

# CS 747, Autumn 2023: Lecture 22

Shivaram Kalyanakrishnan

Department of Computer Science and Engineering  
Indian Institute of Technology Bombay

Autumn 2023

# Reinforcement Learning

## 1. Batch reinforcement learning

- ▶ Experience replay
- ▶ Fitted Q iteration

## 2. Applications

- ▶ Keepaway soccer
- ▶ Atari 2600 games

# Reinforcement Learning

## 1. Batch reinforcement learning

- ▶ Experience replay
- ▶ Fitted Q iteration

## 2. Applications

- ▶ Keepaway soccer
- ▶ Atari 2600 games

# Batch Updates to $\hat{Q}$

- We are back to value function-based learning (with function approximation).

# Batch Updates to $\hat{Q}$

- We are back to value function-based learning (with function approximation).
- On-line methods such as Q-learning “extract” very little information from each transition; are computationally lightweight.

# Batch Updates to $\hat{Q}$

- We are back to value function-based learning (with function approximation).
- On-line methods such as Q-learning “extract” very little information from each transition; are computationally lightweight.
- In many applications, **samples are more expensive than computation**; need to get more out of samples.

# Batch Updates to $\hat{Q}$

- We are back to value function-based learning (with function approximation).
- On-line methods such as Q-learning “extract” very little information from each transition; are computationally lightweight.
- In many applications, **samples are more expensive than computation**; need to get more out of samples.
- **Batch RL** keeps transitions in memory, performs more computationally-intensive updates.

# Batch Updates to $\hat{Q}$

- We are back to value function-based learning (with function approximation).
- On-line methods such as Q-learning “extract” very little information from each transition; are computationally lightweight.
- In many applications, **samples are more expensive than computation**; need to get more out of samples.
- **Batch RL** keeps transitions in memory, performs more computationally-intensive updates.

## **Batch RL outer loop**

$\hat{Q} \leftarrow 0, D \rightarrow \emptyset.$

**Repeat** for ever: //Each iteration is a *batch*.

$\pi \leftarrow \epsilon\text{-greedy}(\hat{Q}).$

Follow  $\pi$  for  $N$  episodes; gather data  $D' = (s_i, a_i, r_i, s_{i+1})_{i=1}^L.$

$D \leftarrow D \cup D'.$

$\hat{Q} \leftarrow \text{BatchUpdate}(D, \hat{Q}). // \hat{Q}$  optional in RHS.



# Experience Replay

- Reference: Lin (1992).
- Assume  $\hat{Q}$  is function-approximated, say by a neural network.

## BatchUpdateExperienceReplay( $D, \hat{Q}$ )

**Repeat**  $M$  times:

- Pick  $(s, a, r, s')$  uniformly at random from  $D$ .
- Tweak  $\hat{Q}$  so that for input  $(s, a)$ , the output “better-matches” target  $r + \gamma \max_{a' \in A} \hat{Q}(s', a')$  (for example, by one step of gradient descent).

**Return**  $\hat{Q}$ .

- Sometimes  $\hat{Q}$  reset/forgotten before the batch update.
- $M$  usually large; hence multiple updates using each sample.

# Fitted Q Iteration

- Reference: Ernst, Geurts, Wehenkel (2005).
- Idea: obtain  $\hat{Q}$  using supervised learning. Wait—labels?

## BatchUpdateFittedQIteration( $D$ )

$\hat{Q}_0 \leftarrow \mathbf{0}$ .

**For**  $i = 0, 1, \dots, H - 1$ :

**For**  $j \in \{1, 2, \dots, L\}$ : //Create a labeled data set.

$x_j \leftarrow \text{FeatureVector}(s_j, a_j)$ .

$y_j \leftarrow r_j + \gamma \max_{a \in A} \hat{Q}_i(s_{j+1}, a)$ .

$\hat{Q}_{i+1} \leftarrow \text{SupervisedLearning}((x_j, y_j)_{j=1}^L)$ .

**Return**  $\hat{Q}_H$ .

- Will not diverge if the supervised learning model is an **averager** (nearest neighbour methods, decision trees, etc.).

# Reinforcement Learning

## 1. Batch reinforcement learning

- ▶ Experience replay
- ▶ Fitted Q iteration

## 2. Applications

- ▶ Keepaway soccer
- ▶ Atari 2600 games

# Keepaway Task, Learning Architecture

- **See video:** <https://www.cs.utexas.edu/~AustinVilla/sim/keepaway/mp4/InitialResults/learn360.mp4>.

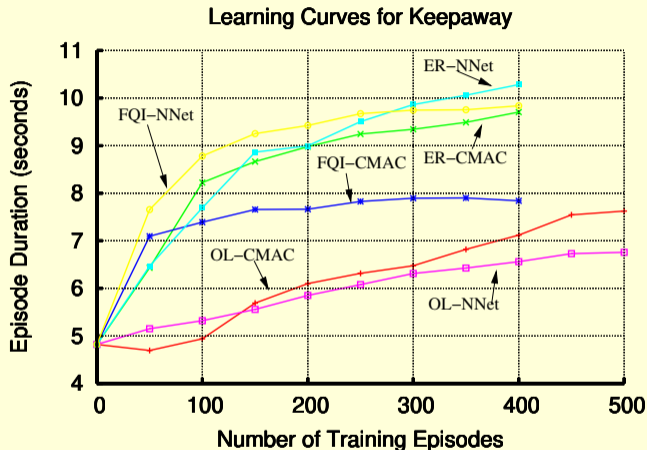
# Keepaway Task, Learning Architecture

- **See video:** <https://www.cs.utexas.edu/~AustinVilla/sim/keepaway/mp4/InitialResults/learn360.mp4>.
- Only learn policy of keeper with ball.
- **States:** specified distances, angles between players, play area.
- **Actions:** hold ball; pass to closer teammate; pass to farther teammate.
- **Reward:** Time between state and next state.
- No discounting.

# Keepaway Task, Learning Architecture

- **See video:** <https://www.cs.utexas.edu/~AustinVilla/sim/keepaway/mp4/InitialResults/learn360.mp4>.
- Only learn policy of keeper with ball.
- **States:** specified distances, angles between players, play area.
- **Actions:** hold ball; pass to closer teammate; pass to farther teammate.
- **Reward:** Time between state and next state.
- No discounting.
  
- $\hat{Q}$  approximated by (1) tile coding, (2) neural network with 1 hidden layer.

# Comparison: On-line vs. Batch RL



**Batch Reinforcement Learning in a Complex Domain.** Shivaram Kalyanakrishnan and Peter Stone, In Proceedings of the Sixth International Joint Conference on Autonomous Agents and Multiagent Systems (AAMAS 2007), pp.650–657, IFAAMAS, 2007.

# Breakout

- Human-level control through deep reinforcement learning.

Volodymyr Mnih, Koray Kavukcuoglu, David Silver, Andrei A. Rusu, Joel Veness, Marc G. Bellemare, Alex Graves, Martin Riedmiller, Andreas K. Fidjeland, Georg Ostrovski, Stig Petersen, Charles Beattie, Amir Sadik, Ioannis Antonoglou, Helen King, Dhharshan Kumaran, Daan Wierstra, Shane Legg, and Demis Hassabis, *Nature*, 518:529–533, 2015.



# Breakout

- **Human-level control through deep reinforcement learning.**

Volodymyr Mnih, Koray Kavukcuoglu, David Silver, Andrei A. Rusu, Joel Veness, Marc G. Bellemare, Alex Graves, Martin Riedmiller, Andreas K. Fidjeland, Georg Ostrovski, Stig Petersen, Charles Beattie, Amir Sadik, Ioannis Antonoglou, Helen King, Dhharshan Kumaran, Daan Wierstra, Shane Legg, and Demis Hassabis, *Nature*, 518:529–533, 2015.

See video: <https://www.youtube.com/watch?v=TmPfTpjtdgg>.

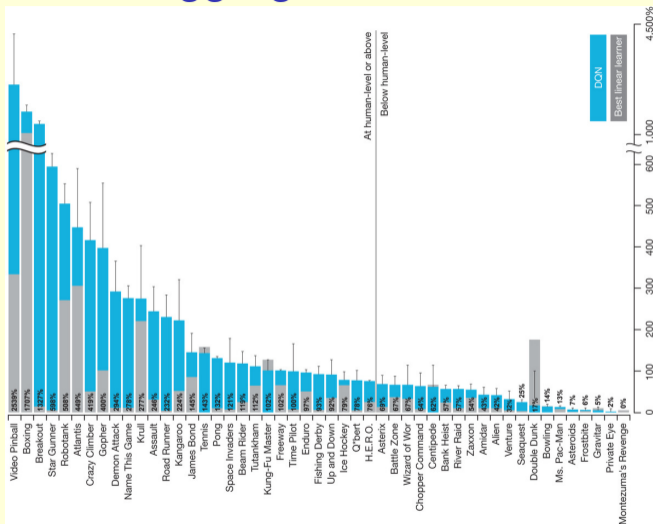
# Breakout

- **Human-level control through deep reinforcement learning.**

Volodymyr Mnih, Koray Kavukcuoglu, David Silver, Andrei A. Rusu, Joel Veness, Marc G. Bellemare, Alex Graves, Martin Riedmiller, Andreas K. Fidjeland, Georg Ostrovski, Stig Petersen, Charles Beattie, Amir Sadik, Ioannis Antonoglou, Helen King, Dhharshan Kumaran, Daan Wierstra, Shane Legg, and Demis Hassabis, *Nature*, 518:529–533, 2015.

See video: <https://www.youtube.com/watch?v=TmPfTpjtdgg>.  
Observe early, middle, and late stages of training.

# Atari 2600 Games: Aggregate Results

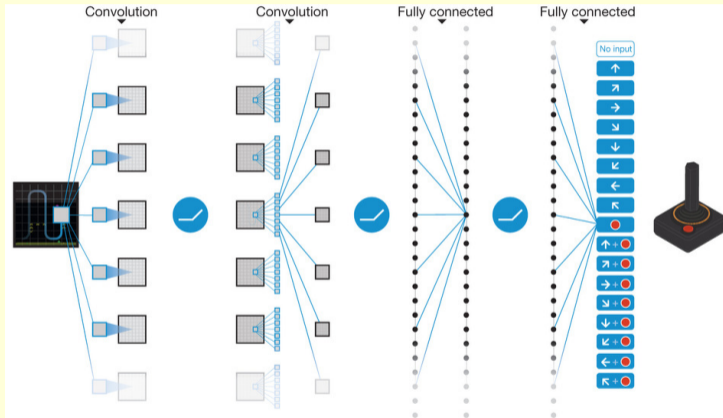


From Mnih *et al.* (2015); for full reference see Slide 9.



# Neural Network-based Representation of $Q$

- **Input:** 4 most-recent  $84 \times 84$  frames. **Output:** 18 action values.



From Mnih *et al.* (2015); for full reference see Slide 9.

- Tens of thousands of weights! How to train?

# DQN Algorithm

- Batch RL, using **experience replay**.
  - A “mini-batch” of  $(s, a, r, s')$  tuples replayed for a few iterations.
  - Q network for providing targets not updated after every atomic update, but still at regular intervals.

# DQN Algorithm

- Batch RL, using **experience replay**.
  - A “mini-batch” of  $(s, a, r, s')$  tuples replayed for a few iterations.
  - Q network for providing targets not updated after every atomic update, but still at regular intervals.
- Rewards clipped to  $[-1, 1]$ .
- **No game-specific** features or hyperparameter-tuning.

# DQN Algorithm

- Batch RL, using **experience replay**.
  - A “mini-batch” of  $(s, a, r, s')$  tuples replayed for a few iterations.
  - Q network for providing targets not updated after every atomic update, but still at regular intervals.
- Rewards clipped to  $[-1, 1]$ .
- **No game-specific** features or hyperparameter-tuning.
- Applied and evaluated on  $\approx 50$  Atari games.
- **Code published**: many implementations now available.
- Results on Atari have subsequently been improved, **new algorithms** (such as A3C) have emerged.



# Summary

- Batch RL motivated by need to
  - **conserve samples** (by trading off with compute time),
  - handle **stability issues** with function approximation.

# Summary

- Batch RL motivated by need to
  - **conserve samples** (by trading off with compute time),
  - handle **stability issues** with function approximation.
- **Experience replay** most simple, common, effective variant.

# Summary

- Batch RL motivated by need to
  - conserve samples (by trading off with compute time),
  - handle stability issues with function approximation.
- Experience replay most simple, common, effective variant.
- Fitted Q iteration also popular; enjoys stability guarantee.

# Summary

- Batch RL motivated by need to
  - **conserve samples** (by trading off with compute time),
  - handle **stability issues** with function approximation.
- **Experience replay** most simple, common, effective variant.
- **Fitted Q iteration** also popular; enjoys stability guarantee.
- Data set  $D$  can be interpreted as an **implicit representation of model**.

# Summary

- Batch RL motivated by need to
  - **conserve samples** (by trading off with compute time),
  - handle **stability issues** with function approximation.
- **Experience replay** most simple, common, effective variant.
- **Fitted Q iteration** also popular; enjoys stability guarantee.
- Data set  $D$  can be interpreted as an **implicit representation of model**.
- **Next class:** Model-based methods (again).