

CS 344

Artificial Intelligence

By Prof: Pushpak Bhattacharya

Class on 15/Mar/2007

# Fuzzy Inferencing

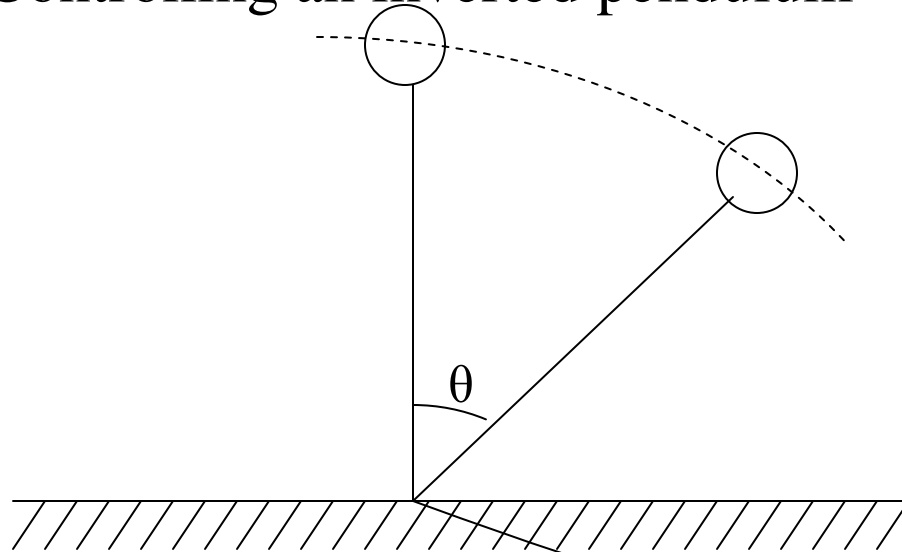
## Core

The Lukasiewicz rule

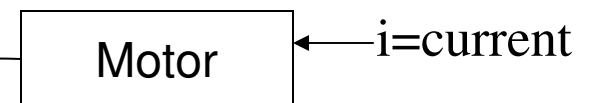
$$t(P \rightarrow Q) = \min[1, 1 + t(P) - t(Q)]$$

## An example

Controlling an inverted pendulum



$$\dot{\theta} = d\theta / dt = \text{angular velocity}$$



The goal: To keep the pendulum in vertical position ( $\theta=0$ ) in dynamic equilibrium. Whenever the pendulum departs from vertical, a torque is produced by sending a current 'i'

Controlling factors for appropriate current

Angle  $\theta$ , Angular velocity  $\dot{\theta}$

Some intuitive rules

If  $\theta$  is +ve small and  $\dot{\theta}$  is -ve small

then current is zero

If  $\theta$  is +ve small and  $\dot{\theta}$  is +ve small

then current is -ve medium

# Control Matrix

$\theta \backslash \dot{\theta}$	-ve med	-ve small	Zero	+ve small	+ve med	
-ve med						
-ve small		+ve med	+ve small	Zero		
Zero		+ve small	Zero	-ve small		
+ve small		Zero	-ve small	-ve med		
+ve med						

Region of interest



Each cell is a rule of the form

If  $\theta$  is  $\langle \rangle$  and  $\dot{\theta}$  is  $\langle \rangle$

then  $i$  is  $\langle \rangle$

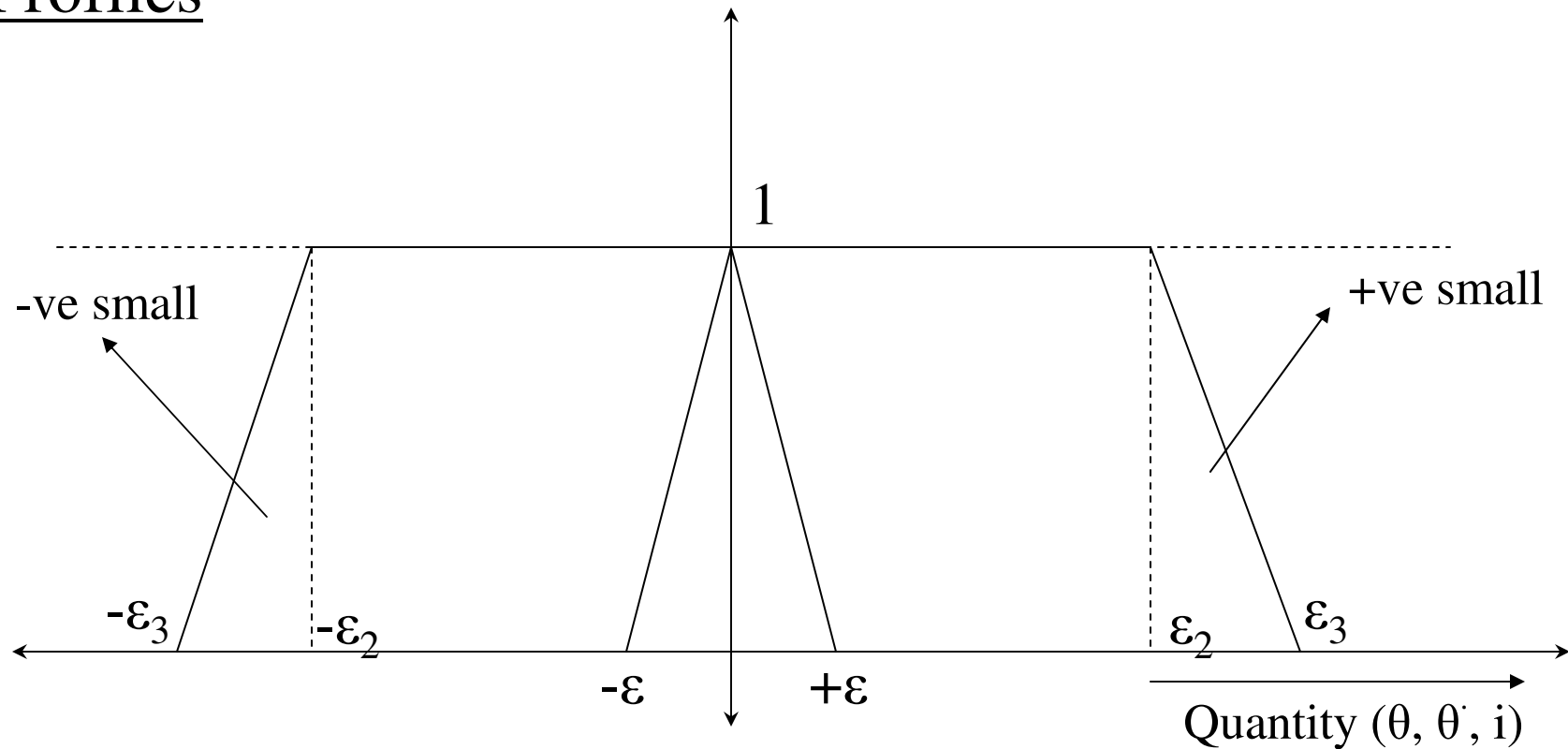
#### 4 “Centre rules”

1. if  $\theta = = \text{Zero}$  and  $\dot{\theta} = = \text{Zero}$  then  $i = \text{Zero}$
2. if  $\theta$  is +ve small and  $\dot{\theta} = = \text{Zero}$  then  $i$  is -ve small
3. if  $\theta$  is -ve small and  $\dot{\theta} = = \text{Zero}$  then  $i$  is +ve small
4. if  $\theta = = \text{Zero}$  and  $\dot{\theta}$  is +ve small then  $i$  is -ve small
5. if  $\theta = = \text{Zero}$  and  $\dot{\theta}$  is -ve small then  $i$  is +ve small

# Linguistic variables

1. Zero
2. +ve small
3. -ve small

## Profiles



# Inference procedure

1. Read actual numerical values of  $\theta$  and  $\theta'$
2. Get the corresponding  $\mu$  values  $\mu_{\text{Zero}}$ ,  $\mu_{(+ve \text{ small})}$ ,  $\mu_{(-ve \text{ small})}$ . This is called FUZZIFICATION
3. For different rules, get the fuzzy I-values from the R.H.S of the rules.
4. “Collate” by some method and get ONE current value. This is called DEFUZZIFICATION
5. Result is one numerical value of ‘i’.