Workshop on Essential Abstractions in GCC

Introduction to Parallelization and Vectorization

GCC Resource Center (www.cse.iitb.ac.in/grc)

Department of Computer Science and Engineering, Indian Institute of Technology, Bombay



3 July 2011

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	Outline			Outline	
Trans	formation for parallel and vector execution		S		
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• Data (dependence		t		







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The Scope of this Tutorial

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The Scope of this Tutorial

- What this tutorial does not address
 - Algorithms used for parallelization and vectorization
 - Code or data structures of the parallelization and vectorization pass of GCC
 - Machine level issues related to parallelization and vectorization
- What this tutorial addresses

Basics of Discovering Parallelism using GCC

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Part 1

Transformations for Parallel and Vector Execution Notes

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A Taxonomy of Parallel Computation

	Single Program	Multiple Programs
Single Data	SPSD	MPSD
Multiple Data	SPMD	MPMD

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and Vectorization 3/28 A Taxonomy of Parallel Computation

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	Single I	Single Program	
	Single Instruction	Multiple Instructions	Multiple Programs
Single Data	SISD	MISD	MPSD
Multiple Data	SIMD	MIMD	MPMD





	Single Program			
	Single Instruction	Multiple Instructions	Multiple Programs	
Single Data	SISD	?	?	
Multiple Data	SIMD	MIMD	MPMD	

Redundant computation for validation of intermediate steps



A Taxonomy of Parallel Computation



Transformations performed by a compiler



A Taxonomy of Parallel Computation

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Vectorization: SISD \Rightarrow SIMD

• Parallelism in executing operation on shorter operands (8-bit, 16-bit, 32-bit operands)

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• Existing 32 or 64-bit arithmetic units used to perform multiple operations in parallel

A 64 bit word \equiv a vector of 2×(32 bits), 4×(16 bits), or 8×(8 bits)

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Data Dependence

Let statements S_i and S_i access memory location m at time instants tand t + k

Access in S_i	Access in S_j	Dependence	Notation
Read <i>m</i>	Write <i>m</i>	Anti (or Pseudo)	$S_i \ \overline{\delta} \ S_j$
Write <i>m</i>	Read <i>m</i>	Flow (or True)	$S_i \delta S_j$
Write <i>m</i>	Write <i>m</i>	Output (or Pseudo)	$S_i \delta^O S_j$
Read <i>m</i>	Read <i>m</i>	Does not matter	

- Pseudo dependences may be eliminated by some transformations
- True dependence prohibits parallel execution of S_i and S_i



Consider dependence between statements S_i and S_i in a loop

- Loop independent dependence. t and t + k occur in the same iteration of a loop
 - S_i and S_i must be executed sequentially
 - Different iterations of the loop can be parallelized
- Loop carried dependence. t and t + k occur in the different iterations of a loop
 - Within an iteration, S_i and S_j can be executed in parallel
 - Different iterations of the loop must be executed sequentially
- S_i and S_i may have both loop carried and loop independent dependences

Data Dependence

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Dependence in Example 3

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Dependence in Example 3

• Program

int A[N], B[N], i; for (i=0; i<N; i++) A[i+1] = A[i] + B[i+1]; /* S1 */</pre>

• Dependence graph

$$S_1$$
 δ_1

• Loop carried flow-dependence Neither parallelization not vectorization is possible

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RHS

0,0

0, 1

0.2

0.3

1.0

1, 1

1,2

1,3

2,0

2, 1

2,2

2,3

3,0

3, 1

3,2

3,3

LHS

1,0

1, 1

1,2

1.3

2,0

2, 1

2,2

2,3

3,0

3, 1

3,2

3,3

4,0

4, 1

4,2

4,3

1,3

2,0

2, 1

2,2

2,3

3,0

3, 1

3,2

3,3

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	Iteration Vectors and Index Vectors: Example 1	
	Iteration Index Vector	

Loop carried dependence exists if

- there are two distinct iteration vectors such that
- the index vectors of LHS and RHS are identical

Conclusion: Dependence exists

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3 July 2011 intro-par-vect: Introduction to Parallelization and Vectorization 17/28 Iteration Vectors and Index Vectors: Example 1





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Iteration Vectors and Index Vectors: Example 2



	Vector	LHS	RHS
for (i=0, i<4; i++)	0,0	0,0	0,0
for (j=0; j<4; j++)	0, 1	0, 1	0,1
{	0,2	0,2	0,2
a[i][i] = a[i][i] + 2	0,3	0,3	0,3
۵ <u>(۱)</u> ۵ <u>(۱)</u> ۲,	1, 0	1, 0	1,0
ſ	1,1	1,1	1,1
	1,2	1,2	1,2
Loop carried dependence exists if	1,3	1,3	1,3
Loop carried dependence exists in	2,0	2,0	2,0
 there are two distinct iteration 	2,1	2, 1	2,1
vectors such that	2,2	2,2	2,2
 the index vectors of LHS and RHS 	2,3	2,3	2,3
are identical	3,0	3,0	3,0
	3,1	3, 1	3,1
Conclusion: No dependence	3,2	3,2	3,2
	3,3	3,3	3,3
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	Example 4: Dependence	





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	Example 4: Dependence	

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Example 4: Dependence



Loop independent anti dependence due to A[i]







Loop independent anti dependence due to B[i]



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Example 4: Dependence

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	Example 4: Dependence	



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Example 4: Dependence



Loop independent flow dependence due to T



Example 4: Dependence



Loop carried anti dependence due to T



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Example 4: Dependence

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Example 4: Dependence

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Example 4: Dependence



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Loop carried output dependence due to T









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Example 4: Dependence

Example 4: Dependence



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Tutorial Problem for Discovering Dependence

Draw the dependence graph for the following program (Earlier program modified to swap 2-dimensional arrays)

for {	(i=0; i <n; i++)<="" th=""><th></th><th></th></n;>		
	for (j=0; j <n; j++)<="" td=""><td></td><td></td></n;>		
	$\{ T = A[i][j]; \}$	/* S1 */	
	A[i][j] = B[i][j]	; /* S2 */	
	B[i][j] = T;	/* S3 */	
	}		
}			







There exists a dependence from statement S_1 to statement S_2 in common nest of loops if and only if there exist two iteration vectors **i** and **j** for the nest, such that

- 1. $\mathbf{i} < \mathbf{j}$ or $\mathbf{i} = \mathbf{j}$ and there exists a path from S₁ to S₂ in the body of the loop,
- 2. statement S_1 accesses memory location M on iteration **i** and statement S_2 accesses location M on iteration \mathbf{j} , and
- 3. one of these accesses is a write access.

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intro-par-vect: Introduction to Parallelization and Vectorization **Tutorial Problem for Discovering Dependence**

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Conjunction of Dependences and Vectorization

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Cyclic Dependency and Vectorization

Conjunction of Dependences and Vectorization





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	Cyclic Dependency and Vectorization	

Cyclic True Dependence	Cyclic Anti Dependence
<pre>int A[N], B[N], i; for (i=0; i<n; i++)="" {<br="">B[i+2] = A[i]; A[i+1] = B[i];</n;></pre>	<pre>int A[N], B[N], i; for (i=0; i<n; i++)="" {<br="">B[i] = A[i+1]; A[i] = B[i+2];</n;></pre>
}	}

Rescheduling of statements will not break the cyclic dependency - cannot vectorize

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Last but not the least

Thank You!



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