design choices (see Dalal's thesis)
  - Typical settings
    - cells: 6-8 pixels wide
    - cell blocks: 2x2 or 3x3 rectangular
- The original formulation contains redundant information
- Efficient and intuitive dimensionality reduction by analytic projection