Probabilistic Robust Query Optimization

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Outline

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Making Uncertainty Explicit

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Related Work [Chu et al, 2002]

Conclusion



Motivation

Current focus of optimizers is on the best plan possible

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- However, consistency and predictability is ignored
- Also, cardinality estimation errors might exist

Current issues

- Attribute Value Independence(AVI) assumption rarely holds
- ▶ Problems with many dimensions("Curse of Dimensionality")

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Performance v/s Predictability

- Some plans might always be slow (e.g. Sequential Scans)
- Others, might be fast for some range of selectivities, slow otherwise (e.g. Algorithms related to indexes)
- Ideally, the user should be free to decide what he wants

Solving the uncertainty problem

- Rather than giving point estimates, probaility distributions would be a better idea
- > Then, select plan with least expected cost, not just least cost

 Can just call the optimizer several times for different selectivities, a waste of time

Incorporating the Probability Distribution

- How do we decide between 2 plans given their probability distributions?
- ► User decides on performance v/s predictability
- User specifies confidence threshold X%
- \blacktriangleright The plan is picked which has lower cost X% of the time

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Selectivity Estimation via Sampling

- Use precomputed random samples to guess the probability distribution for the selectivity
- For joins create "Join Synopses" (limited to joins on foreign keys)

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Avoids build-up of estimation errors due to AVI

Join Synopses

- ▶ The join synopsis for a relation R is constructed as follows:
 - 1. Construct a uniform random sample from R
 - 2. For every relation S such that R has a foreign key to S, join the sample of R with S

- 3. Repeat step 2 recursively
- This is performed while updating statistics

Deriving the Probability Distribution

- We use Bayes' rule to estimate the probability of a predicate succeeding given the observations on the sample set, X, a vector ⟨x₁, x₂,..., x_n⟩
- The equation becomes:

$$f(z|X) = \frac{P[X|p=z]f(z)}{\int_0^1 P[X|p=y]f(y)dy}$$
(1)

 f(z) is not always given. We can estimate it given the workload, or use the uniform prior i.e. f(z) = 1 or Jeffreys' prior i.e. f(z) ∝ z^{-1/2}(1 − z)^{-1/2}

Deriving the Probability Distribution(contd.)

- Suppose k tuples satisfy the predicate
- The fraction of tuples satisfying the predicate is p, and that of those that don't is 1 - p
- The variables x_i are independent and identically distributed Bernoulli random variables, so Pr[X|p = z] = z^k(1 - z)^{n-k}
- Combining the above equation with f(z) = 1, we get

$$f(z|X) = \frac{z^k (1-z)^{n-k}}{\int_0^1 y^k (1-y)^{n-k} dy}$$
(2)

- The denominator is independent of z, and may be treated as a normalizing constant
- ► Thus, it is the beta distribution with parameters (k + 1, n - k + 1)

The estimation procedure

- The estimation procedure can be summed up as follows:
 - 1. Select the correct sample based on relations present in the query
 - 2. Evaluate the predicate on the sample and use Bayes' rule to infer probability distribution
 - 3. Choose confidence threshold, T based on user preference, and assign $s = cdf^{-1}(T)$

4. Return s as the selectivity for the predicate

The estimation procedure (contd.)

- ► T will be smaller if the user prefers a more aggressive approach, larger for a more predictive approach
- Sample size is most important factor in determining the distribution.

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Building the Analytical model

- Consider a query Q, with 2 possible plans P₁ and P₂, running on a table with N rows
- Either plan may be optimal given the selectivity of the query
- ► We assume a linear cost model of the form v_ix + f_i for plan P_i, with v_i being the cost per tuple and f_i, the fixed overhead per execution

Analytical results



Figure: Confidence Threshold effect



Figure: Performance v/s Predictability



Figure: Effect of Sample Size



Figure: Crossover point at high selectivity

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Experimental results





Figure: Selectivity v/s Time

Figure: Performance v/s Predictability

Figure: Results for a query with 2 predicates



Figure: Effect of varying sample size

Related Work [Chu et al, 2002]

- [Chu et al, 2002] also looks at using Least Expected Cost(LEC)
- It is shown that LEC can be applied not just to cost functions related to running time, but also to more general cost functions
- In addition, the conditions under which current optimizers can produce LEC plans are investigated

When do we get LEC plans

- We can obtain LEC plans if there exists a parameter setting that gives an LEC plan
- Some conditions help us find such a parameter efficiently, such as
 - The presence of a dominant plan
 - The cost of a plan being linear in the parameters of interest
 - The cost of a plan being the sum of products of independent parameters

 Parameters that don't fit these criteria can be transformed so that they do

More general cost functions

 Cost functions that aren't necessarily a function of running time can be easily evaluated using LEC

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However, current optimizers can't be used

Least expected user cost query optimization

- Dynamic programming algorithms like System R are considered
- If the cost function is additive, an LEC plan is produced

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- Can modify System R to produce LEC plan
- Can also include variance in the cost function

Conclusion

- Estimation of cardinality distribution using random sampling of relation
- User-defined threshold decides cardinality estimate for optimization
- However, evaluated only for limited conditions
- Might be possible to use LEC optimization with current techniques, but only in some cases

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