CS 747, Autumn 2022: Lecture 26

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Autumn 2022

Shivaram Kalyanakrishnan (2022)

Application of RL to Go

- AlphaGo
- Summary and outlook

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Main References Mastering the game of Go with deep neural networks and tree search.

David Silver, Aja Huang, Chris J. Maddison, Arthur Guez, Laurent Sifre, George van den Driessche, Julian Schrittwieser, Ioannis Antonoglou, Veda Panneershelvam, Marc Lanctot, Sander Dieleman, Dominik Grewe, John Nham, Nal Kalchbrenner, Ilya Sutskever, Timothy Lillicrap, Madeleine Leach, Koray Kavukcuoglu, Thore Graepel, and Demis Hassabis, Nature: 529:484–489, 2016.

• Mastering the game of Go without human knowledge.

David Silver, Julian Schrittwieser, Karen Simonyan, Ioannis Antonoglou, Aja Huang, Arthur Guez, Thomas Hubert, Lucas Baker, Matthew Lai, Adrian Bolton, Yutian Chen, Timothy Lillicrap, Fan Hui, Laurent Sifre, George van den Driessche, Thore Graepel, and Demis Hassabis, Nature, 550:354–358, 2017.

• A general reinforcement learning algorithm that masters chess, shogi, and Go through self-play.

David Silver, Thomas Hubert, Julian Schrittwieser, Ioannis Antonoglou, Matthew Lai, Arthur Guez, Marc Lanctot, Laurent Sifre, Dharshan Kumaran, Thore Graepel, Timothy Lillicrap, Karen Simonyan, and Demis Hassabis, Science: 362(6419):1140–1144, 2018.

 In 2016, Google DeepMind's AlphaGo program (Silver *et al.*, 2016) defeats Lee Sedol (international champion), 4–1.



[1] https://upload.wikimedia.org/wikipedia/commons/thumb/5/56/Lee_Sedol_%28B%29_vs_AlphaGo_%28W%29_-_Game_1.svg/ 734px-Lee_Sedol_%28B%29_vs_AlphaGo_%28W%29_-_Game_1.svg.png. CC image courtesy of Wesalius on WikiMedia Commons licensed under CC-BV-SA-4.0.

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- 19 × 19 board; turn-based; black and white stones.
- Surround opponent's stones to capture them.

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- Surround opponent's stones to capture them.
- AlphaGo ingredients:
- Value network v_{θ} .
- Policy networks p_{σ} , p_{ρ} .
- Rollout policy network p_{π} .

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How learned, how used?

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1. Supervised Learning of Policy Networks

- *p*_σ obtained by supervised learning on data (30 million moves) from expert games in KGS Go Server database.
- 13-layer CNN; 48 hand-designed input features per position, softmax output (over legal actions).
- Trained using gradient ascent to maximise log-likelihood; accuracy = 57%.

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- Trained using gradient ascent to maximise log-likelihood; accuracy = 57%.
- p_{π} trained similarly, to be used for rollouts.
- Linear + softmax; accuracy = 24%; much faster to compute (2 μ s for forward pass, compared to 3*ms* for p_{σ}).

2. Self-play, Reinforcement Learning *p*_ρ(0) = *p*_σ. Good initial seed.

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Ensures stable progress in sequence of agents.

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- "Many games" = few thousands; learning steps = few tens.
- Learning using **Reinforce** with v_{θ} subtracted as baseline.
- Reward: +1 for win, -1 for loss, 0 for all other states.
- p_{ρ} (without search) has win record
- . 80% against p_{σ} (without search),
- . 85% against Pachi (independent agent using MCTS).

• Evaluation function in search should *ideally* be V^* . Instead use v_{θ} , an approximation of $V^{\pi_{\rho}}$ since π_{ρ} is the best available policy.

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- Many orders of magnitude faster to compute than by rollout for similar error thresholds.

4. Decision-time Planning

Uses a version of MCTS in which

$$\mathsf{ucb}(s,a) = Q(s,a) + \mathsf{constant} imes p_\sigma(s,a) imes rac{\sqrt{\mathit{visits}(s)}}{\mathit{visits}(s,a)+1}.$$

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- Standard version: 48 CPUs, 8 GPUs.
- Distributed version: 1200 CPUs, 176 GPUs.

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- Watch "AlphaGo The Movie":

https://www.youtube.com/watch?v=WXuK6gekU1Y.

Getting Sleeker and Stronger

- AlphaGo Zero (Silver et al., 2017)
- Can be trained/run on single machine with 4 TPUs.
- Tabula rasa learning; no bootstrapping from expert games.
- Only raw features (black/white/empty) used.
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• 2019: Lee Sedol retires from professional play.

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- Published literature in RL has exploded in the last 5–10 years.

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- Successes have popularised RL, viewed as a fundamental ingredient of autonomous decision-making systems.
- Published literature in RL has exploded in the last 5–10 years.
- Usually needs lots of computation, data (hence simulators).
- Not the method of choice across all domains.

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- Related courses/areas to explore:

Game theory and multiagent systems; on-line learning; neural networks and deep learning; linear optimisation, MDPs, stochastic approximation; cognitive science, neuroscience; robotics;