

CS766: Analysis of concurrent programs 2022

Lecture 5: Concurrent objects

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Compile date: 2022-02-18

Topic 5.1

Concurrent objects

Concurrent libraries

- ▶ We often **do not write** low-level concurrent code ourselves
- ▶ Concurrency is usually **handled by** concurrent libraries
- ▶ We only **call the functions** of the libraries; library code negotiates concurrent access.
- ▶ They provide interface to **abstract concurrent objects** such as : stacks, queues, sets, etc

Concurrent objects

Definition 5.1

A *concurrent object* is a data structure that can be modified by multiple threads and provides an interface with certain guarantees.

Example 5.1

A concurrent queue can store a collection of things. Threads can call the following functions.

- ▶ $enq(e)$ – adds element e in the collection
- ▶ $e = deq()$ – removes element e in the collection

The elements enter/leave the collection in FIFO order.

Example: LockQueue

```
int head = 0, tail = 0;           // always increasing
Object items[CAP];               // some size
Lock lock;                       // guarded by lock

Object deq() {
    lock.lock();
    if (tail == head) {           // Queue is empty
        lock.unlock();
        throw Empty;
    }
    x = items[head % CAP];        // pick from store
    head++;                      // remove an element
    lock.unlock();               // release lock
    return x;
}
```

LockQueue: enq

```
void enq( Object x ) {  
    l.lock();  
    if (tail-head == CAP) {           // Queue is full  
        l.unlock();  
        throw Full;  
    }  
    items[tail % CAP] = x;           // place in store  
    tail++;                          // insert element  
    l.unlock();                      // release lock  
}
```

Why Lockqueue is a queue?

- ▶ Due to lock, one thread accesses data at a time
- ▶ We can intuitively see it is a queue. We will see the formal definition.

Let us make things complicated. Let us drop Locks!!!

Locks $\Rightarrow$ waiting

Example: LockFreeQueue

```
int head = 0, tail 0;           // always increasing
Object items[CAP];              // some size

Object deq() {
    if(tail == head) throw Empty; // Queue is empty
    x = items[head % CAP]; head++; // remove an element
    return x;
}

void enq( Object x ) {
    if (tail-head == CAP) throw Full; // Queue is full
    items[tail % CAP] = x; tail++;    // insert element
}
```

Is the above a queue?

No exclusive
access

LockFreeQueue: single enq and single deq

In general, LockFreeQueue may not be a queue.

Example 5.2

A bad interleaving between two concurrent enq.

```
enq1: items[0] = x1;  
enq2: items[0] = x2;  
enq1: tail = 1  
enq2: tail = 1
```

Let us consider a scenario, where there is one thread for enqueue and one for dequeue.

Is LockFreeQueue a queue in the restrictive setting?

LockFreeQueue is a queue

Assume exception were not thrown.

The following proves invariants at various program locations.

$\{0 \leq \text{tail} - \text{head} \leq \text{CAP}\}$

Loop : ... = *deq*()

$\{0 \leq \text{tail} - \text{head} \leq \text{CAP}\}$

0 : if(head == tail)

$\{P : 0 < \text{tail} - \text{head} \leq \text{CAP}\}$

1 : x = items[head%CAP];

$\{0 < \text{tail} - \text{head} \leq \text{CAP}\}$

2 : head ++;

$\{0 \leq \text{tail} - \text{head} \leq \text{CAP}\}$

$\{0 \leq \text{tail} - \text{head} \leq \text{CAP}\}$

||

Loop : *enq*(x)

$\{0 \leq \text{tail} - \text{head} \leq \text{CAP}\}$

0 : if(tail - head $\neq$ CAP);

$\{Q : 0 \leq \text{tail} - \text{head} < \text{CAP}\}$

1 : items[tail%CAP] = x;

$\{0 \leq \text{tail} - \text{head} < \text{CAP}\}$

2 : tail ++;

$\{0 \leq \text{tail} - \text{head} \leq \text{CAP}\}$

Exercise 5.1

Verify interference checks.

LockFreeQueue is a queue

If both the threads about to execute updates on `items`.

$$\begin{array}{l} \{P : 0 < \text{tail} - \text{head} \leq \text{CAP}\} \\ 1 : x = \text{items}[\text{head} \% \text{CAP}]; \end{array} \quad || \quad \begin{array}{l} \{Q : 0 \leq \text{tail} - \text{head} < \text{CAP}\} \\ 1 : \text{items}[\text{tail} \% \text{CAP}] = x; \end{array}$$

Both the invariants have to be true, i.e., $P \wedge Q = 0 < \text{tail} - \text{head} < \text{CAP}$

Therefore, $\text{tail} \% \text{CAP} \neq \text{head} \% \text{CAP}$

Therefore, they do not have race condition over elements of `items`.

Therefore, the `enq()` and `deq()` will always behave as if they run one after another.

How do we decide who ran first?

LockFreeQueue : who ran first?

Usually writes are commit points, where a call to the interface says to the world that it is done.

$\{0 < \text{tail} - \text{head} \leq \text{CAP}\}$	$\parallel$	$\{0 \leq \text{tail} - \text{head} < \text{CAP}\}$
2 : head ++;		2 : tail ++;

The thread that executed their update statement first ran first.

Why these writes are the commit point?

We need to look at LockFreeQueue more precisely.

Machine accurate LockFreeQueue

```
int head = 0, tail = 0; Object items[CAP];
```

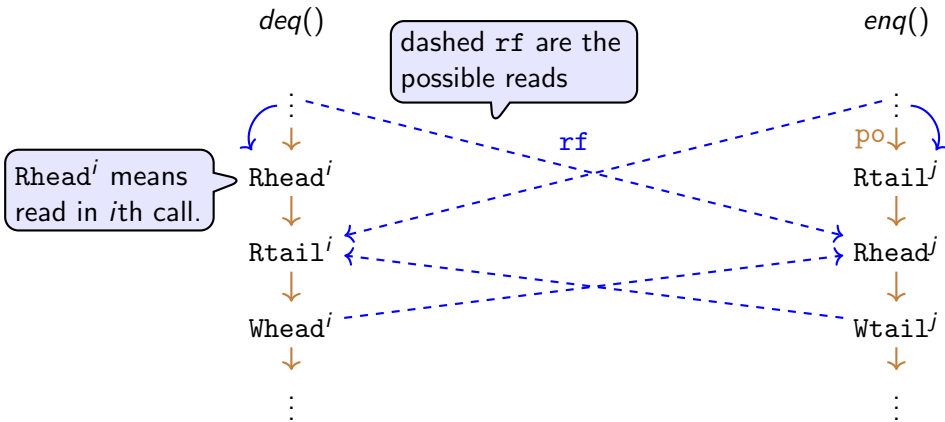
```
Object deq() {  
    l_tail = tail;  
    l_head = head;  
    if(l_tail == l_head) throw Empty;  
    x = items[l_head % CAP];  
    head = l_head + 1;  
    return x;  
}
```

Data is first copied to locals then used.
At the end result is copied to globals

```
void enq( Object x ) {  
    l_tail = tail;  
    l_head = head;  
    if (l_tail - l_head == CAP) throw Full;  
    items[l_tail % CAP] = x;  
    tail = l_tail + 1;  
}
```

Read write pattern in LockFreeQueue

Two reads and a write in each call.



If $Whead^i$ and $Wtail^j$ are ordered according to $(po \cup rf \cup ws \cup fr)^+$ then then we run them in same order in sequential version. Otherwise, we can choose any order.

Proof technique (vague overview)

- ▶ In an algorithm, identify data and control variables.
 - ▶ Control variables control the flow of execution and decide when to update data
 - ▶ Data simply stores the data
- ▶ Find invariants at all locations that show that there is no race over data variables.
- ▶ Show that in all executions we can **linearize**: identify points **where each thread committed**.
- ▶ Compare the **linearized execution with a reference implementation**.

Topic 5.2

Michel & scott queue

Example: Michel & scott queue

- ▶ Let us look at a real lock-free queue
- ▶ Data is stored at linked list
- ▶ `tail` is lazily updated
- ▶ Needs help of CAS instruction from hardware

Compare-and-swap(CAS)

CAS instruction is atomic and has the following effect.

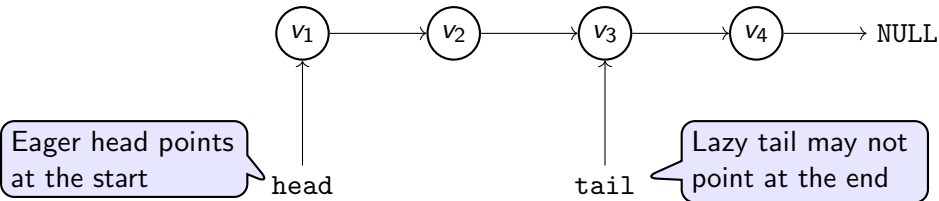
```
bool CAS( p, old_val, new_val) {  
    if( *p == old_val ) {  
        *p = new_val;  
        return true;    // update and return true  
    }  
    return false;      // do nothing and return false  
}
```

Michel & scott queue: initialization

```
struct Node = { Object data, Node* next; }
```

```
Node* head, tail;
```

```
initialize() {  
    node = new Node() // Allocate a free node  
    node->next = NULL // Make it the only node in the list  
    head = tail = node // Both Head and Tail point to it  
}
```



Michel & scott enqueue

```
enq(Object x){
    node = new node(); node->data = x; node->next = NULL; //Allocate

    while(1) {
        l_tail = tail; l_next = l_tail->next //read queue state

        if(l_next == NULL) { //really a tail?
            if( CAS(&(l_tail->next), l_next, node) ) { //try to insert
                CAS( &tail, l_tail, node); //may return false
                return;
            }
        } else { // tail is not at the end. ODD!! :- (
            CAS( &tail, l_tail, l_next) //correcting failures
        }
    }
}
```

// Enqueue done.

Michel & scott dequeue

```
Object dequeue(){
    while(1){                                // try until done
        l_head = head
        l_tail = tail
        l_next = l_head->next                // read queue state

        if(l_head != l_tail) {
            v = l_next->value // Read value before CAS (why?)
            if( CAS(&head, l_head, next) ) return v; //dequeue done
        }else{
            if( l_next == NULL) return NULL; // queue is empty
            CAS(&tail, l_tail, l_next) // Try to advance tail
        }
    }
}
```

Topic 5.3

UnboundedQueue

Example: UnboundedQueue

Here is another concurrent implementation of queue

```
Vector q;  
  
void* enq(int x) { // x > 0  
    q.push_back(x)  
}  
  
int deq() {  
    while( true ) {  
        l = q.length()  
        for( i = 0 ; i < l; i ++ ) {  
            atomic{ x=q[i]; q[i]=0; }           // atomic  
            if ( x != 0) return x;  
        }  
    }  
}
```

Is the above a queue?

End of Lecture 5