

CS 617 Object Oriented Systems  
Lecture 9  
Polymorphism: Mere Syntactic Vs. Dynamic  
Binding,  
Subtyping, Subsumption  
Covariance, Contravariance  
3:30-5:00 pm Thu, Jan 31

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# Outline

- 1 Dynamic Binding and Polymorphism
- 2 Some Syntactic Forms of Genericity/Polymorphism
- 3 Subtyping
- 4 Subsumption Rules

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# Dynamic Binding and Polymorphism I

```
class A {
public:
    virtual void f () { cout << "A.f "; };
    virtual void g () { cout << "A.g "; };
    virtual void h () { cout << "A.h "; };
    virtual void k () { cout << "A.k "; };
};
class B : public A {
public:
    virtual void g () { cout << "B.g "; };
    virtual void h () { cout << "B.h "; };
};
class C : public B {
public:
    virtual void h () { cout << "C.h "; };
    virtual void k () { cout << "C.k "; };
};
```

# Dynamic Binding and Polymorphism II

```
main () {  
  C *cp = new C;  
  B* bp = cp;  
  A* a1 = cp;  
  A* a2 = bp;  
  A* a3 = new B;  
  cp->f(); cp->g(); cp->h(); cp->k();  
  bp->f(); bp->g(); bp->h(); bp->k();  
  a1->f(); a1->g(); a1->h(); a1->k();  
  a2->f(); a2->g(); a2->h(); a2->k();  
  a3->f(); a3->g(); a3->h(); a3->k();  
}
```

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# Member Function Overloading I

```
class Complex {  
    int i ; // real component  
    int j ; // imaginary component  
public:  
    Complex (int x, int y) { i=x; j=y; }  
    Complex add (Complex a) {  
        i += a.i ; j += a.j;  
        Complex tmp (i,j);  
        return (tmp); }  
    Complex add (int i) {  
        Complex tmp (i,0);  
        add (tmp); }  
    void printState () { ... print c1 and c2 ... };  
};
```

## Member Function Overloading II

```
int main () {  
  Complex c1 (2,3), c2(4,6);  
    c1.printState();  
    c2.printState();  
    c1.add (c2);  
    c1.add (100);  
    c1.printState();  
    c2.printState();  
}
```



# Operator Overloading I

```
class Complex {  
private:  
    int i ; // real component  
    int j ; // imaginary component  
public:  
    Complex (int x, int y) { i=x; j=y; }  
    Complex operator + (Complex a) {  
        Complex tmp (i+a.i,j+a.j);  
        return (tmp); }  
    Complex operator + (int x) {  
        Complex tmp (i+x,j);  
        return (tmp); }  
    void printState () { ... }  
};
```

## Operator Overloading II

```
int main () {  
  Complex c1 (2,3), c2(4,6);  
  ..print c1 and c2 before the addition..  
  c1 = c1+c2;  
  c1 = c1+100;  
  c1+c2;  
  c1+100;  
  ..print c1 and c2 after c1=c1+c2; c1=c1+100; c1+c2; c1+100; ..  
}
```

# Templates I

```
template <class T>
class Node {
public:
    T element;
    Node<T> *next;
    Node<T> *previous;
    Node (T e) { element = e; next=previous=NULL;}
};
```

## Templates II

```
template <class T>
class List {

protected:

int len; // cardinality
Node<T> *head;
Node<T> *tail;

public:

    List ();
    List <T>& in (T element);
    // attach given elem at beginning
```

## Templates III

```
T out ();  
// take away front elem and return it.  
// receiver list is the pruned one
```

```
List <T>& push (T element);  
// attach given elem at end
```

```
T pop ();  
// take away last node and return it.  
//receiver list is the pruned one
```

```
List <T>& operator << (T element);  
// same as in ; receiver list returned
```

## Templates IV

```
List <T>& operator + (T element);  
// same as push ; receiver list returned  
  
T operator - () ;  
// same as out; element returned: unary prefix  
  
T operator ~ () ;  
// same as pop; element returned: unary prefix  
  
void read_visit (ListVisitor<T> *visitor);  
// visitor object gets to reads all elements
```

## Templates V

```
void rw_visit (ListVisitor<T> *visitor);  
//visitor object gets to read/write  
// transformed elements are to be returned  
  
int length () {return len;}  
  
List <T> & operator = (List <T> inputlist);  
// copy constructor  
  
void nullify ();  
// nullifies the given list by terminating it  
  
};
```

## Templates VI

```
int main (void) {  
  
    List <char> l,m,n;  
    List <Account> la;  
  
    //.....  
  
}
```



# Syntactic Polymorphism

- Polymorphism Merely syntactic
- Compiler can remove polymorphism during compile time through a type analysis
- For example: all calls to overloaded functions are resolved
- Same type list is used to hold elements of different types, but the compiler generates two different implementations for two different types
- No dynamic binding in syntactic polymorphism

# Polymorphism at Runtime

Can we use a value of one type where a value of another type is expected?

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## Relating Two Different Types

- Principle of Safe Substitution: A value of one type can safely used where a value of another type is expected
- When can you say a value of type  $T_1$  can be used where a value of type  $T_2$  is expected?

A a;

B b;

C c;

R f(B val) {.. use val here ..}

..

..

f(a); when is this permitted?

f(c); when is this permitted?

## Consider Some Types which are Finite Sets of Integers

we know something about type int:

$\text{int} = \{-\text{MAXINT} .. 0 \dots +\text{MAXINT} \}$

Now Let's define types A, B, C as below

Type A = {1,2,3,4,5}

Type B = {1,2,3}

Type C = {1,2}

What can we say about type safety of the above program?

## What about acceptability of returned parameter?

```
A a;  
B b;  
C c;  
R f(B val) {.. use val here ..}
```

..

..

a = f(x); when is this permitted?

b = f(x); when is this permitted?

c = f(x); when is this permitted?

## The Subtype Relation

$S <: T$       (Meaning: S is a subtype of T)

It's safe to use a value of a subtype where a value of a supertype is expected.

i.e.  $\frac{s:S, S <: T}{s:T}$

(called The Rule of Subsumption: The latter subsumes (includes) the former)

Formulate Rules for Subtyping for simple types, structures, functions, and now **Object Types**

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# Set Types

Subsets are Subtypes

## Record Types

One Rule (depth rule):

$$\frac{\text{for each } i \in 1..n \ S_i <: T_i, \ s : S_{1..n}}{s : T_{1..n}}$$

$S_{1..n}, T_{1..n}$  are two records

Formulate a rule based on width of records?

# Function Types

$$f : T_1 \rightarrow T_2$$
$$g : S_1 \rightarrow S_2$$

When is  $g <: f$  ?

## Now to Subtyping induced by Class Inheritance

```
class A {  
    public T2 f(T1);  
    public T4 g(T3);  
}  
class B inherits A {  
    public S2 f(S1);  
    public S4 g(S3);  
}  
main () {  
    A a = new B  
    X x = new X  
    Y y  
    y = a.f(x) ← when will this statement work safely?  
}
```

# Covariance and Contravariance

Which one is type-safe?

At what point of time do you guarantee type safety?

## Subtyping and Subsumption put to Use

- Code written in terms of supertype works on all its subtypes
- Code written in terms of an interface will work on all classes implementing the interface
- code written in terms of a superclass will work on all its subclasses
- Provided that subtyping is established between the base and the derived entities