# Scheduling Messages with Deadlines in Multi-hop Real-time Sensor Networks [*]

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## Abstract

*Consider a team of robots equipped with sensors that collaborate with one another to achieve a common goal. Sensors on robots produce periodic updates that must be transmitted to other robots and processed in real-time to enable such collaboration. Since the robots communicate with one another over an ad-hoc wireless network, we consider the problem of providing timeliness guarantees for multi-hop message transmissions in such a network. We derive the effective deadline and the latest start time for per-hop message transmissions from the validity intervals of the sensor data and the constraints imposed by the consuming task at the destination. Our technique schedules messages by carefully exploiting spatial channel reuse for each per-hop transmission to avoid MAC layer collisions, so that deadline misses are minimized. Extensive simulations show the effectiveness of our channel reuse-based SLF (smallest latest-start-time first) technique when compared to a simple per-hop SLF technique, especially at moderate to high channel utilization or when the probability of collisions is high.*

## 1 Introduction

Wireless sensor networks have received increased research attention in recent years. Emerging sensor applications include habitat monitoring, pollution detection, weather forecasting, and monitoring disasters such as earthquakes, fires and floods. In many applications, sensor data must be delivered with time constraints so that appropriate actions taken in real-time [18].

Consider the scenario where a group of robots are searching for people trapped inside a building on fire. Each robot is equipped with numerous devices such as camera, temperature, pressure, location, and infrared sensors. The robots communicate with one another over an ad-hoc wireless network and collaborate as a team to achieve their common goal. For instance, the robots need to pool sensory information to determine, in real-time, where to move individually and collectively. Further, if an object of interest is discovered by one robot, the discovery must be transmitted to the outside world in real-time, together with other information such as the location and the temperature map of the area. However, existing wireless protocols such as 802.11b do not provide timeliness guarantees on network transmissions due to packet collisions, exponential back-offs, and the false blocking problem [16].

In this paper, we focus on the problem of providing timeliness guarantees for multi-hop transmissions in a real-time robotic sensor application. In such applications, each message is associated with a deadline and may need to traverse multiple hops from the source to the destination. Message deadlines are derived from the validity of the accompanying sensor data and the start time of the consuming task at the destination. We show that the problem of meeting message deadlines is NP-hard even for single hop message transmissions. Consequently, we propose heuristics for online scheduling of messages with deadline constraints. Our technique (i) schedules messages based on their per-hop timeliness constraints, (ii) carefully exploits spatial reuse of the wireless channel and (iii) explicitly avoids collisions to reduce deadline misses. We evaluate our technique using simulations of various robot topologies and examine the impact of various system and sensor parameters on meeting timeliness constraints. Our results show that: the channel-reuse-based algorithm outperforms the CSMA/CA-based algorithm for a wide variety of experimental settings, and especially when (i) the channel utilization (the fraction of bandwidth the wireless channel is busy over a time interval) is high, (ii) the interference range is large, or (iii) the probability of collisions is high.

Spatial channel reuse in ad-hoc networks has been studied from the perspective of minimizing the total transmis-

sion time [8], or improving channel utilization, through-put and fairness [11, 12]. However, using spatial reuse to address the problem of meeting real-time constraints for multi-hop messages has not been studied, especially for sensor communication. A detailed comparison with related research efforts is presented in Section 6.

The remainder of this paper is structured as follows. Section 2 presents the application background, our system model and the problem formulation. Section 3 discusses the design issues for scheduling messages with deadlines. Section 4 describes our scheduling heuristics in detail. Experimental results are presented in Section 5, and finally, we address related work and summarize our work in Sections 6 and 7.

## 2 Background, System Model and Problem Formulation

### 2.1 Application Background

Consider a team of robots that collaborate to achieve a common task, such as searching for trapped people in a building on fire, exploring the territory of Mars, or building a map of an unknown environment. The robots are equipped with numerous sensors such as camera, temperature, pressure, infrared sensors, and positioning devices. Due to energy and weight considerations, each robot may only carry a subset of the sensors and needs to communicate with other robots for other sensor readings. Each robot is also equipped with a wireless connectivity, and the robots communicate with one another over an ad-hoc network. Due to the finite transmission range of the wireless, if a destination robot is not within the effective range of the sender, a sensor message will need to traverse through intermediate robots to reach its destination.

To achieve their common goal, each robot in the team may be assigned one or more tasks. For instance, a robot that is assigned the task of generating an up-to-date temperature map of the fire will need to periodically receive temperature readings from other robots along with their locations. Robotic teams are typically organized as *leader-follower* groups [20], where the leader robot is designed with a task of determining a "plan" for the team at each step. A plan consists of two components: a communication plan and a path plan. Communication plan tells the robots who is talking to whom; path plan tells robots where to move next.

To compute a plan, the leader takes into account (i) the current positions of follower robots, (ii) the overall goal and (iii) all "important" sensor readings that have been reported (e.g., smoke in a certain area). Each time when a new plan is constructed, it is conveyed to the follower robots which then exchange messages according to the communication plan and move according to the path plan (see Figure 1). In this
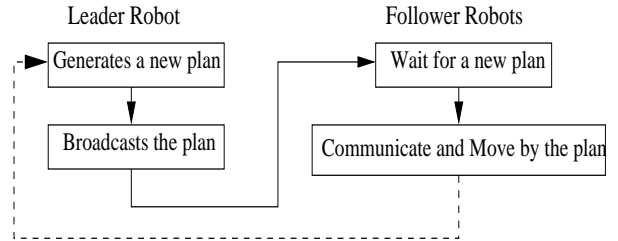


**Figure 1. Plan generation and execution**

model, actions required for (1) communicating the plan, (2) transmitting sensor updates, and (3) sending required sensor values, if any, back to the leader to create a new plan are the three components of the constructed plan. Thus, plans need to be computed in real-time to enable the robots to move continuously and communicate in real-time.

### 2.2 Data Validity and Transmission Deadlines

In real-time sensor applications, the values of sensor data reflect the current state of the environment. Since the environment may be constantly changing, sensor readings have a temporal interval for which they are valid. For instance, the temperature readings from a few minutes back are no longer valid if the fire in a room burns out of control. We use the term *data validity* to define the time interval for which a data value produced by a sensor is valid.

In this work, we assume that sensors produce data periodically, determined by the *sensor period*. Each data value is propagated from the source robot to one or more destination robots for processing. Each value has a data validity interval associated with it, and the value must reach the destination before the validity interval expires. Further, the sensor message must arrive at the destination before the start time of the consuming task that consumes it. Thus, the effective deadline of a sensor message is the minimum of the data validity deadline and the start time of the consuming task. Formally, if a sensor value is produced at time $t$, and its validity is $v$ time units, then the effective deadline of sensor message $m$ is:

$$ed(m) = \min(t + v, \delta) \qquad (1)$$

where $\delta$ is the start time of the consuming task that consumes $m$. Suppose that the message needs to traverse $h$ hops from the source to the destination and let $m^i$ denote the transmission of message $m$ at the $i^{th}$ hop. Further, let the path delay $pd(m^i)$ denote the total propagation delay and transmission time that will be incurred on the remaining hops to the destination. Then the latest transmission start time (LST) of the message at the $i^{th}$ hop is:

$$l(m^i) = ed(m) - pd(m^i) \qquad (2)$$

The LST denotes the *latest time* by which the $i^{th}$ hop must start transmitting the message in order for it to reach the destination by its effective deadline. If there are multiple messages queued up at a robot awaiting transmissions, then their LSTs can be used to derive a transmission schedule.

## 2.3  Problem Formulation

Given a team of robots equipped with sensors, suppose that each sensor produces a new value periodically, once every $p_i$ time units. Suppose that this sensor value needs to be sent to from the source robot $R_s$ to a destination robot $R_d$ for processing before its effective deadline $ed$.

Since the robots form an ad-hoc network, the sensor message will need to traverse multiple hops to reach its destination. We exploit a specific characteristic of our robotic application to route messages over the ad-hoc network. Specifically, the leader robot is aware of the precise location of each robot for purposes of path planning. Since the location of each robot is known, the leader has a complete view of the ad-hoc network and can compute an optimal route from each sensor to the destination robot during planning. Computed routes are conveyed to the robots for forwarding messages. Since planner has full knowledge of the topology and the movement of robots, it can recompute routes before the underlying topology changes. By exploiting this specific characteristic of the robotic application, the need for a dynamic route discovery protocol can be avoided [15].

In this paper, we will discuss the difficulties and solutions for the last two phases of a communication plan, and leave out the broadcast phase since it has been thoroughly studied in networking community. Given a set of sensor messages that are generated periodically, their associated deadlines and their routes, we study the problem of scheduling message transmissions at each hop so that end-to-end deadline violations are minimized. A desirable scheduler should not only be cognizant of message deadlines when making scheduling decision, it should also effectively use the channel bandwidth by (1) avoiding collisions to minimize the useless bandwidth utilization, and (2) exploiting spatial reuse to maximize bandwidth utilization. Since packet collisions cause a node to back-off and retransmit, they increase the end-to-end delay for a message transmission. Avoiding collisions—two simultaneous transmissions will not collide if and only if the two receivers are mutually outside the other sender's interference range[1]—is crucial for providing timeliness guarantees. Similarly, exploiting spatial reuse enables multiple simultaneous transmissions, enabling the application to maximize its use of the channel
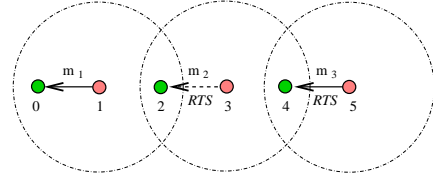
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[1]Transmission range of a sender is defined to be the radial range where all nodes inside it can successfully receive a transmission from the sender; interference range is the distance where the sender's transmissions interfere with a node that is receiving a message sent by a third node.



**Figure 2. Example of false blocking and channel reuse**

capacity.

## 3. Design Considerations

Wireless networks based on the 802.11 family use CSMA/CA algorithms at the MAC layer. In this section, we argue that CSMA/CA networks have certain drawbacks that can hamper timeliness guarantees that are crucial in real-time sensor applications.

First, despite the use of collision avoidance techniques, CSMA/CA networks do not completely eliminate the possibility of a collision. Second, senders can back-off exponentially when they sense ongoing transmissions on the channel. Third, CSMA/CA networks use a clear-to-send (CTS)/request-to-send (RTS) protocol for collision avoidance. In such networks, a node must explicitly request permission to transmit by sending a "request-to-send" (RTS) and must receive a "clear-to-send" (CTS) acknowledgment before sending data. Further, all nodes in the vicinity that receive these messages must avoid transmission for the transmission duration, and are thus *blocked*. This can lead to the false blocking problem [16] which reduces spatial channel reuse, as illustrated next.

### 3.1  Message Contention and Channel Reuse

Consider a simple one hop transmission example depicted in Figure 2. The location of each node and transmission range of each sender are shown in the figure. For simplicity, we assume the interference range is equal to the transmission range. As shown in Figure 2, three single hop messages $m_1$, $m_2$ and $m_3$ need to be scheduled for transmission. Table 1 depicts the arrival time (AT), the transmission duration (TT)(the difference between the instants when the first bit is sent out and the last bit is received by the receiver), and the effective deadline (ED), for each message. The latest start time (LST), calculated using Equation 2, is also shown in the table.

Since $m_1$ arrives at time 0 and is the only message in the system, node 1 transmits a RTS and receives a CTS acknowledgment from node 0. Since node 2 also receives this RTS, it is blocked during the transmission of $m_1$. When message $m_2$ arrives at time 1, node 3 sends a RTS to node

| Message | AT | TT | ED | LST |
|---------|-----|-----|-----|-----|
| $m_1$ | 0 | 2 | 6 | 4 |
| $m_2$ | 1 | 5 | 8 | 3 |
| $m_3$ | 1 | 2 | 8 | 6 |

**Table 1. Message characteristics**



**Figure 3. Parallel transmissions reduce deadline misses.**

| Message | AT | TT | ED | LST |
|---------|-----|-----|-----|-----|
| $m_1$ | 0 | 2 | 6 | 4 |
| $m_2$ | 1 | 6 | 8 | 2 |
| $m_3$ | 1 | 2 | 10 | 8 |

**Table 2. Message characteristics**



**Figure 4. Deadline misses caused by parallel transmissions.**

2 but does not receive a response. Node 4 receives this RTS message as well and is also blocked. Consequently, when node 5 sends a RTS to node 4 for message $m_3$, it does not receive a CTS and is unable to transmit $m_3$. Observe, from Figure 2, that $m_1$ and $m_3$ do not interfere with one another and it is possible to transmit them simultaneously. This is referred to as *false blocking*. In this example, false blocking causes the messages to be transmitted sequentially in the order $m_1$, $m_2$ and $m_3$, resulting in poor spatial reuse. More importantly, doing so causes $m_3$ to miss its deadline.

However, if the scheduler were to exploit spatial reuse and transmit $m_3$ in parallel with $m_1$, followed by $m_2$, then all messages are able to meet their deadlines (see Figure 3).

### 3.2 Why Simple Channel Reuse is Not Sufficient?

Although the previous example demonstrated the benefits of exploiting spatial channel reuse for meeting deadline constraints, surprisingly, parallelizing transmissions via spatial reuse can sometimes *increase* deadline misses. Consider the same scenario depicted in Figure 2 but with the parameters listed in Table 2. Like before, the sensor message $m_1$ is transmitted first at time $t = 0$. Since $m_1$ and $m_2$ interfere with one another, $m_2$ is blocked. However, when $m_3$ arrives at time $t = 1$, it can be transmitted in parallel with $m_1$ since the two transmissions do not interfere. Assuming this is done, $m_2$ can not be transmitted until $m_3$ finishes at time $t = 3$. Since message $m_2$ requires a transmission duration of 6 time units, $m_2$ will finish only at $t = 9$, causing it to miss its deadline (see Figure 4). In this scenario, the only schedule that satisfies all deadlines is to transmit the messages sequentially: $m_1, m_2$ and $m_3$. The example shows that naively maximizing spatial reuse can sometime be detrimental in meeting deadline guarantees. Thus, the message scheduler should consider the potential impact of scheduling a message on future message transmissions.
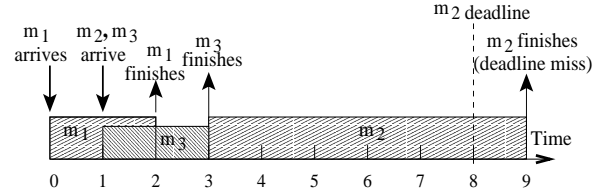
## 4 Scheduling Messages With Deadlines

The problem of scheduling parallel messages with deadlines over wireless channel can be shown to be NP-hard. The problem is NP-hard even when messages traverse a single hop, having unit transmission durations and identical effective deadlines. This can be proved by reducing the graph k-colorability problem [4] to it, where a contention graph $G = (V, E)$ is used to represent conflicts among transmissions. In the graph, each vertex represents a transmission, and an edge exists between two vertices iff the two transmissions (vertices) cannot be scheduled simultaneously. If the graph is k-colorable, all transmissions can be completed within k time units.

Due to the NP-hard nature, we must resort to heuristics to schedule multi-hop messages through the network. In this section, we present two such heuristics.

### 4.1 Per-Hop Smallest LST First (PH-SLF)

Per-hop Smallest LST First (PH-SLF) is a distributed scheduler, where each node makes local scheduling decisions independent of other nodes. In this approach, given a set of messages that are queued up at a node, the node schedules the message with the smallest LST for transmission. Observe that the latest start time (LST), as defined in Equation 2, is the deadline by which the node must start transmitting the message in order for it to meet its effective (end-to-end) deadline. The underlying MAC protocol is vanilla CSMA/CA. As a result, collisions and the resulting back-offs, and false blocking can not be eliminated in this approach. The advantage of this approach is that it can be used in conjunction with vanilla 802.11 networks, since PH-SLF can be implemented in software in the OS driver.

We use PH-SLF as our baseline algorithm. In the rest of

this section, we present an approach that explicitly avoids collisions and maximizes spatial reuse.

## 4.2 Channel Reuse-based Smallest LST First (CR-SLF)

The goal of our Channel Reuse-based Smallest LST First (CR-SLF) approach is to be cognizant of message deadlines at each hop, while avoiding collisions and exploiting spatial reuse. Before presenting the approach, we define some terminology. Table 3 lists the key attributes for a message and the associated terminology.

| Notation | Meaning |
|---|---|
| $m_x^i$ | message $m_x$ at the $i^{th}$ hop |
| $T(m_x^i)$ | the transmission of $m_x^i$ |
| $a(m_x^i)$ | the arrival time of $m_x$ at the $i^{th}$ hop |
| $d(m_x^i)$ | the deadline of $m_x^i$, $d(m_x^i) = ed(m_x)$ |
| $l(m_x^i)$ | the latest start time *(LST)* of $T(m_x^i)$, see Eq. 2 |
| $s(m_x^i)$ | the transmission start time of $T(m_x^i)$ |
| $f(m_x^i)$ | finish time of $m_x^i$—the time $m_x$ reaches the next hop |
| $e(m_x)$ | the execution time for $m_x$ (same for all per-hop transmissions of $m_x$) |

**Table 3. Message attributes**

Since sensor updates are generated periodically, the arrival time of a message at the source (first hop) is the time at which the sensor data is produced. The arrival time at an intermediate node is the time the last bit of the message arrives at that hop enroute to the destination. Observe that the arrival time at an intermediate node depends on when the message is scheduled for transmission at the previous hop. The start time is the time when message is scheduled for transmission and the finish time is the time when the message is completely received by the next hop node (and the channel becomes idle again). The execution time is the time for which the channel is busy and is the sum of the transmission delay and the propagation delay (the difference between the instants when the first bit is sent out and the last bit is received by the next hop). Observe that,

$$a(m_x^{i+1}) = f(m_x^i) = s(m_x^i) + e(m_x^i)$$

In the rest of this paper, transmission refers to a per-hop transmission unless specified otherwise. With this background, we present the intuition behind our approach, followed by the details.

### 4.2.1 Overview

Given a set of nodes, their locations and transmission ranges as well as a set of messages queued up at these nodes, their destinations, effective deadlines, and the associated routes, our scheduler derives a schedule to meet these deadlines.

By a schedule, we mean that the transmission start time of each message is computed for all hops from the source to the destination.

The scheduler exploits the following characteristics in deriving this schedule:

- It maximizes spatial reuse by scheduling non-interfering message transmissions in parallel.

- It considers message transmissions in the order of their LSTs. The LST is the "local" deadline of a transmission at a hop, since it is the latest time by which the message must be scheduled to meet its end-to-end effective deadline.

The basic idea is to partition the set of message transmissions into *disjoint sets* such that transmissions within each set do not interfere with one another and can be executed in parallel. These sets are ordered sequentially, and all transmissions within a set must finish before transmissions in the next set can begin.

To construct these sets, the scheduler considers the transmissions in order of their LSTs. At each step, the transmission with the smallest LST is chosen and the scheduler checks if it is feasible to assign this transmission to an existing set. It is feasible to do so only if (i) the transmission does not interfere with existing message transmissions in that set, (ii) the message can be scheduled for transmission so that its finish time is no later than its deadline, and (iii) inserting this transmission into the set does not cause deadline violations for currently scheduled transmissions in other sets. If no existing set is feasible, a new set is created with that message transmission so long as the deadline is met. Once a message is scheduled at hop $i$, it can be considered for scheduling at hop $i + 1$. Observe that a message needs to be transmitted hop by hop, since the arrival time at the next hop is not known until it is scheduled for transmission at the previous hop. The above process continues until all queued up messages are scheduled along all hops from their sources to their destinations (i.e., the message transmission on each hop is assigned to a feasible set). The constructed sets define the transmission schedule for these multi-hop messages.

The scheduler that executes such an algorithm is designed to be a centralized scheduler. A centralized model is reasonable for a team of robots since a centralized path planner is used to determine the movement plan for each robot. Because the planner has complete knowledge of the location of all nodes and the messages they need to send, the communication scheduler can run in conjunction with the planner as depicted in Figure 1.

### 4.2.2 Details of the Algorithm

Initially, the schedule $\mathcal{S}$ is empty: $\mathcal{S} = \phi$. The goal is to construct a set of sets $\mathcal{S} = \{S_1, S_2, ..., S_n\}$ where elements are disjoint and message transmissions in each set are non-interfering. We define a *start time* and a *finish time* for each set $S_j$. The *start time* of set $S_j$, $s(S_j)$, denotes the instant where all its transmissions can start using the channel; the *finish time* of $S_j$, $f(S_j)$, denotes the instant where all transmissions have reached the their respective receivers. In general, $s(S_{j+1}) = f(S_j)$; that is, transmissions in a set can start to transmit when those in the prior set have finished.

The algorithm proceeds in the following steps.

**Step 1 :** *Select a transmission to schedule.* From the list of yet to be scheduled message transmissions, the scheduler chooses the one with the *smallest* LST. This enables the scheduler to consider the most urgent transmission first. Other strategies are possible, such as choosing transmissions based on the earliest data validity first or earliest start time first, although we do not consider such alternatives in this paper.

**Step 2:** *Assign this message transmission to a set.* Suppose that $n$ sets have been constructed in the partial schedule thus far: $S_1, S_2, ..., S_n$, and $T(m_x^i)$ has been selected. The scheduler attempts to assign this transmission to the *first feasible set* in the set list. If no existing set is feasible (or the schedule is empty), then a new set $S_{n+1}$ is added to the list and $T(m_x^i)$ is inserted into this set so long as the deadline constraint is not violated.

A set $S_j$ to be feasible for a message transmission $T(m_x^i)$ iff the following conditions are satisfied.

1. The finish time of the set $f(S_j)$ is later than the arrival time of the message $a(m_x^i)$. This indicates that a message transmission should be added to a set only if there is some temporal overlap with existing transmissions so that parallelism can be exploited.

2. The finish time of $m_x^i$ is no later than its effective deadline, i.e. $f(m_x^i) = max(s(S_j), a(m_x^i)) + e(m_x^i) \leq d(m_x^i)$.

3. $T(m_x^i)$ does not interfere with any existing message transmissions in $S_j$.

4. The insertion of the transmission $T(m_x^i)$ into $S_j$ does not violate deadlines of messages in subsequent sets $S_k, j < k \leq n$.

The first three conditions are easy to understand, so we elaborate on the fourth condition. If the current message $m_x^i$ happens to be the longest message or its transmission finishes last in $S_j$, then the duration for which $S_j$ occupies the wireless channel is increased. As a result, the transmission start times of messages in subsequent sets will need to be pushed forward. Since a later start time may violate their deadlines, the scheduler needs to verify that inserting this transmission of $m_x^i$ in $S_j$ does not impact the deadline meeting of subsequent message transmissions. To do so, we first need to compute the new finish time of $S_j$. If inserted in $S_j$, the start time of $m_x^i$ is $s(m_x^i) = max(s(S_j), a(m_x^i))$. Then, its finish time is $f(m_x^i) = s(m_x^i) + e(m_x^i)$. The new finish time of the set is the maximum finish time of all messages in the set: $f_{new}(S_j) = max_{\forall x}(f(m_x))$.

Next, we can compute the amount by which all subsequent transmissions are pushed forward. This is done by computing the new start time of each set $S_k$, $j < k \leq n$, which is simply the finish time of the previous set: $s(S_k)) = f(S_{k-1})$. The new start time of each message transmission $T(m_y)$ in the set is recomputed as $s(m_y) = max(s(S_k), a(m_y))$. Then, the finish time is $f(m_y) = s(m_y) + e(m_y)$. The new finish time of the set is the maximum finish time of all messages in the set: $f_{new}(S_k) = max_{\forall y}(f(m_y))$, $T(m_y) \in S_k$. Given the new start and finish times of the affected messages, the scheduler needs to verify that the finish time of each message is not later than its deadline: $f(m_y) \leq d(m_y)$. If no deadlines are violated, then it is possible to insert the current selected message transmission, $T(m_x^i)$, in $S_j$.

The scheduler searches for the first set in the list $S_1, S_2, ..S_n$ that is feasible and inserts the selected transmission into that set. If no existing set is feasible and inserting the transmission into a new set $S_{n+1}$ violates its deadline, then the algorithm can not meet the deadline for this message. In this scenario, the message is removed from consideration and all scheduled transmissions for hops 1 to $i - 1$ are removed from the corresponding sets. And then the start/finish times of those sets are adjusted accordingly.

**Step 3 :** *Update the finish time of the feasible set and insert a new transmission for the next hop.* If a feasible set $S_j$ is found, then the transmission $T(m_x^i)$ is inserted into the set, and the new finish time is updated as discussed above. The transmission $T(m_x^i)$ is deleted from the list of yet to be scheduled transmissions, and the next hop transmission $T(m_x^{i+1})$ is inserted into the list, assuming that hop $i$ is not already the destination for the message. All these steps are repeated until the list of unscheduled transmissions becomes empty.

### 4.2.3 An Example

In this section, we will use a simple one-hop transmission example to illustrate the basic procedure of the algorithm. Consider the example shown in Figure 2 with message characteristics in Table 1. Because $T(m_1)$ has the smallest LST, it is selected first. Initially, the schedule set is empty, a new set $S_1$ is created for the transmission of $m_1$, and we have: $s(S_1) = 0$, $f(S_1) = f(m_1) = 2$.

Then, $T(m_2)$ is considered since it has the smallest LST. Since $T(m_2)$ interferes with $T(m_1)$, set $S_1$ is not feasible and a new set is needed for $T(m_2)$. Thus, we have two sets: $S_1 = \{T(m_1)\}$, $S_2 = \{T(m_2)\}$, and $s(S_2) = f(S_1) = 2, f(S_2) = max(s(S_2), a(m_2)) + e(m_2) = 2 + 5 = 7$. Finally, let us consider the last transmission of $m_3$. Consider $S_1$ first with the four conditions: 1) The finish time of $S_1$ is 2 which is later than $a(m_3)$, 2) $f(m_3) = max(s(S_1), a(m_3)) + e(m_3) = 1 + 2 = 3 < d(m_3)$, 3) Transmission of $m_3$ will not interfere with the existing transmission of $m_1$ in the set, 4) Since $f(m_3) = 3 > f(S_1)$, we have the new possible finish time for $S_1$: $f_{new}(S_1) = f(m_3) = 3$; so the new start time for $S_2$ is $s_{new}(S_2) = f_{new}(S_1) = 3$ and we have $f_{new}(m_2) = 3 + 5 = 8 \le d(m_2) = 8$. Therefore, $S_1$ is feasible for $T(m_3)$, transmission of $m_3$ is assigned to $S_1$. The final schedule is : $S_1 = \{T(m_1), T(m_3)\}$, $S_2 = \{T(m_2)\}$, which indicates that $m_1$ and $m_3$ are transmitted in parallel, followed by the transmission of $m_2$.

# 5 Performance Evaluation

We have designed an event-driven simulator to simulate a team of robots that exchange multi-hop sensor messages and move in the environment. We compare the performance of our proposed algorithm CR-SLF with the PH-SLF scheduling using our simulator. We evaluate the impact of sensor period, deadline and message size based on specific transmission topology. We also investigate how the different interference ranges may affect the properties of the algorithms. Last, we study the impact of node mobility; observe that the movement of a team of robots is highly correlated, and consequently, mobility models such as the random waypoint are not suitable for our scenario.

The metrics used to measure performance is the *Deadline Miss Ratio* which is defined to be:

$$\frac{number\ of\ unsuccessful\ end-to-end\ transmissions}{total\ end-to-end\ transmissions}$$

A successful message transmission is one where the message is transmitted from the source to the destination before the effective deadline. Note here, for the CSMA/CA based algorithm PH-SLF, a message that cannot meet the deadline will still be transmitted from the source through the network; but for the proposed algorithm CR-SLF, once a message is found that it cannot meet the deadline, it will not be scheduled to transmit.The deadline-missing in CR-SLF happens for two reasons: one is the design problem which means that those messages cannot meet the deadlines using any algorithms, the other reason is since the problem is NP-hard, the heuristic algorithm may not be able to find the optimal solution.
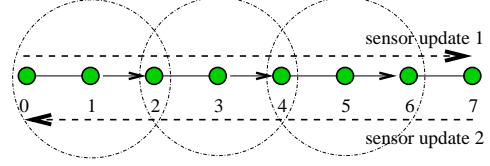


**Figure 5. Scenario 1: transmissions over a robot chain**

## 5.1 Experimental Settings

The wireless card on each robot and its radio parameter are based on the existing commercial product (e.g., Lucent Wavelan card) with a 2 Mbps data rate and a transmission range of 250 meters. Unless specified otherwise, the interference range is set to be equal to the transmission range, and each pair of nodes (robots) are separated by the distance of 200 meters which is likely to yield close to the maximum capacity possible [9].

Table 4 gives the default parameter settings used in our simulations. The effective deadlines are specified in relative terms, relative to the start times of the respective transmissions at the source.

| Message Size | Sensor Period | Relative Deadline |
|---|---|---|
| 512 byte | 10ms | 50ms |

**Table 4. Default Settings**

## 5.2 Impact of the Sensor Period and Deadline

In this experiment, the robotic group is based on a chain topology with 8 robots, as illustrated in Figure 5. Two sensor messages periodically travel through intermediate nodes from two end robots to the opposite end on both directions. We use this scenario to demonstrate the effectiveness of our proposed algorithm, CR-SLF, for different sensor periods and deadlines, and compare it to PH-SLF scheduling.

The impact of varying the sensor periods is shown in Figure 6. In this simulation, the period to generate a new message is depicted on the x-axis. We can see that CR-SLF has fewer deadline misses than the PH-SLF scheduling, especially when the period is between 10ms and 20ms and where collisions are likely unless the scheduler is careful. Beyond 20ms, since the transmission duration per hop is approximately around 2ms. When the next update is generated, the previous one has reached the destination (without considering the update from the opposite direction). Hence, the probability of collisions is very low. Therefore, both algorithms are able to schedule messages with few collisions or deadline misses.
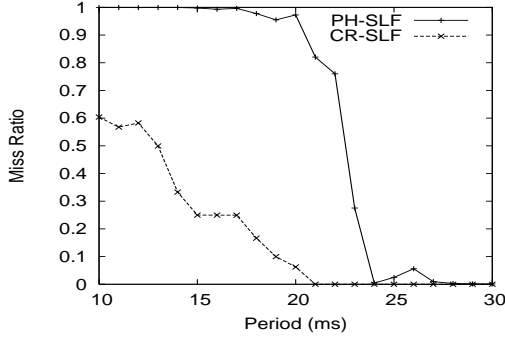
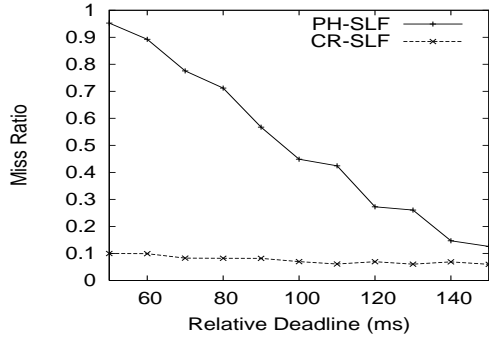**Figure 6. Impact of sensor period**



**Figure 8. Impact of distance**



**Figure 7. Impact of message deadline**



**Figure 9. Scenario 2: transmissions over a cross topology**

The impact of message deadlines is shown in Figure 7. Here, the sensor period is set to 19ms. As the deadline of each sensor update goes from 50ms to 150ms, we have 40% improvement for CR-SLF and 87% improvement for PH-SLF. The reasons we have less improvement for CR-SLF are: 1) although the deadlines are different, the utilization and the probability of collisions are the same; CR-SLF has already explicitly taken these issues into account, and the deadline will only affect the order of transmissions considered, 2) for the PH-SLF scheduling, the larger deadline actually gives it more chances to back off and retransmit, increasing the number of eventual successful transmissions.

### 5.3 Impact of Distance

In the previous section, we evaluated the impact of the sensor period and message deadline with a node distance of 200 meters. In this section, we study how varying the distance between robots affects the results.

We assume the chain topology and assume that two sensor updates are periodically generated from two ends. The period is set to 19ms. We vary the distance between each pair of robots from 50 meters to 200 meters and plot the resulting miss ratio in Figure 8. We observe that CR-SLF performs much better than PH-SLF for all settings. Specifi-
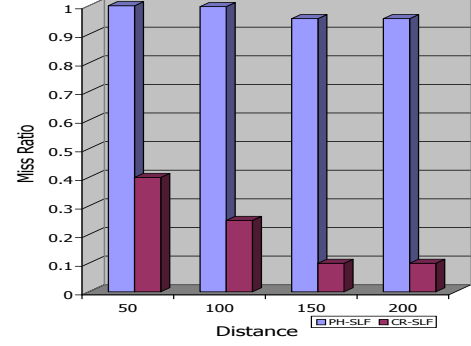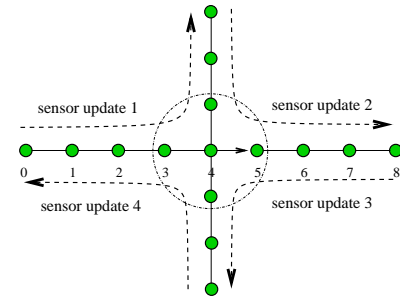
cally, when the distance between nodes is small, i.e., 50 meters, the interference due to one transmission from one node will impact at least 5 other nodes (transmissions on node 2 to node 5 will affect transmissions on all other nodes). Even with this high interference, our proposed algorithm, CR-SLF enables more than 60% of the messages to meet their deadlines, while no message meets its deadline when a CSMA/CA-based algorithm is used.

### 5.4 Impact of Message Size

In this example, we study the effect of varying the message size. We use a cross topology as shown in Figure 9. There are four periodic sensor updates traveling through the network. The period of each sensor is 30ms and the relative deadline is 100ms.

We vary the message size from 256 bytes to 1024 bytes for each respective transmission and measure the miss ratio. The results are shown in Table 5. As we know, the packet size reflects the transmission duration. Since small packet sizes have a smaller probability of collisions, both algorithms work very well. However, as the packet size increases, the per hop transmission duration increases. This increases the duration for which the channel is busy, since
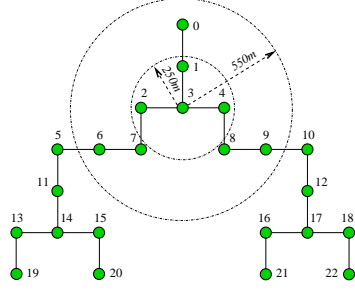
**Figure 10. Scenario 3: tree topology with various interference ranges**

many transmissions may be traversing intermediate hops at the same time. Consequently, collisions cause exponential back-offs and increase the queue delay at each hop. As a result, the performance of PH-SLF scheduling degrades a lot. On the other hand, since CR-SLF explicitly avoids collisions, it is able to meet the deadlines for larger message sizes, so long as the messages are feasible.

| Size | PH-SLF | CR-SLF |
|------|--------|--------|
| (byte) | MissRatio | MissRatio |
| 256 | 0 | 0 |
| 512 | 0.725 | 0.124 |
| 1024 | 0.996 | 0.394 |

.

**Table 5. Impact of message size**

## 5.5 Impact of Interference Range

Note that one node can interfere with message reception at another node even when they are too far apart for successful transmission [9]. In this simulation, we use a tree topology, shown in Figure 10, to study the impact of the interference range. Observe that in a tree, the interference increases for nodes closer with the root, due to the larger node density. We use the parameters in [9] to vary the interference range. We consider two different interference ranges, namely 250 meters and 550 meters, and two different sensor periods, namely 20ms and 25ms. Sensor messages from two leaf nodes, node 19 and 22, are assumed to be sent out periodically to the root (node 0). The third sensor update is sent from a leaf, node 20, to another leaf on the other side, node 21. The relative deadline for each message update is set to 200ms.

We measure the miss ratio for all four combinations of the interference ranges and the sensor periods. Figure 11 shows the results and we have several observations. First, CR-SLF performs better than the PH-SLF scheduling for all different parameters. Second, for a fixed sensor period, when the interference range increases, the miss ratio increases for both algorithms, but the difference between the
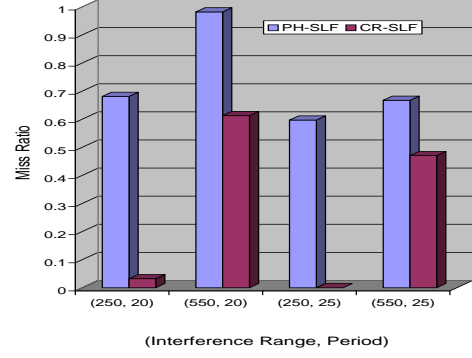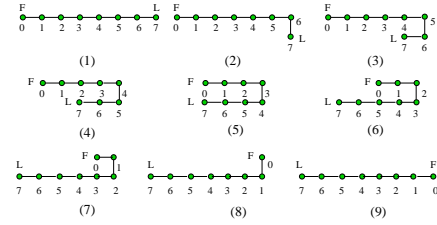


**Figure 11. Impact of interference range**



**Figure 12. Scenario 4: movement of a robot team**

two algorithms gets smaller. The reason is that if the interference range is small, the probability of collisions is dominated by the sensor period. However, when the period is larger, the occurrence of collisions is dominated by both of the sensor period and the interference range.

## 5.6 Impact of Routing and Node Mobility

In this section, we consider the impact of routing and node mobility. Figure 12 depicts the sequence of the moves in a robot chain, where the leader (node 7) leads the team to make a U-turn. Two sensor messages traverse the chain, one from node 0 to 7 and vice versa, with sensor period of 15ms. Two scenarios are considered here: (i) overlay routing, where each update traverses through all intermediate nodes of the overlay chain, and (ii) shortest path routing, where transmissions use the shortest path from the source to destination.

The results of CR-SLF are shown in Figure 13. For the overlay routing, since the update has to travel through every intermediate node, as the team moves from position (1) to (5), the interference increases due to the increase of the node density. Hence, the miss ratio increases. But when the team moves from (5) to (9), the team becomes a chain again, the miss ratio decreases since the interference decreases.

For the shortest path routing, the algorithm will always find the shortest path for message transmissions. For instance, in position (5), messages are directly sent out from
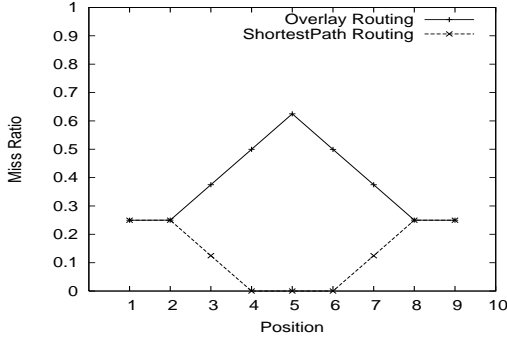
**Figure 13. Impact of mobility**

node 0 to 7 without passing through any other nodes. So when the team moves from position (1) to (5), the number of intermediate routers involved actually decreases. This causes the miss ratio to decrease since the probability of collisions also decreases.

### 5.7 Summary of Our Results

In summary, CR-SLF performs much better than the PH-SLF algorithm in term of the measurement for miss ratio, especially when utilization is high and/or the probability of collisions is high. The major reason is that CR-SLF explicitly avoids collisions while PH-SLF incurs exponential back-off at each collision. Also, CR-SLF doesn't inject infeasible packets into the network once it finds out the packet cannot meet the deadline; hence, the infeasible packet will not affect other feasible packets.

## 6 Related Work

Real-time research challenges for wireless sensor work are addressed in [19, 18]. An early work that studied the real-time communication in sensor networks is [10], where a novel velocity monotonic scheduling was proposed. At each hop, packets are scheduled based on the highest velocity requirement, and the velocity is calculated by the deadline and the distance to travel of each packet. In contrast, our CR-SLF algorithm exploits a specific feature of the robotic application and uses the knowledge at the leader robot to compute the transmission schedule for all nodes. SPEED [6] uses feedback control technique to support soft real-time communication service with a desired delivery speed across the sensor network, so that the end-to-end delay is proportional to the distance between the source and destination. Since each node maintains an average delay for packet transmission, given a distance to travel in hops, whether a packet will meet its deadline can be determined. SPEED focuses on routing service whereas our focus is on message scheduling to guarantee meeting the deadlines. Additional differences between their technique and ours are: 1) maximizing useful bandwidth utilization is explicitly taken into account for scheduling message transmissions to meet the deadlines in our method, and 2) we only inject those messages that can meet deadlines into the network.

In [2], a hexagonal cellular network architecture is used as the infrastructure for wireless transmission. The EDF scheduler is used at each node for intra-cell packet transmission; each router can transmit and receive in the same direction at the same time for inter-cell messages. In [21], the delay performance of policed traffic to provide statistical real-time guarantees over wireless networks is studied. The problem of minimizing the total packet transmission time in a wireless sensor network was studied in [8]. However, the paper considers only single hop transmissions and there is no deadline constraint.

Recently, there has been work on the relationship between the delay and capacity or throughput in wireless networks [5, 17, 3, 13, 14]. All of these efforts focus on computing asymptotic performance bounds. By modeling neighboring interference as conflict graph, lower and upper bounds on the maximum throughput for a given network and workload are computed in [7].

## 7 Concluding Remarks and Future Work

In this paper, we presented two heuristics for scheduling message transmissions with validity and processing constraints in multi-hop robotic sensor networks. Our results show that CR-SLF outperforms PH-SLF since it not only takes the deadline into account, but also attempts to schedule parallel per-hop transmissions as many as possible, so that the end-to-end effective deadlines can be met. We now discuss two other issues.

**Scalability** In this work, we assume a leader node that is responsible for routing, scheduling and path planning decisions. This is a realistic model for small robotic teams. When team becomes large, the whole group can be split to multiple smaller groups. A hierarchical communication infrastructure can then used, and our algorithm can be used for communications at each level.

**Mobility** In robotic applications, the speed of a robot is usually much slower than message transmissions. Since robots can transmit messages while moving, we must ensure that these transmissions will succeed, which means that the overlay network topology must not change even though two nodes may move in opposite directions. Our current work assumes that the leader robot will recompute new routes and a new schedule before a topology change and while the nodes are moving as per the current plan. However, due to the issues of speed, signal strength and routing, this is a problem that needs further study.

We made a few assumptions in our paper that would need to be changed in future work. First, the non-circular and time-varying nature of communication cells need to be studied. Second, packet loss rates typically increase with distance [1], resulting in retransmissions that is not included in our current evaluation metrics. Although we did not specifically consider transmission losses, we believe that our results will hold even in perturbed settings. We will incorporate these issues in future work.

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