CS 735: Formal Models for Concurrent and Asynchronous Systems

- Introduction

Instructor: Akshay S

Jan 5, 2016

Course hours: Slot11, Tuesdays and Fridays 3:30-5:00pm

1

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- Introduction

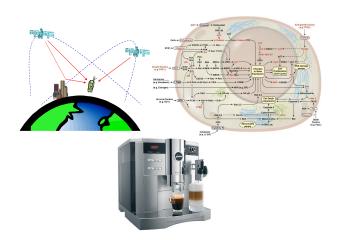
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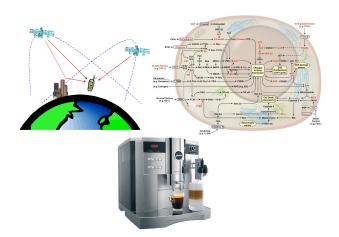
Introduce Formal Models for distributed systems



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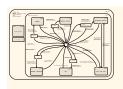
▶ Distributed: Concurrent, asynchronous, communicating,...

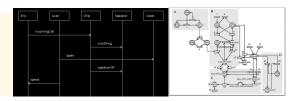


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- ▶ Distributed: Concurrent, asynchronous, communicating,...
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- ► Formal models: Mathematical description, graphical notations, Automata models

Questions that we will tackle

- ► Analysis of such models
- ► Characterization, relations
- ▶ Underlying properties, generalizations

Topics and models that we will cover in this course:

- 1. Petri nets
- 2. Well-structured transition systems
- 3. Distributed automata models and their behaviors
- 4. Extensions and recent advances

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- 1. Petri nets
 - ▶ Elementary nets, Place/Transition nets
 - ▶ Behaviors traces, posets, unfoldings.
 - ▶ Decision problems reachability, coverability
 - ▶ Tools, implementations and case-studies
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- 2. Well-structured transition systems
 - ▶ A generalized abstraction for infinite-state systems
 - ▶ Well-quasi orders and well-founded systems
 - ▶ Applications to show termination of infinite systems
 - ▶ Theoretical bounds on complexity
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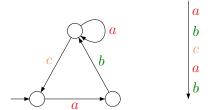
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3. Distributed automata models and their behaviors

- ► Asynchronous automata
- Message passing automata: Also called Communicating finite-state machines
- ▶ Lossy channel machines

4. Extensions and recent advances

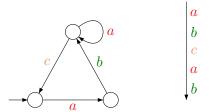
Automata



▶ Behaviours are words, i.e., sequences of actions over a finite alphabet $\Sigma = \{a, b, c\}$.

4

Automata



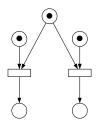
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Questions

- ▶ How shall we distribute it?
- ▶ How shall we add concurrent behaviors?

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Petri Nets



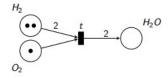


- ▶ An old model for distributed systems
 - ▶ invented by Carl Petri (-at the age of 13- in 1939? or '62)
 - \blacktriangleright to model resource consumption and so on...

Examples of Petri nets

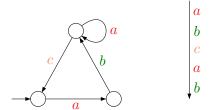
- ▶ A chemical reaction: $2H_2 + O_2 \rightarrow 2H_2O$.
- ► A library
- ► A producer-consumer example
- ► A coffee machine

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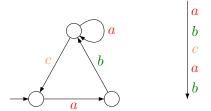
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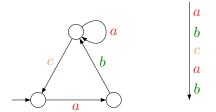
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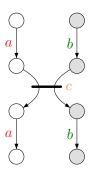
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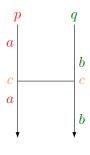
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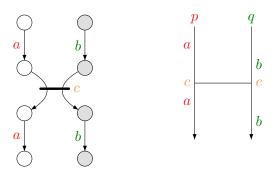
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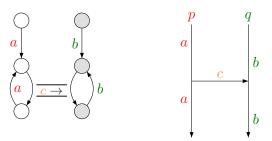
- ► Actions are distributed across processes (with sharing!)
- ▶ Some actions are shared, e.g., c is allowed only if both p and q move on c.

Asynchronous Automata



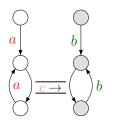
- ▶ What are the properties of languages accepted by such automata? E.g. above accepts {abcab, bacab, bacba, abcba}.
- ightharpoonup Given a language L, (when) can it be accepted by such an asynchronous automaton?

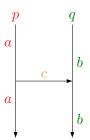
Message Passing Automata



- ▶ In fact, this formalism is Turing powerful!
- ▶ We will consider decidability issues.

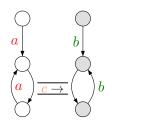
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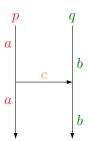




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Message Passing Automata





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- ▶ (Surprising fact: If you are allowed to lose messages randomly then it is decidable!) These are called Lossy channel systems.

Distributing automata

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- ► Take products of automata with shared/communicated actions
- ► Consider local states and local transitions and see how they evolve

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- ▶ Theory of well-structured transition systems
- Under-approximate verification
- Fixed-point approaches

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Pictures and Mathematics

- ▶ How do you write these objects mathematically?
- ▶ Why write them mathematically?

Some take-aways from this course

- ▶ Different formal models for distributed systems
- ▶ Mathematical formalisms that reason about (the infinite) behaviors of such systems.
- ► Techniques to automatically analyze such systems.
- ▶ How to use them and where they are applied.

Logistics

Evaluation (flexible... upto a point)

- ► Continuous evaluation assignments/quizzes : 40%
- ► Exam (Midsem/Endsem): 35 %
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Course material, references will be posted at

- ▶ http://www.cse.iitb.ac.in/~akshayss/teaching.html
- ▶ Piazza will be set up soon.