

CS 723 Introduction to Probability and Linear Algebra, IITB Autumn 2009 notes errata

This is an errata for the lecture notes. Sub-sections names correspond to the names of the files.

cs723Notes.pdf

Here, page numbers denote the actual page numbers shown on every page. The following corrections were suggested by Sagar:

1. Page no. 8, last para: instead of " $0 < k \leq 1$ " it should be " $k \geq 1$ and k integer".
2. Page no. 13, paragraph after Definition 3.2.1: instead of "Now each of $E_i \cup B$ is" it should be " $E_i \cap B$ ".

cs723Scans1.pdf

Here, page numbers are as shown in a pdfviewer. The following corrections were suggested by Sagar:

1. Page no. 7: The line after the plot: " f_X increases till $\lambda - 1$ and then decreases". Actually " f_X increases till $\lambda - 1$, then $f(\lambda - 1) = f(\lambda)$ and it decreases after λ " (it is actually shown in the plot).
2. Page no. 18: In the bottom half, it should be $f_Y(y) = (1/a)f_X((y-b)/a) = \begin{cases} 0 & y < b, \\ 1/a & b \leq y \leq a+b, \\ 0 & y \geq a+b \end{cases}$ (While current version shows equal to 1 for this case).
3. Page no. 20: The second last line, the integral should be " $\lim_{a \rightarrow \infty} \dots$ " instead of " $\lim_{a \rightarrow 0} \dots$ ".
4. Page no. 23: Last para: $\text{var}(X) = 1/12$ for Uniform $[0, 1]$ (notes show $1/3$). This was also pointed out by Lokesh and Salil.
5. Page no. 24: Third to last line: in the formula for $f_Y(y)$ it should be $e^{-(y-\mu)^2/(2\sigma^2)}$, $y \in \mathbb{R}$. In the notes, instead of y , x is used.
6. Page no. 61: Fourth line: instead of "if all $q_y = 1/m$ (for $y = 1$ to m)," it should be "if $p_1 = p_2 = \dots = p_m$ ".

Salil suggested the following correction in Page 21: Line 2 sumation should read $\sum_{x_i \in E} |x_i| f_X(x_i)$ (Currently, the index i is missing inside the sum).

cs723Scans2.pdf

Here, page numbers are as shown in a pdfviewer. Here is a correction revealed in the lectures: Page 61: The statement which says idependence implies conditional independence is false. Enough examples were shown in support of this in the lecture.

The following correction was suggested by Lokesh and Salil:

1. Page 6: In the last TWO equations, final result is written incorrectly as $E[X]$ (in both of them) whereas it should be $E[g(X)]$.

cs723Scans3.pdf

Here page numbers are as shown in a pdfviewer. Here is a correction stressed upon in the lectures: Page 69: the statement “if all eigen-values are real, then the matrix is symmetric” is ofcourse false. There are examples in support of this elsewhere in the notes.

The following comments are by Sagar:

1. Page no. 13: Fourth step: instead of $=$ it should be $\leq$. This was also suggested by Salil.
2. Page no. 27: Need to mention that the transformation matrices M_{T_1} and M_{T_2} for the transformations $T_1 : V \rightarrow W$ and $T_2 : W \rightarrow U$ respectively are with respect to the same basis in the vector space W .
3. Page no. 34: The step after the step 4; “since $\mathcal{N}(M)$ and $\mathcal{R}(M)$ are subspaces in $\mathbb{R}^n$, we have $\dim(\mathcal{N}(M)) + r_r \leq n$. Actually, as mentioned in lectures, we need to use fact that they are not arbitrary subspace in $\mathbb{R}^n$, but they are orthogonal subspaces and hence the statement about dimensionality is true.
4. Page no. 37: The third line says that “The equation $M^T Mx = M^T b$ always has a solution.” But the reasoning given is not sufficient. The reasoning is as follows (as explained in lectures): It means $M^T(Mx - b) = 0$ has a solution. Now $\mathcal{C}(M)$ and $\mathcal{N}(M^T)$ are orthogonal complements and hence b can be written as a linear combination of columns of M and a basis of $\mathcal{N}(M^T)$, say $b = M\beta + \alpha_1 u_1 + \dots + \alpha_k u_k$, where $u_1, \dots, u_k$ is a basis of $\mathcal{N}(M^T)$. It is easy to see that $x = \beta$ is indeed a solution for $M^T(Mx - b) = 0$. If columns of M are not linearly independent then we can have multiple such β 's. Otherwise, there is exactly one such β and hence a unique solution to $M^T Mx = M^T b$. Exactly in this case $M^T M$ is invertible.
5. Page no. 59: In the second example, instead of “Hence the eigen values are 0, 0, 2” it should be 0, 0, 3. This was also pointed by Rachit and Rajdeep.
6. Page no. 68: Second para first line: instead of “orthogonal complement of M ” it should be “orthogonal complement of subspace spanned by v_1 ”.
7. Page no. 81: Second subpoint in the second point should be “orthonormal basis of **column** space is u_2, u_3 .”

The following comments are from Rajdeep:

1. Page 39: The line defining gradient of Lagrangian contains error. Its written as: $\nabla_x L = 0 \Rightarrow 2x + M^T \lambda = 0$, whereas it should be: $\nabla_x L = 0 \Rightarrow x + M^T \lambda = 0$. This was also pointed out by Lokesh.
2. Page 67: Proof of iii. Second line. Should be ”Pick any eigen value” (instead of pick any eigenvector)

The following correction was suggested by Rachit:

1. On page 26: $T(v_{m+1}) = 0w_1 + 0w_2 + \dots + mw_m$ (Currently coefficient of w_2 is 2 instead of 0).

Salil found that the link <http://www.sn1.salk.edu/shlens/pub/notes/pca.pdf> (referred to on the last page) is not available any more. It is now available at www.sn1.salk.edu/shlens/pca.pdf.