## CS310 : Automata Theory 2019 IITB, India Tutorial sheet 6 PDA=CFG, DPDA, and CNF

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- 1. Give a PDA to accept the following languages if possible
  - (a)  $\{a^i b^j c^k | i = j \text{ or } j = k\}$
  - (b)  $\{a^i b^j c^k | i \neq j \text{ or } j \neq k\}$
  - (c) The set of all strings with twice as many 0's as 1's.
  - (d)  $\{0,1\}^* \{ww | w \in \{0,1\}^*\}$
- 2. Give a construction that converts a PDA P to another PDA P' such that P' has a single state and  $L^{\epsilon}(P) = L^{\epsilon}(P')$ ? Compare the sizes of P and P'.
- 3. Consider the construction from the lecture 17 to obtain an equivalent PDA A from a grammar G. Prove or disprove: if G be an unambiguous grammar, A is a DPDA.
- 4. Consider the following grammar
  - (a)  $P \rightarrow 0P0$
  - (b)  $P \rightarrow 1P1$
  - (c)  $P \to \epsilon$
  - (d)  $P \rightarrow 1$

The following equivalent PDA recognizes the same language by empty stack.

$$A = (\{q\}, \{0, 1\}, \{0, 1, P\}, \delta, q, P, \{\})$$

$$\begin{array}{c} \epsilon, P/1P1 \\ \epsilon, P/0P0 \\ \\ \text{start} \longrightarrow \begin{array}{c} Q \\ Q \\ Q \\ 0 \\ 1, 1/\epsilon \\ 0, 0/\epsilon \end{array} \epsilon, P/1 \\ \end{array}$$

Consider word w = 1001001. Give a leftmost derivation for w from G and an accepting run of A. For each step of the derivation, give the segment of the run that simulates the step.

- 5. Prove or disprove: for any DPDA A, there is a DPDA A' such that L(A) = L(A') and any  $\epsilon$ -transition in A' is decreasing (i.e.  $\delta(q, \epsilon, Z) = \{(q', \epsilon)\}$ ).
- 6. Convert the following grammars into Chomsky normal form(CNF)
  - (a)

$$\begin{split} S &\to ASB \mid \epsilon \\ A &\to aAS \mid a \\ B &\to SbS \mid A \mid bb \end{split}$$

(b)

$$S \rightarrow 0A0 \mid 1B1 \mid BB$$

$$A \rightarrow C$$

$$B \rightarrow S \mid A$$

$$C \rightarrow S \mid \epsilon$$