Workshop on Essential Abstractions in GCC

GDFA: Generic Data Flow Analyser for GCC

GCC Resource Center (www.cse.iitb.ac.in/grc)

Department of Computer Science and Engineering, Indian Institute of Technology, Bombay



July 2009

(日) (四) (문) (문) (문)

Motivation

- Introduction to data flow analysis
 - Live variables analysis
 - Available expressions analysis
- Common abstractions in data flow analysis
- Implementing data flow analysis using gdfa
- Design and Implementation of gdfa



Part 1

Introduction to Data Flow Analysis

◆□▶ ◆圖▶ ◆臣▶ ◆臣▶ 臣 のへで

Motivation behind gdfa

- Specification Vs. implementation
- Orthogonality of specification of data flow analysis and the process of performing data flow analysis
- Practical significance of generalizations
- Ease of extending data flow analysers

Part 2

Introduction to Data Flow Analysis

◆□▶ ◆圖▶ ◆臣▶ ◆臣▶ 臣 のへで









A variable v is live at a program point p, if some path from p to program exit contains an r-value occurrence of v which is not preceded by an l-value occurrence of v.





Essential Abstrations in GCC

4/37

Defining Data Flow Analysis for Live Variables Analysis







Essential Abstrations in GCC





4/37

Defining Data Flow Analysis for Live Variables Analysis



GCC Resource Center, IIT Bombay





Essential Abstrations in GCC

$$Gen_n = \{ v \mid variable v is used in basic block n and is not preceded by a definition of v \} Kill_n = \{ v \mid basic block n contains a definition of v \}$$



r-value occurrence Value is only read, e.g. x,y,z in x.sum = y.data + z.data Gen_n = { $v \mid$ variable v is used in basic block n and is not preceded by a definition of v } Kill_n = { $v \mid$ basic block n contains a definition of v }













Essential Abstrations in GCC





GCC Resource Center, IIT Bombay

6/37



Essential Abstrations in GCC

7/37

Data Flow Equations For Live Variables Analysis

$$In_n = (Out_n - Kill_n) \cup Gen_n$$
$$Out_n = \begin{cases} BI \ n \text{ is } End \text{ block} \\ \bigcup_{s \in succ(n)} In_s \text{ otherwise} \end{cases}$$



7/37

Data Flow Equations For Live Variables Analysis

$$In_n = (Out_n - Kill_n) \cup Gen_n$$
$$Out_n = \begin{cases} BI \ n \ is \ End \ block \\ \bigcup_{s \in succ(n)} In_s \ otherwise \end{cases}$$

 In_n and Out_n are sets of variables.









Essential Abstrations in GCC





Essential Abstrations in GCC



Essential Abstrations in GCC





Essential Abstrations in GCC





Essential Abstrations in GCC

8/37

Performing Live Variables Analysis



Essential Abstrations in GCC







Using Data Flow Information of Live Variables Analysis

- Used for register allocation.
 - If variable x is live in a basic block b, it is a potential candidate for register allocation.



Using Data Flow Information of Live Variables Analysis

• Used for register allocation.

If variable x is live in a basic block b, it is a potential candidate for register allocation.

Used for dead code elimination.
If variable x is not live after an assignment x = ..., then the assginment is redundant and can be deleted as dead code.



11/37

Defining Available Expressions Analysis

An expression e is available at a program point p, if every path from program entry to p contains an evaluation of ewhich is not followed by a definition of any operand of e.


Defining Available Expressions Analysis

An expression e is available at a program point p, if every path from program entry to p contains an evaluation of ewhich is not followed by a definition of any operand of e.



Defining Available Expressions Analysis

An expression e is available at a program point p, if every path from program entry to p contains an evaluation of ewhich is not followed by a definition of any operand of e.



Defining Available Expressions Analysis

An expression e is available at a program point p, if every path from program entry to p contains an evaluation of ewhich is not followed by a definition of any operand of e.



Local Data Flow Properties for Available Expressions Analysis

 $Gen_n = \{ e \mid expression \ e \ is \ evaluated \ in \ basic \ block \ n \ and this \ evaluation \ is \ not \ followed \ by \ a \ definition \ of \ any \ operand \ of \ e \}$

 $Kill_n = \{ e \mid basic block n contains a definition of an operand of e \}$



Data Flow Equations For Available Expressions Analysis

$$In_n = \begin{cases} BIn \text{ is } Start \text{ block} \\ \bigcap_{p \in pred(n)} Out_p & \text{ otherwise} \end{cases}$$

$$Out_n = Gen_n \cup (In_n - Kill_n)$$



Data Flow Equations For Available Expressions Analysis

$$In_n = \begin{cases} BIn \text{ is } Start \text{ block} \\ \bigcap_{p \in pred(n)} Out_p & \text{ otherwise} \end{cases}$$

$$Out_n = Gen_n \cup (In_n - Kill_n)$$

Alternatively,

$$Out_n = f_n(In_n),$$
 where

 $f_n(X) = \operatorname{Gen}_n \cup (X - \operatorname{Kill}_n)$



Data Flow Equations For Available Expressions Analysis

$$In_n = \begin{cases} BIn \text{ is } Start \text{ block} \\ \bigcap_{p \in pred(n)} Out_p & \text{ otherwise} \end{cases}$$

$$Out_n = Gen_n \cup (In_n - Kill_n)$$

Alternatively,

$$Out_n = f_n(In_n),$$
 where

$$f_n(X) = \operatorname{Gen}_n \cup (X - \operatorname{Kill}_n)$$

 In_n and Out_n are sets of expressions.



• Used for common subsexpression elimination.



- Used for common subsexpression elimination.
 - If an expression is available at the entry of a block b and



- Used for common subsexpression elimination.
 - If an expression is available at the entry of a block b and
 - a computation of the expression exists in b such that



- Used for common subsexpression elimination.
 - If an expression is available at the entry of a block b and
 - a computation of the expression exists in b such that
 - it is not preceded by a definition of any of its operands

- Used for common subsexpression elimination.
 - If an expression is available at the entry of a block b and
 - a computation of the expression exists in b such that
 - it is not preceded by a definition of any of its operands

Then the expression is redundant.

- Used for common subsexpression elimination.
 - If an expression is available at the entry of a block b and
 - a computation of the expression exists in b such that
 - it is not preceded by a definition of any of its operands

Then the expression is redundant.

• Expression must be upwards exposed or locally anticipable.



- Used for common subsexpression elimination.
 - If an expression is available at the entry of a block b and
 - a computation of the expression exists in b such that
 - it is not preceded by a definition of any of its operands

Then the expression is redundant.

- Expression must be upwards exposed or locally anticipable.
- Expressions in Gen_n are downwards exposed.



Part 3

Common Abstractions in Data Flow Analysis

◆□▶ ◆□▶ ◆三▶ ◆三▶ 三三 少へで

Common Form of Data Flow Equations

$\begin{array}{rcl} X_i &=& f(Y_i) \\ Y_i &=& \prod X_j \end{array}$



Common Form of Data Flow Equations





Common Form of Data Flow Equations





Common Form of Data Flow Equations



| | Confluence | | |
|---------------|----------------------|--------------------------------|--|
| Union | | Intersection | |
| Forward | Reaching Definitions | Available Expressions | |
| Backward | Live Variables | Anticipable Exressions | |
| Bidirectional | | Partial Redundancy Elimination | |
| (limited) | | (Original M-R Formulation) | |



| Any Path | | | |
|---------------|----------------------|--------------------------------|--|
| | | | |
| | | | |
| | Confluence | | |
| | Union Intersection | | |
| Forward | Reaching Definitions | Available Expressions | |
| Backward | Live Variables | Anticipable Exressions | |
| Bidirectional | | Partial Redundancy Elimination | |
| (limited) | | (Original M-R Formulation) | |



| Any Path | | | |
|---------------|---------------------------------------|-----------------------|--|
| All Paths | | | |
| | | | |
| | Confluence | | |
| | Union | Intersection | |
| Forward | Reaching Definitions | Available Expressions | |
| Backward | Live Variables Anticipable Exressions | | |
| Bidirectional | Partial Redundancy Elimination | | |
| (limited) | (Original M-R Formulation) | | |



| Any Path All Paths | | | |
|-----------------------|----------------------|--------------------------------|--|
| | Confluence | | |
| | Union | Intersection | |
| Forward | Reaching Definitions | Available Expressions | |
| Backward | Live Variables | Anticipable Exressions | |
| Bidirectional | | Partial Redundancy Elimination | |
| (limited) | | (Original M-R Formulation) | |



| 0 | Any | Path All Paths | |
|---------------|----------------------|--------------------------------|--|
| | | Confluence / | |
| | Union | Intersection | |
| Forward | Reaching Definitions | Available Expressions | |
| Backward | Live Variables | Anticipable Exressions | |
| Bidirectional | | Partial Redundancy Elimination | |
| (limited) | | (Original M-R Formulation) | |
| 0,0 | | | |



GCC Resource Center, IIT Bombay



| | Any | All Paths | |
|---------------|----------------------|--------------------------------|--|
| | | Confluence | |
| | Union | Intersection | |
| Forward | Reaching Definitions | Available Expressions | |
| Backward | Live Variables | Anticipable Exressions | |
| Bidirectional | | Partial Redundancy Elimination | |
| (limited) | | (Original M-R Formulation) | |
| | | | |



The Abstraction of Flow Functions



The Abstraction of Data Flow Values



GCC Resource Center, IIT Bombay



The Abstraction of Data Flow Equations

$$In_{n} = \begin{cases} BIStart \sqcap \overleftarrow{f_{n}}(Out_{n}) & n = Start \\ \left(\prod_{m \in pred(n)} \overrightarrow{f_{m \to n}}(Out_{m})\right) \sqcap \overleftarrow{f_{n}}(Out_{n}) & \text{otherwise} \end{cases}$$
$$Out_{n} = \begin{cases} BIEnd \sqcap \overrightarrow{f_{n}}(In_{n}) & n = End \\ \left(\prod_{m \in succ(n)} \overleftarrow{f_{m \to n}}(In_{m})\right) \sqcap \overrightarrow{f_{n}}(In_{n}) & \text{otherwise} \end{cases}$$



Iterative Methods of Performing Data Flow Analysis

Successive recomputation after conservative initialization (\top)

- *Round Robin*. Repeated traversals over nodes in a fixed order Termination : After values stabilise
 - + Simplest to understand and implement
 - May perform unnecessary computations



Iterative Methods of Performing Data Flow Analysis

Successive recomputation after conservative initialization (\top)

- Round Robin. Repeated traversals over nodes in a fixed order Termination : After values stabilise
 - + Simplest to understand and implement
 - May perform unnecessary computations

Our examples use this method.



Iterative Methods of Performing Data Flow Analysis

Successive recomputation after conservative initialization (\top)

- Round Robin. Repeated traversals over nodes in a fixed order Termination : After values stabilise
 - + Simplest to understand and implement
 - May perform unnecessary computations

Our examples use this method.

- *Work List*. Dynamic list of nodes which need recomputation Termination : When the list becomes empty
 - $+\,$ Demand driven. Avoid unnecessary computations.
 - Overheads of maintaining work list.

Common Form of Flow Functions

$$f_n(X) = (X - \operatorname{Kill}_n(X)) \cup \operatorname{Gen}_n(X)$$

• For General Data Flow Frameworks

$$Gen_n(X) = ConstGen_n \cup DepGen_n(X)$$

 $Kill_n(X) = ConstKill_n \cup DepKill_n(X)$

• For bit vector frameworks

$$Gen_n(X) = ConstGen_n$$

 $Kill_n(X) = ConstKill_n$

Defining Flow Functions for Bit Vector Frameworks

• Live variables analysis

| | Entity | Manipulation | Exposition |
|------------------------|----------|--------------|------------|
| ConstGen _n | Variable | Use | Upwards |
| ConstKill _n | Variable | Modification | Anywhere |

• Available expressions analysis

| | Entity | Manipulation | Exposition |
|-------------------|------------|--------------|------------|
| Gen _n | Expression | Use | Downwards |
| Kill _n | Expression | Modification | Anywhere |



Part 5

Implementing Data Flow Analysis using gdfa

◆□▶ ◆□▶ ◆臣▶ ◆臣▶ 臣 のへで

Implementing Available Expressions Analysis

- 1. Specifying available expressions analysis
- 2. Implementing the entry function of available expressions analysis pass
- 3. Registering the available expressions analysis pass
 - 3.1 Declaring the pass
 - 3.2 Registering the pass
 - 3.3 Positioning the pass



Step 1: Specifying Available Expressions Analysis

```
struct gimple_pfbv_dfa_spec gdfa_ave =
ł
     entity_expr,
                                    /* entity
                                                            */
                                    /* top_value
                                                            */
     ONES,
     ZEROS,
                                    /* entry_info
                                                            */
     ONES,
                                    /* exit_info
                                                            */
     FORWARD,
                                    /* traversal_order
                                                            */
     INTERSECTION,
                                    /* confluence
                                                            */
```




*/

*/

*/

*/

*/

*/

*/

*/

*/

*/

Step 1: Specifying Available Expressions Analysis

```
struct gimple_pfbv_dfa_spec gdfa_ave =
ł
     entity_expr,
                                   /* entity
                                   /* top_value
     ONES,
     ZEROS,
                                   /* entry_info
     ONES,
                                   /* exit_info
     FORWARD,
                                   /* traversal_order
     INTERSECTION,
                                   /* confluence
                                   /* gen_effect
     entity_use,
     down_exp,
                                   /* gen_exposition
                                   /* kill_effect
     entity_mod,
                                   /* kill_exposition
     any_where,
```



*/

*/

*/

*/

*/

*/

*/

*/

*/

*/

*/

Step 1: Specifying Available Expressions Analysis

```
struct gimple_pfbv_dfa_spec gdfa_ave =
ł
     entity_expr,
                                   /* entity
                                   /* top_value
     ONES,
     ZEROS,
                                   /* entry_info
     ONES,
                                   /* exit_info
     FORWARD,
                                   /* traversal_order
     INTERSECTION,
                                   /* confluence
                                   /* gen_effect
     entity_use,
     down_exp,
                                   /* gen_exposition
                                   /* kill_effect
     entity_mod,
                                   /* kill_exposition
     any_where,
     global_only,
                                   /* preserved_dfi
```



Step 1: Specifying Available Expressions Analysis

```
struct gimple_pfbv_dfa_spec gdfa_ave =
ł
     entity_expr,
                                   /* entity
                                                          */
                                   /* top_value
                                                          */
     ONES,
     ZEROS,
                                   /* entry_info
                                                          */
     ONES,
                                   /* exit_info
                                                          */
     FORWARD,
                                   /* traversal_order
                                                          */
     INTERSECTION,
                                   /* confluence
                                                          */
                                   /* gen_effect
                                                          */
     entity_use,
                                   /* gen_exposition
     down_exp,
                                                          */
                                   /* kill_effect
                                                          */
     entity_mod,
                                   /* kill_exposition
     any_where,
                                                          */
     global_only,
                                   /* preserved_dfi
                                                          */
     identity_forward_edge_flow,
                                   /* forward_edge_flow
                                                          */
     stop_flow_along_edge,
                                   /* backward_edge_flow */
     forward_gen_kill_node_flow,
                                   /* forward_node_flow
                                                          */
     stop_flow_along_node
                                   /* backward_node_flow */
};
```



July 09

Step 2: Implementing Available Expressions Analysis Pass



Step 3.1: Declaring the Available Expressions Analysis Pass

```
struct tree_opt_pass pass_gimple_pfbv_ave_dfa =
ł
  "gdfa_ave",
                          /* name */
 NULL,
                          /* gate */
 gimple_pfbv_ave_dfa,
                          /* execute */
 NULL,
                          /* sub */
 NULL,
                          /* next */
 0,
                          /* static_pass_number */
 0,
                          /* tv id */
                          /* properties_required */
 0,
 0,
                          /* properties_provided */
 0,
                          /* properties_destroyed */
                          /* todo_flags_start */
 0,
                          /* todo_flags_finish */
 0,
                          /* letter */
 0
};
```

July 09

Step 3.2: Registering the Available Expressions Analysis Pass

In file file tree-pass.h

extern struct tree_opt_pass pass_gimple_pfbv_ave_dfa;



28/37

Step 3.3: Positioning the Pass

In function init_optimization_passes in file passes.c.

```
NEXT_PASS (pass_build_cfg);
/* Intraprocedural dfa passes begin */
NEXT_PASS (pass_init_gimple_pfbvdfa);
NEXT_PASS (pass_gimple_pfbv_ave_dfa);
```



29/37

Specifying Live Variables Analysis

- Entity should be entity_var
- \top , *BIStart* and *BIEnd* should be ZEROS
- Direction should be BACKWARD
- Confluence should be UNION
- Exposition should be up_exp
- Forward edge flow should be stop_flow_along_edge
- Forward node flow should be stop_flow_along_node
- Backward edge flow should be identity_backward_edge_flow
- Backward node flow should be backward_gen_kill_node_flow



Part 7

gdfa: Design and Implementation

◆□▶ ◆□▶ ◆臣▶ ◆臣▶ 臣 のへで

Specification Data Structure

```
struct gimple_pfbv_dfa_spec
{
```

```
entity_name
initial_value
initial_value
traversal_direction
meet_operation
```

```
entity;
top_value_spec;
entry_info;
exit_info;
traversal_order;
confluence;
```

Essential Abstrations in GCC



Specification Data Structure

```
struct gimple_pfbv_dfa_spec
{
```

```
entity_name
initial_value
initial_value
traversal_direction
meet_operation
entity_manipulation
entity_occurrence
entity_manipulation
entity_occurrence
```

entity; top_value_spec; entry_info; exit_info; traversal_order; confluence; gen_effect; gen_exposition; kill_effect; kill_exposition;

};

30/37

Specification Data Structure

```
struct gimple_pfbv_dfa_spec
{
```

```
entity_name
                          entity;
initial_value
                          top_value_spec;
initial_value
                          entry_info;
initial_value
                          exit_info;
traversal_direction
                          traversal_order;
meet_operation
                          confluence;
entity_manipulation
                          gen_effect;
entity_occurrence
                          gen_exposition;
entity_manipulation
                          kill_effect;
                          kill_exposition;
entity_occurrence
dfi_to_be_preserved
                          preserved_dfi;
dfvalue (*forward_edge_flow)(basic_block src, basic_block dest)
dfvalue (*backward_edge_flow) (basic_block src, basic_block dest)
dfvalue (*forward_node_flow)(basic_block bb);
dfvalue (*backward_node_flow)(basic_block bb);
```

};

Specification Primitives

| Enumerated Type | Possible Values |
|---------------------|---|
| entity_name | <pre>entity_expr, entity_var, entity_defn</pre> |
| initial_value | ONES, ZEROS |
| traversal_direction | FORWARD, BACKWARD, BIDIRECTIONAL |
| meet_operation | UNION, INTERSECTION |
| entity_manipulation | <pre>entity_use, entity_mod</pre> |
| entity_occurrence | up_exp, down_exp, any_where |
| dfi_to_be_preserved | all, global_only, no_value |



Pre-Defined Edge Flow Functions

• Edge Flow Functions

| Edge Flow Function | Returned value |
|---|------------------|
| <pre>identity_forward_edge_flow(src, dest)</pre> | CURRENT_OUT(src) |
| <pre>identity_backward_edge_flow(src, dest)</pre> | CURRENT_IN(dest) |
| <pre>stop_flow_along_edge(src, dest)</pre> | top_value |



Pre-Defined Edge Flow Functions

Edge Flow Functions

| Edge Flow Function | Returned value |
|---|------------------|
| <pre>identity_forward_edge_flow(src, dest)</pre> | CURRENT_OUT(src) |
| <pre>identity_backward_edge_flow(src, dest)</pre> | CURRENT_IN(dest) |
| <pre>stop_flow_along_edge(src, dest)</pre> | top_value |

Node Flow Functions

| Node Flow Function | Returned value |
|--|--|
| identity_forward_node_flow(bb) | CURRENT_IN(bb) |
| <pre>identity_backward_node_flow(bb)</pre> | CURRENT_OUT(bb) |
| <pre>stop_flow_along_node(bb)</pre> | top_value |
| forward_gen_kill_node_flow(bb) | CURRENT_GEN(bb) ∪ (CURRENT_IN(bb) - CURRENT_KILL(bb)) |
| backward_gen_kill_node_flow(bb) | CURRENT_GEN(bb) ∪ (CURRENT_OUT(bb) - CURRENT_KILL(bb)) |

Essential Abstrations in GCC

GCC Resource Center, IIT Bombay



33/37

The Generic Driver for Global Data Flow Analysis

```
pfbv_dfi ** gdfa_driver(struct gimple_pfbv_dfa_spec dfa_spec)
{    if (find_entity_size(dfa_spec) == 0) return NULL;
    initialize_special_values(dfa_spec);
    create_dfi_space();
    traversal_order = dfa_spec.traversal_order;
    confluence = dfa_spec.confluence;
```

```
local_dfa(dfa_spec);
```

```
forward_edge_flow = dfa_spec.forward_edge_flow;
backward_edge_flow = dfa_spec.backward_edge_flow;
forward_node_flow = dfa_spec.forward_node_flow;
backward_node_flow = dfa_spec.backward_node_flow;
perform_pfbvdfa();
```

```
preserve_dfi(dfa_spec.preserved_dfi);
return current_pfbv_dfi;
```



}

• The Main Difficulty: Interface with the intermediate representation details



- The Main Difficulty: Interface with the intermediate representation details
- State of Art: The user is expected to supply the flow function implementation



- The Main Difficulty: Interface with the intermediate representation details
- State of Art: The user is expected to supply the flow function implementation
- Our Key Ideas:
 - ► Local data flow analysis is a special case of global data flow analysis Other than the start and end blocks (≡ statements), every block has just one predecessor and one successor



- The Main Difficulty: Interface with the intermediate representation details
- State of Art: The user is expected to supply the flow function implementation
- Our Key Ideas:
 - ► Local data flow analysis is a special case of global data flow analysis Other than the start and end blocks (≡ statements), every block has just one predecessor and one successor
 - ConstGen_n and ConstKill_n are just different names given to particular sets of entities accumulated by traversing these basic blocks



• Traverse statements in a basic block in appropriate order

| Exposition | Direction | |
|------------|------------|--|
| up_exp | backward | |
| down_exp | forward | |
| any_where | don't care | |

- Solve the recurrence
 - accumulated_entities = (accumulated_entities
 - remove_entities)
 - $\cup \, \texttt{add_entities}$



Entity is entity_expr.

| Exposition | Manipulation | a = b * c | | b = b * c | |
|------------|--------------|-----------|--------|-----------|--------|
| | | add | remove | add | remove |
| upwards | use | | | | |
| downwards | use | | | | |
| upwards | modification | | | | |
| downwards | modification | | | | |



Entity is entity_expr.

| Exposition | Manipulation | a = b * c | | b = b * c | |
|------------|--------------|-----------|--------|-----------|--------|
| | | add | remove | add | remove |
| upwards | use | b * c | | | |
| downwards | use | | | | |
| upwards | modification | | | | |
| downwards | modification | | | | |



Entity is entity_expr.

| Exposition | Manipulation | a = b * c | | b = b * c | |
|------------|--------------|-----------|---------|-----------|--------|
| | | add | remove | add | remove |
| upwards | use | b * c | expr(a) | | |
| downwards | use | | | | |
| upwards | modification | | | | |
| downwards | modification | | | | |



Entity is entity_expr.

| Exposition | Manipulation | a = b * c | | b = b * c | |
|------------|--------------|-----------|---------|-----------|--------|
| | | add | remove | add | remove |
| upwards | use | b * c | expr(a) | b * c | |
| downwards | use | | | | |
| upwards | modification | | | | |
| downwards | modification | | | | |



Entity is entity_expr.

| Exposition | Manipulation | a = b * c | | b = b * c | |
|------------|--------------|-----------|---------|-----------|---------|
| | | add | remove | add | remove |
| upwards | use | b * c | expr(a) | b * c | expr(b) |
| downwards | use | | | | |
| upwards | modification | | | | |
| downwards | modification | | | | |



Entity is entity_expr.

| Exposition | Manipulation | a = b * c | | b = b * c | |
|------------|--------------|-----------|---------|-----------|---------|
| | | add | remove | add | remove |
| upwards | use | b * c | expr(a) | b * c | expr(b) |
| downwards | use | b * c | | | |
| upwards | modification | | | | |
| downwards | modification | | | | |



Entity is entity_expr.

| Exposition | Manipulation | a = | a = b * c | | b = b * c | |
|------------|--------------|-------|-----------|-------|-----------|--|
| | | add | remove | add | remove | |
| upwards | use | b * c | expr(a) | b * c | expr(b) | |
| downwards | use | b * c | expr(a) | | | |
| upwards | modification | | | | | |
| downwards | modification | | | | | |



Entity is entity_expr.

| Exposition | Manipulation | a = b * c b | | b = b | = b * c | |
|------------|--------------|---------------|---------|--------|---------|--|
| | Manipulation | add | remove | remove | | |
| upwards | use | b * c | expr(a) | b * c | expr(b) | |
| downwards | use | b * c | expr(a) | Ø | | |
| upwards | modification | | | | | |
| downwards | modification | | | | | |



Entity is entity_expr.

| Exposition | Manipulation | a = b * c | | b = b * c | |
|------------|--------------|-----------|---------|-----------|---------|
| | manipulation | add | remove | add | remove |
| upwards | use | b * c | expr(a) | b * c | expr(b) |
| downwards | use | b * c | expr(a) | Ø | expr(b) |
| upwards | modification | | | | |
| downwards | modification | | | | |



Entity is entity_expr.

| Exposition | Manipulation | a = b * c | | b = b * c | |
|------------|--------------|-----------|----------|-----------|---------|
| | Manipulation | add | d remove | add | remove |
| upwards | use | b * c | expr(a) | b * c | expr(b) |
| downwards | use | b * c | expr(a) | Ø | expr(b) |
| upwards | modification | expr(a) | | | |
| downwards | modification | | | | |



Entity is entity_expr.

| Exposition | Manipulation | a = b * c | | b = b * c | |
|------------|--------------|-----------|---------|-----------|---------|
| | Manipulation | add | remove | add | remove |
| upwards | use | b * c | expr(a) | b * c | expr(b) |
| downwards | use | b * c | expr(a) | Ø | expr(b) |
| upwards | modification | expr(a) | b * c | | |
| downwards | modification | | | | |



Entity is entity_expr.

| Exposition | Manipulation | a = b * c $b = b$ | |) * C | |
|------------|--------------|-------------------|------------|-----------------------|---------|
| | Manipulation | add | add remove | | remove |
| upwards | use | b * c | expr(a) | b * c | expr(b) |
| downwards | use | b * c | expr(a) | Ø | expr(b) |
| upwards | modification | expr(a) | b * c | $\exp(b) - \{b * c\}$ | |
| downwards | modification | | | | |



Entity is entity_expr.

| Exposition | Manipulation | a = b * c $b = b$ | |) * C | |
|------------|--------------|-------------------|------------|-----------------------|---------|
| | Manipulation | add | remove add | add | remove |
| upwards | use | b * c | expr(a) | b * c | expr(b) |
| downwards | use | b * c | expr(a) | Ø | expr(b) |
| upwards | modification | expr(a) | b * c | $\exp(b) - \{b * c\}$ | b * c |
| downwards | modification | | | | |



Entity is entity_expr.

| Exposition | Manipulation | a = b * c $b = b$ | |) * C | |
|------------|--------------|-------------------|---------|-----------------------|---------|
| | Manipulation | add | remove | add | remove |
| upwards | use | b * c | expr(a) | b * c | expr(b) |
| downwards | use | b * c | expr(a) | Ø | expr(b) |
| upwards | modification | expr(a) | b * c | $\exp(b) - \{b * c\}$ | b * c |
| downwards | modification | expr(a) | | | |



Entity is entity_expr.

| Exposition | Manipulation | a = b * c $b = b$ | |) * C | |
|------------|--------------|-------------------|---------|-----------------------|---------|
| | Manipulation | add | remove | add | remove |
| upwards | use | b * c | expr(a) | b * c | expr(b) |
| downwards | use | b * c | expr(a) | Ø | expr(b) |
| upwards | modification | expr(a) | b * c | $\exp(b) - \{b * c\}$ | b * c |
| downwards | modification | expr(a) | b * c | | |


Example for Available Expressions Analysis

Entity is entity_expr.

Let expr(x) denote the set of all expressions of x

| Exposition | Manipulation | a = b * c | | b = b * c | |
|------------|--------------|-----------|---------|-----------------------|---------|
| | | add | remove | add | remove |
| upwards | use | b * c | expr(a) | b * c | expr(b) |
| downwards | use | b * c | expr(a) | Ø | expr(b) |
| upwards | modification | expr(a) | b * c | $\exp(b) - \{b * c\}$ | b * c |
| downwards | modification | expr(a) | b * c | expr(b) | |



Example for Available Expressions Analysis

Entity is entity_expr.

Let expr(x) denote the set of all expressions of x

| Exposition | Manipulation | a = b * c | | b = b * c | |
|------------|--------------|-----------|---------|-----------------------|---------|
| | | add | remove | add | remove |
| upwards | use | b * c | expr(a) | b * c | expr(b) |
| downwards | use | b * c | expr(a) | Ø | expr(b) |
| upwards | modification | expr(a) | b * c | $\exp(b) - \{b * c\}$ | b * c |
| downwards | modification | expr(a) | b * c | expr(b) | Ø |



Example for Available Expressions Analysis

Entity is entity_expr.

Let expr(x) denote the set of all expressions of x

| Exposition | Manipulation | a = b * c | | b = b * c | |
|------------|--------------|-----------|---------|-----------------------|---------|
| | | add | remove | add | remove |
| upwards | use | b * c | expr(a) | b * c | expr(b) |
| downwards | use | b * c | expr(a) | Ø | expr(b) |
| upwards | modification | expr(a) | b * c | $\exp(b) - \{b * c\}$ | b * c |
| downwards | modification | expr(a) | b * c | expr(b) | Ø |

Note: In the case of modifications, if we first add then remove the entities modication, the set difference is not required



Future Work

37/37

Main thrust

- Supporting general data flow frameworks
- Supporting interprocedural analysis

