

# CS766: Analysis of concurrent programs 2023

## Lecture 6: Linearizability

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# Topic 6.1

## UnboundedQueue

## Example: UnboundedQueue

Here is another concurrent implementation of queue

```
int q[LARGE]; // array initialized to zero
int back;

void* enq(int x) { // x > 0
    atomic{l = back++;}
    q[l] = x;
}

int deq() {
    while( true ) {
        l = back;
        for( i = 0 ; i < l; i ++ ) {
            atomic{ x=q[i]; q[i]=0; } // atomic
            if ( x != 0) return x;
        }
    }
}
```

enq has two global actions.

deq has single effective action.

## Example: an interesting execution

```
thread1: call enq(42)
thread1:  0 = back++;

thread2: call enq(24)
thread2:  1 = back++;
thread2:  q[1] = 24;
thread2:  return; //enq(24);
```

Status of array q after the above execution.

0	24	0	0	...	...
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## Example: two possible expansion of the execution

### Execution 1

```
thread1: call enq(42)
thread1: 0 = back++;
```

```
thread2: call enq(24)
thread2: 1 = back++;
thread2: q[1] = 24;
thread2: return; //enq(24)
```

```
thread3: call deq()
thread3: 2 = back;
thread3: 0 = q[0]; q[0]=0;
thread3: 24= q[1]; q[1]=0;
thread3: return 24; //deq()
```

```
thread1: q[0] = 42;
```

### Execution 2

```
thread1: call enq(42)
thread1: 0 = back++;
```

```
thread2: call enq(24)
thread2: 1 = back++;
thread2: q[1] = 24;
thread2: return; //enq(24)
```

```
thread1: q[0] = 42;
thread3: call deq()
thread3: 2 = back;
thread3: 42=q[0]; q[0]=0;
thread3: return 42; //deq()
//
```

Linearization  
point of enq(42)

Linearization  
point of enq(24)

Linearization  
point of enq(24)

Linearization  
point of enq(42)

Where is the linearization point?

How to characterize the linearization point?

End of Lecture 6