

# CS772: Deep Learning for Natural Language Processing (DL-NLP)

## *Word Vectors*

Pushpak Bhattacharyya

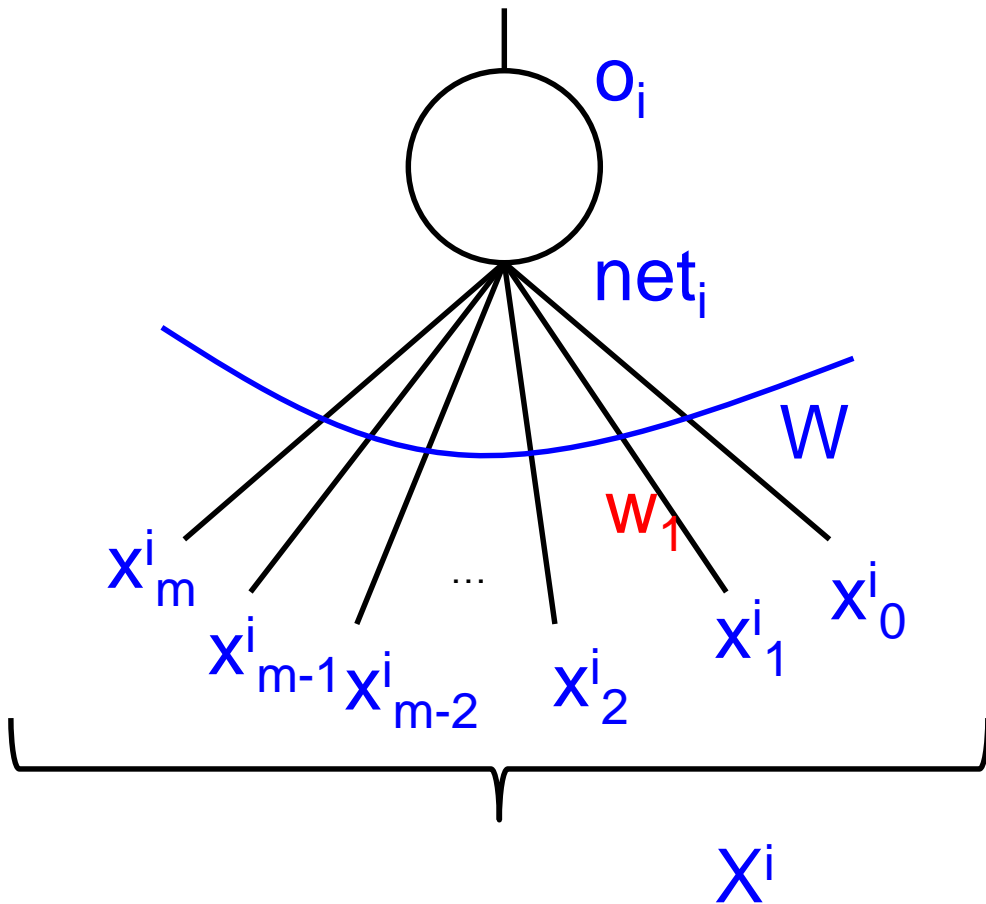
Computer Science and Engineering  
Department

IIT Bombay

*Week 4 of 23<sup>rd</sup> Jan, 2023*

Re-cap

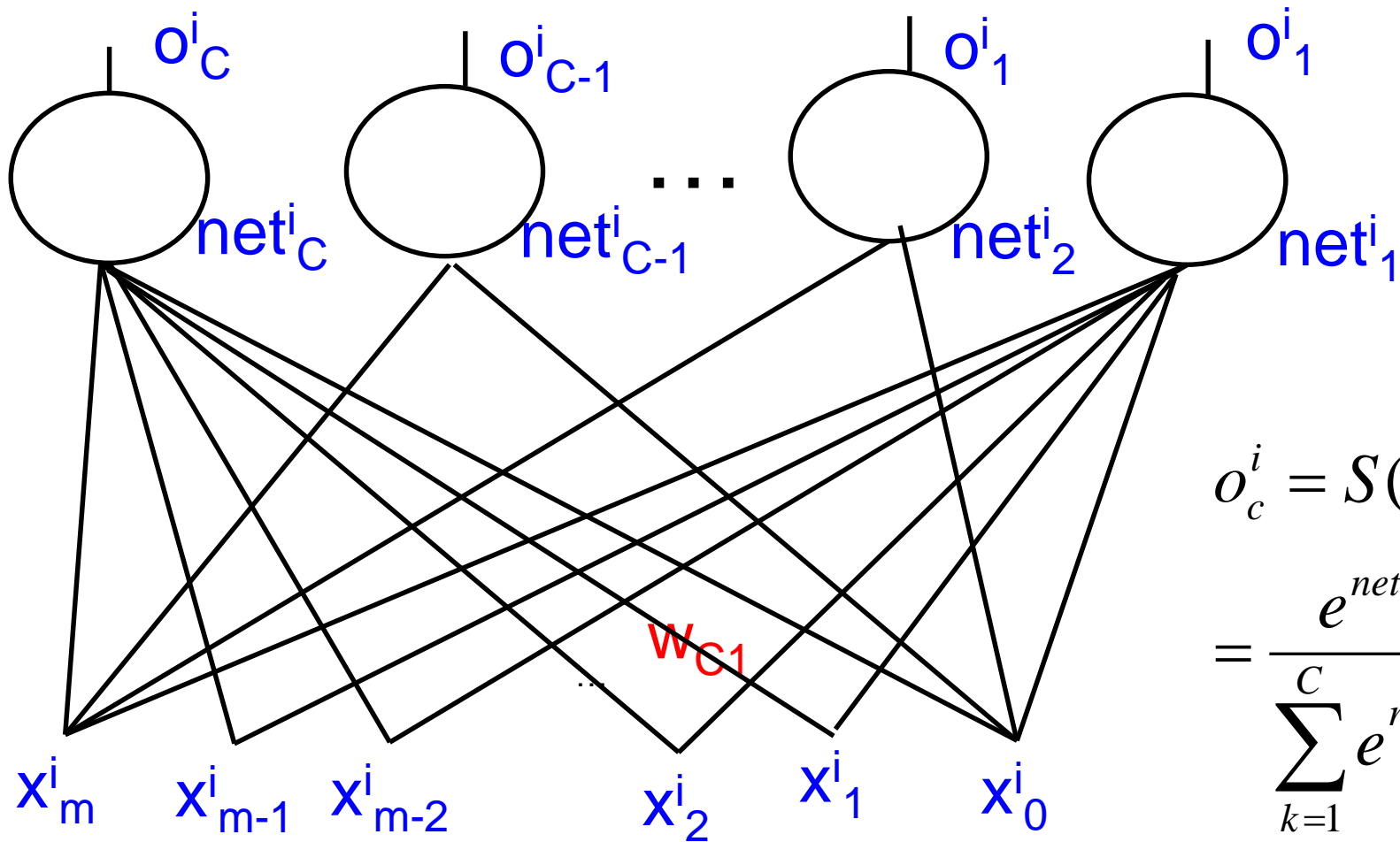
# Sigmoid neuron



$$o^i = \frac{1}{1 + e^{-net^i}}$$

$$net_i = W \cdot X^i = \sum_{j=0}^m w_j x_j^i$$

# Softmax Neuron

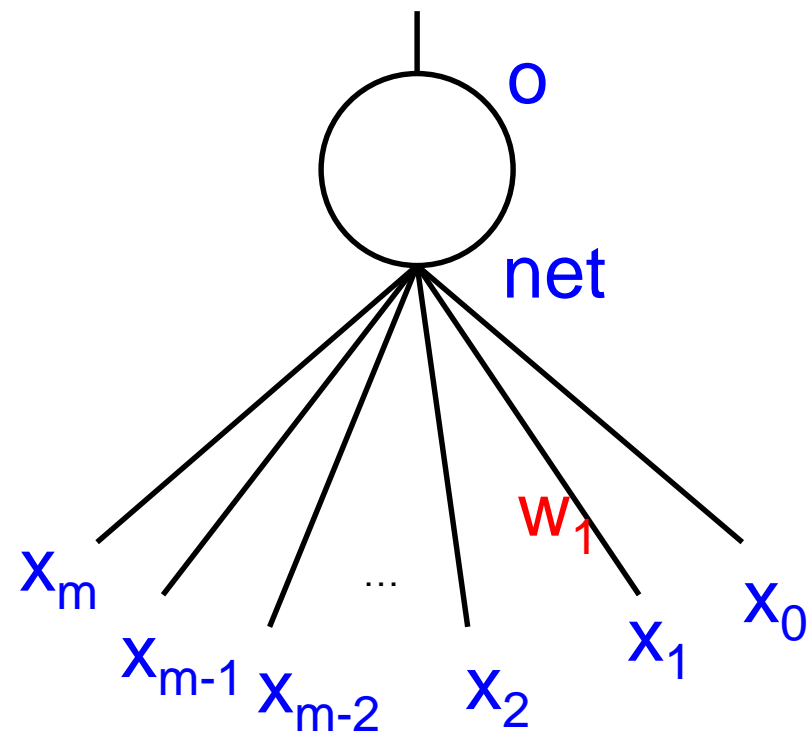


$$o_c^i = S(NET^i)_c$$

$$= \frac{e^{net_c^i}}{\sum_{k=1}^c e^{net_k^i}}$$

Output for class c (small c), c:1 to C

# Single sigmoid neuron- weight change rule



$$\frac{\partial E}{\partial w_1} = \frac{\partial E}{\partial o} \cdot \frac{\partial o}{\partial net} \cdot \frac{\partial net}{\partial w_1}$$

$$E = -t \log o - (1-t) \log(1-o)$$

$$\Rightarrow \frac{\partial E}{\partial o} = -\frac{t}{o} + \frac{1-t}{1-o} = -\frac{t-o}{o(1-o)}$$

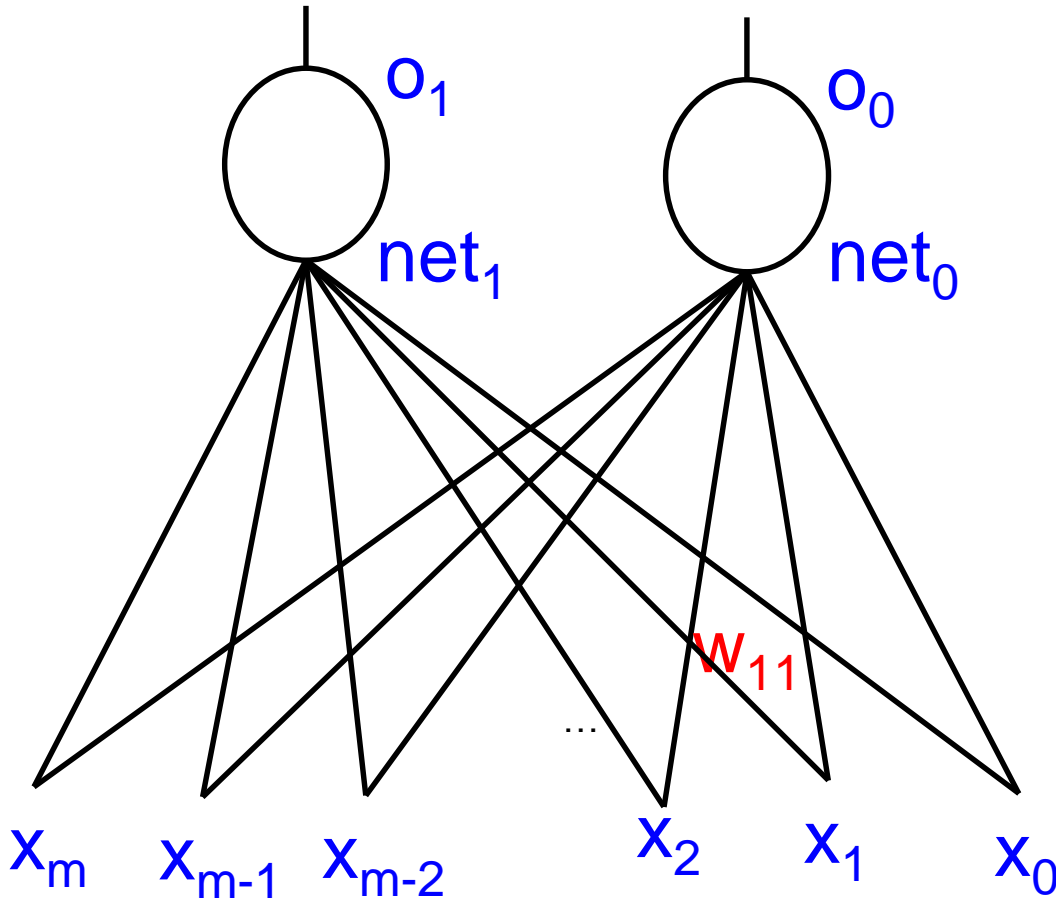
$$o = \frac{1}{1+e^{-net}} \text{ (sigmoid)} \Rightarrow \frac{\partial o}{\partial net} = o(1-o)$$

$$net = \sum_{j=0}^m w_j x_j \Rightarrow \frac{\partial net}{\partial w_1} = x_1$$

$$\Rightarrow \Delta w_1 = \eta \frac{\partial E}{\partial w_1} = \eta(t-o)x_1$$

$$\Delta w_1 = \eta(t-o)x_1$$

Multiple neurons in the output layer: softmax+*cross entropy* loss (1/2): illustrated with 2 neurons and single training data point



$$O = \langle o_1, o_0 \rangle$$

$$NET = \langle net_1, net_0 \rangle$$

$$o_1 = \frac{e^{net_1}}{e^{net_1} + e^{net_0}}, \quad o_0 = \frac{e^{net_0}}{e^{net_1} + e^{net_0}}$$

$$\frac{\partial O}{\partial NET} = \begin{bmatrix} \frac{\partial o_0}{\partial net_0} & \frac{\partial o_1}{\partial net_0} \\ \frac{\partial o_0}{\partial net_1} & \frac{\partial o_1}{\partial net_1} \end{bmatrix}$$

$$= \begin{bmatrix} o_0(1-o_0) & -o_0o_1 \\ -o_1o_0 & o_1(1-o_1) \end{bmatrix}$$

# Softmax and Cross Entropy (2/2)

$$E = -t_1 \log o_1 - t_0 \log o_0$$

$$o_1 = \frac{e^{net_1}}{e^{net_1} + e^{net_0}}, o_0 = \frac{e^{net_0}}{e^{net_1} + e^{net_0}}$$

$$\frac{\partial E}{\partial w_{11}} = -\frac{t_1}{o_1} \frac{\partial o_1}{\partial w_{11}} - \frac{t_0}{o_0} \frac{\partial o_0}{\partial w_{11}}$$

$$\frac{\partial o_1}{\partial w_{11}} = \frac{\partial o_1}{\partial net_1} \cdot \frac{\partial net_1}{\partial w_{11}} + \frac{\partial o_1}{\partial net_0} \cdot \frac{\partial net_0}{\partial w_{11}} = o_1(1-o_1)x_1 + 0$$

$$\frac{\partial o_0}{\partial w_{11}} = \frac{\partial o_0}{\partial net_1} \cdot \frac{\partial net_1}{\partial w_{11}} + \frac{\partial o_0}{\partial net_0} \cdot \frac{\partial net_0}{\partial w_{11}} = -o_1 o_0 x_1 + 0$$

$$\Rightarrow \frac{\partial E}{\partial w_{11}} = -t_1(1-o_1)x_1 + t_0 o_1 x_1 = -t_1(1-o_1)x_1 + (1-t_1)o_1 x_1$$

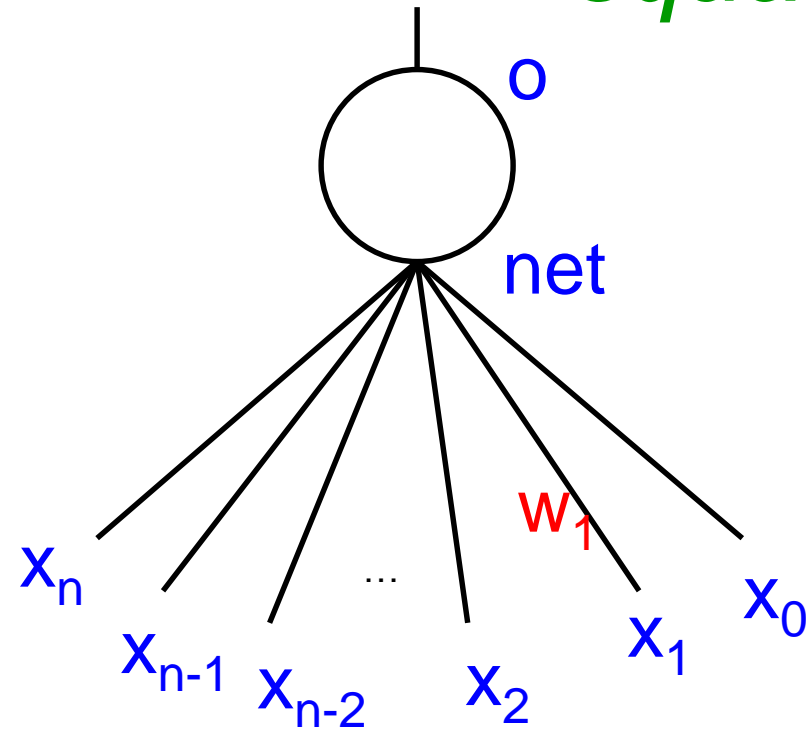
$$= [-t_1 + t_1 o_1 + o_1 - t_1 o_1]x_1 = -(t_1 - o_1)x_1$$

$$\Delta w_{11} = -\eta \frac{\partial E}{\partial w_{11}} = \eta(t_1 - o_1)x_1$$

Weight change rule with TSS



# Single neuron: *sigmoid+total sum square (tss) loss*



Lets consider wlg  $w_1$ . Change is weight  $\Delta w_1 = -\eta \delta L / \delta w_1$   
 $\eta = \text{learning rate}$ ,

$$L = \text{loss} = \frac{1}{2}(t - o)^2,$$

$t = \text{target}$ ,  $o = \text{observed output}$

$$\frac{\partial L}{\partial w_1} = \frac{\partial L}{\partial o} \cdot \frac{\partial o}{\partial \text{net}} \cdot \frac{\partial \text{net}}{\partial w_1}$$

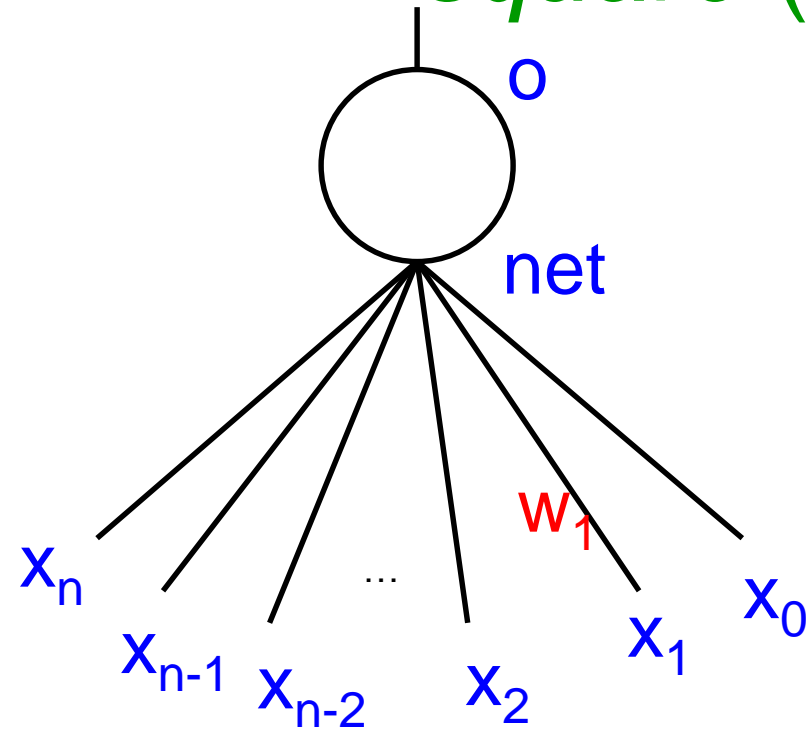
$$L = \frac{1}{2}(t - o)^2 \Rightarrow \frac{\partial L}{\partial o} = -(t - o) \quad (1)$$

$$o = \frac{1}{1 + e^{-\text{net}}} \text{ (sigmoid)} \Rightarrow \frac{\partial o}{\partial \text{net}} = o(1 - o) \quad (2)$$

$$\text{net} = \sum_{i=0}^n w_i x_i \Rightarrow \frac{\partial \text{net}}{\partial w_1} = x_1 \quad (3)$$

$$\Rightarrow \Delta w_1 = \eta(t - o)o(1 - o)x_1$$

# Single neuron: *sigmoid+total sum square (tss) loss (cntd)*



$$\frac{\partial L}{\partial w_1} = \frac{\partial L}{\partial o} \cdot \frac{\partial o}{\partial net} \cdot \frac{\partial net}{\partial w_1}$$

$$L = \frac{1}{2} (t - o)^2 \Rightarrow \frac{\partial L}{\partial o} = (t - o) \quad (1)$$

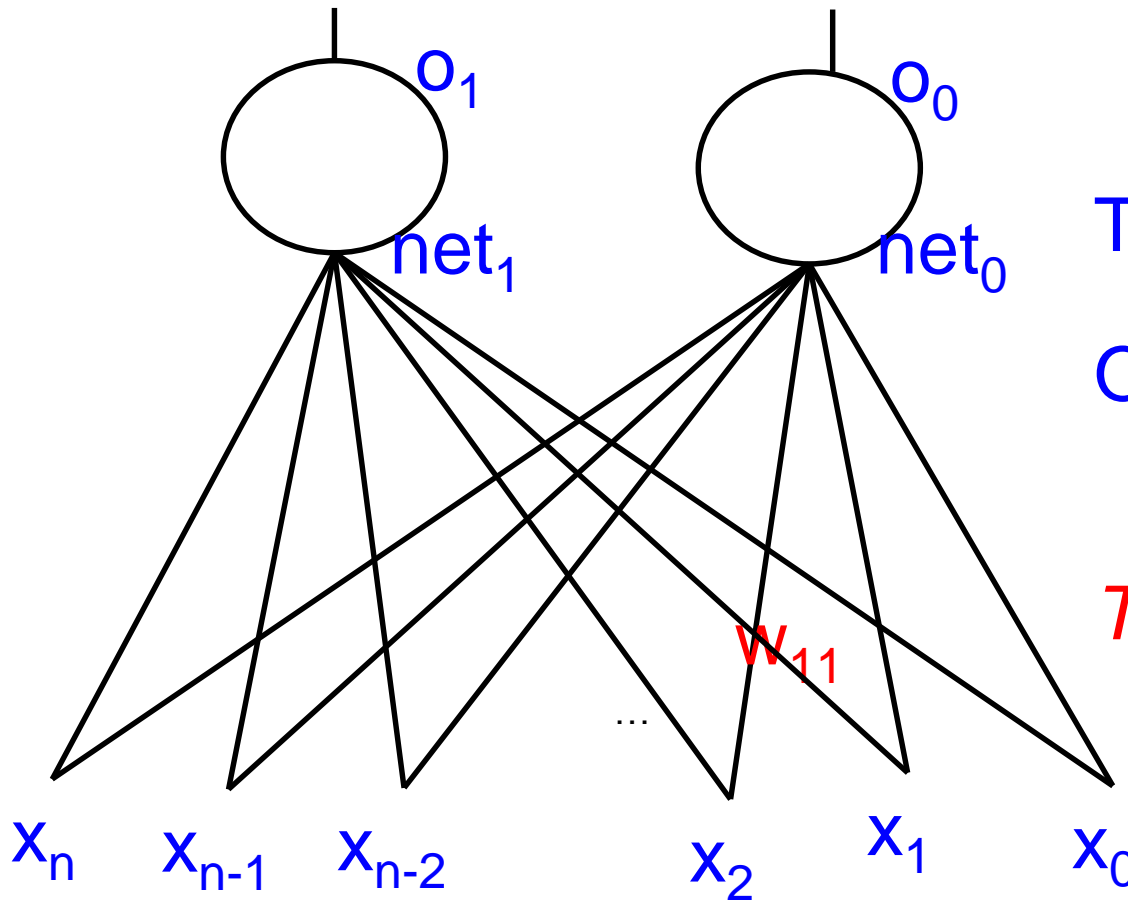
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$$\Rightarrow \Delta w_1 = \eta (t - o) o (1 - o) x_1$$

$$\Delta w_1 = \eta (t - o) o (1 - o) x_1$$

# Multiple neurons in the output layer: *sigmoid+total sum square (tss) loss*



Target vector:  $\langle t_1, t_0 \rangle$

Observed vector:  
 $\langle o_1, o_0 \rangle$

$$TSS \text{ Loss} = \frac{1}{2}[(t_1 - o_1)^2 + (t_0 - o_0)^2]$$

$$\Delta w_{11} = \eta(t_1 - o_1)o_1(1 - o_1)x_1$$

# General Backpropagation Rule

- General weight updating rule:

$$\Delta w_{ji} = \eta \delta_j o_i$$

- Where

$$\delta_j = (t_j - o_j) o_j (1 - o_j) \quad \text{for outermost layer}$$

$$= \sum_{k \in \text{next layer}} (w_{kj} \delta_k) o_j (1 - o_j) o_i \quad \text{for hidden layers}$$

# Word Vectors

# Deriving the word vector: setting

$$W^s : w_0^s, w_1^s, w_2^s, \dots, w_i^s, \dots, w_m^s$$

$W^s$ : word sequence in the  $s^{\text{th}}$  Sentence

$$V_{w_i} : [v_0^i, v_1^i, v_2^i, \dots, v_k^i, \dots, v_d^i]$$

$V_{w_i}$ : word vector of  $w_i$

$$J = P(w_j | w_i)$$

$$L = -P(w_j | w_i)$$

$$P(w_j | w_i) = \frac{e^{V_{w_i} \cdot V_{w_j}}}{\sum_{j'=1}^{|V|} e^{V_{w_i} \cdot V_{w_{j'}}}}$$

$$LL = -V_{w_i} \cdot V_{w_j} + \ln \left( \sum_{j'=1}^{|V|} e^{V_{w_i} \cdot V_{w_{j'}}} \right)$$

# Deriving the word vector: Optimization

(1/2)

$$V_{w_i} : [v_0^i, v_1^i, v_2^i, \dots, v_k^i, \dots, v_d^i] = [u_0, u_1, u_2, \dots, u_k, \dots, u_d]$$

$$V_{w_j} : [v_0^j, v_1^j, v_2^j, \dots, v_k^j, \dots, v_d^j] = [v_0, v_1, v_2, \dots, v_k, \dots, v_d]$$

$$V_{w_{j'}} : [v_0^{j'}, v_1^{j'}, v_2^{j'}, \dots, v_k^{j'}, \dots, v_d^{j'}]$$

$$V_{w_i} \cdot V_{w_j} = \sum_{k=0}^d u_k v_k$$

$$\frac{\partial LL}{\partial u_k} = -v_k + \frac{\frac{\partial}{\partial u_k} \left( \sum_{j'=1}^{|V|} e^{\sum_{k=0}^d u_k v_k^{j'}} \right)}{\sum_{j'=1}^{|V|} e^{\sum_{k=0}^d u_k v_k^{j'}}}$$

# Deriving the word vector: Optimization

$$\begin{aligned}
 &= -v_k + \frac{\sum_{j'=1}^{|\mathcal{V}|} \frac{\partial}{\partial u_k} \left( e^{\sum_{k=0}^d u_k v_k'} \right)}{\sum_{j'=1}^{|\mathcal{V}|} e^{\sum_{k=0}^d u_k v_k'}} = -v_k + \frac{\sum_{j'=1}^{|\mathcal{V}|} e^{\sum_{k=0}^d u_k v_k'} \frac{\partial}{\partial u_k} \left( \sum_{k=0}^d u_k v_k' \right)}{\sum_{j'=1}^{|\mathcal{V}|} e^{\sum_{k=0}^d u_k v_k'}} \\
 &= -v_k + \frac{\sum_{j'=1}^{|\mathcal{V}|} e^{\sum_{k=0}^d u_k v_k'} v_k}{\sum_{j'=1}^{|\mathcal{V}|} e^{\sum_{k=0}^d u_k v_k'}} = -v_k + \sum_{j'=1}^{|\mathcal{V}|} P(w_{j'} | w_i) \cdot v_{k'} = -v_k + E(v_{k'})
 \end{aligned}$$



# Deriving the word vector, Gradient Descent: $\Delta u_k$

$$\Delta u_k = -\eta \frac{\partial LL}{\partial u_k} = \eta [v_k - E(v_{k'})]$$

# Representation

# How to input text to neural net? Issue of REPRESENTATION

- Inputs have to be sets of numbers
  - We will soon see why
- These numbers form **REPRESENTATIONS**
- What is a good representation? At what granularity: words, n-grams, phrases, sentences

# Issues

- What is a good representation? At what granularity: words, n-grams, phrases, sentences
- Sentence is important- (a) *I bank with SBI;* (b) *I took a stroll on the river bank;* (c) *this bank sanctions loans quickly*
- Each 'bank' should have a different representation
- We have to LEARN these representations

# Principle behind representation

- Proverb: “A man is known by the company he keeps”
- Similarly: “A word is known/**represented** by the company it keeps”
- “Company” → Distributional Similarity

# Representation: to learn or not learn?

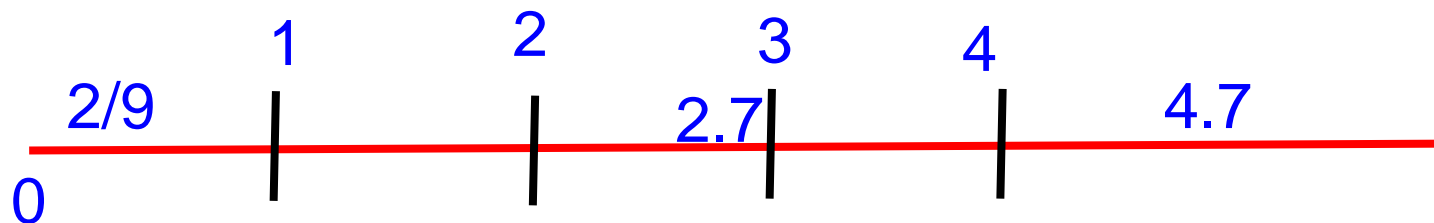
- 1-hot representation does not capture many nuances, e.g., semantic similarity
  - But is a good starting point
- Collocations also do not fully capture all the facets
  - But is a good starting point

# So learn the representation...

- Learning Objective
- ***MAXIMIZE CONTEXT  
PROBABILITY***

# Foundations-1: Embedding

- Way of taking a discrete entity to a continuous space
- E.g., 1, 2, 3, 2.7,  $2/9$ ,  $22^{1/2}$ , ... are numerical symbols
- But they are points on the real line
- Natural embedding
- Words' embedding not so intuitive!





# Foundations-2: Purpose of Embedding

- Enter geometric space
- Take advantage of “distance measures”- Euclidean distance, Riemannian distance and so on
- “Distance” gives a way of computing similarity

# Foundations-3: Similarity and difference

- Recognizing similarity and difference-  
foundation of intelligence
- Lot of Pattern Recognition is devoted to this task (Duda, Hart, Stork, 2<sup>nd</sup> Edition, 2000)
- Lot of NLP is based on Text Similarity
- Words, phrases, sentences, paras and so on (verticals)
- Lexical, Syntactic, Semantic, Pragmatic (Horizontal)

# Similarity study in MT

English:

*This blanket is very soft*

Hindi:

*yaha kambal bahut naram hai*

Bangla:

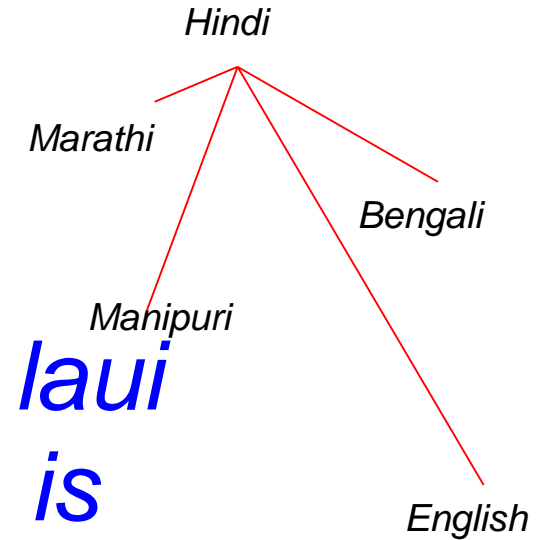
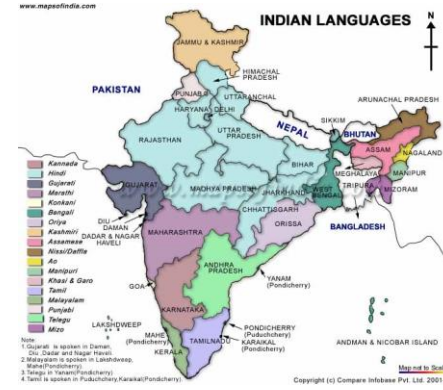
*ei kambal ti khub naram <null>*

Marathi:

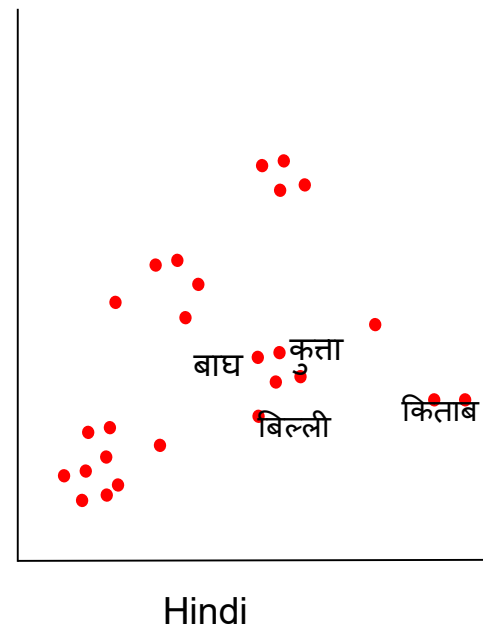
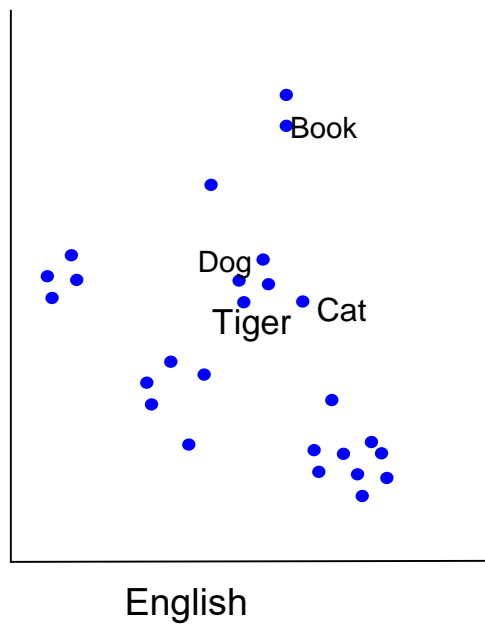
*haa kambal khup naram aahe*

Manipuri:

*kampor asi mon mon laui*  
*blanket this soft soft is*



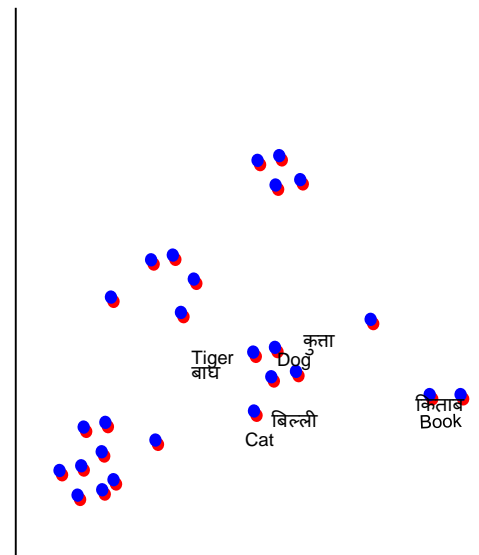
# ISO-Metricity



# Across Cross-lingual Mapping

This involves strong assumption that embedding spaces across languages are isomorphic, which is not true specifically for distance languages (Søgaard et al. 2018). However, without this assumption unsupervised NMT is not possible.

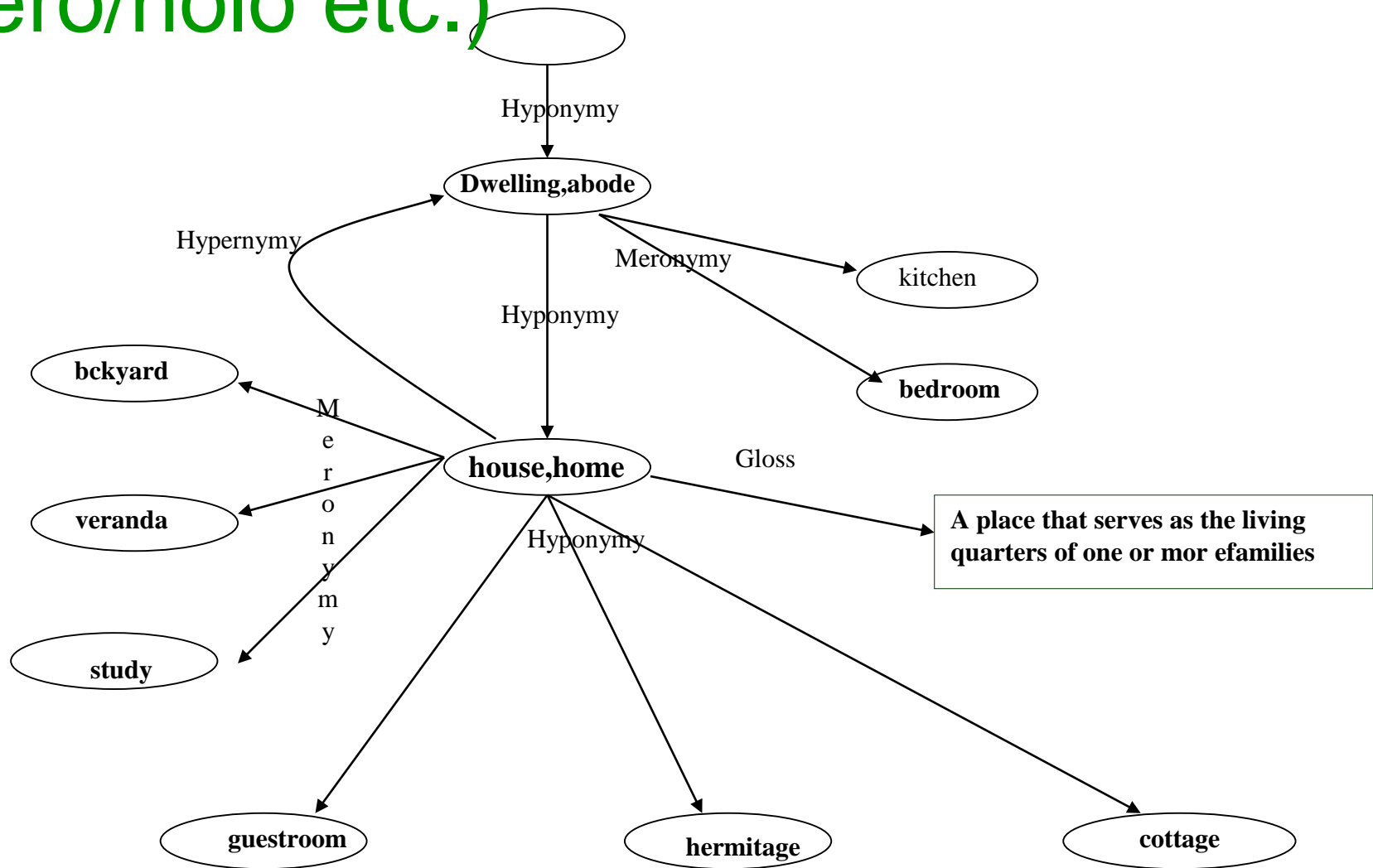
Søgaard, Anders, Sebastian Ruder, and Ivan Vulić. 2018. On the limitations of unsupervised bilingual dictionary induction. ACL



# Foundations-4: Syntagmatic and Paradigmatic Relations

- Syntagmatic and paradigmatic relations
  - Lexico-semantic relations: synonymy, antonymy, hypernymy, meronymy, troponymy etc. **CAT is-a ANIMAL**
  - Cooccurrence: **CATS MEW**
- Wordnet: primarily paradigmatic relations
- ConceptNet: primarily Syntagmatic Relations

# WordNet Sub-Graph with lexico-semantic relations (hyper/hypo, mero/holo etc.)



# Lexical and Semantic relations in wordnet

1. Synonymy (e.g., *house, home*)
  2. Hypernymy / Hyponymy (kind-of, e.g., *cat*  $\leftrightarrow$  *animal*)
  3. Antonymy (e.g., *white and black*)
  4. Meronymy / Holonymy (part of, e.g., *cat and tail*)
  5. Gradation (e.g., *sleep*  $\rightarrow$  *doze*  $\rightarrow$  *wake up*)
  6. Entailment (e.g., *snoring*  $\rightarrow$  *sleeping*)
  7. Troponymy (manner of, e.g., *whispering and talking*)
- 1, 3 and 5 are lexical (*word to word*), rest are semantic (*synset to synset*).



# 'Paradigmatic Relations' and 'Substitutability'

- Words in paradigmatic relations can substitute each other in the sentential context
- E.g., 'The cat is drinking milk' → 'The animal is drinking milk'
- Substitutability is a foundational concept in linguistics and NLP

# Foundations-5: Learning and Learning Objective

- Probability of getting the context words given the target should be maximized (skip gram)
- Probability of getting the target given context words should be maximized (CBOW)

# Learning objective (skip gram)

$$J'(\theta) = \frac{1}{T} \prod_{t=1}^T \prod_{\substack{-m \leq j \leq m \\ j \neq 0}} p(w_{t+j} | w_t; \theta)$$

$$J(\theta) = -\frac{1}{T} \prod_{t=1}^T \prod_{\substack{-m \leq j \leq m \\ j \neq 0}} p(w_{t+j} | w_t; \theta)$$

$$\text{Minimize } L = -\sum_{t=1}^T \sum_{\substack{-m \leq j \leq m \\ j \neq 0}} \log[p(w_{t+j} | w_t; \theta)]$$

# Modelling $P(\text{context word}|\text{input word})$ (1/2)

- We want, say,  $P(\text{'bark'}|\text{'dog'})$
- Take the weight vector **FROM** 'dog' neuron **TO** projection layer (call this  $u_{dog}$ )
- Take the weight vector **TO** 'bark' neuron **FROM** projection layer (call this  $v_{bark}$ )
- When initialized  $u_{dog}$  and  $v_{bark}$  give the initial estimates of word vectors of 'dog' and 'bark'
- The weights and therefore the word vectors get fixed by back propagation

# Modelling $P(\text{context word}|\text{input word})$ (2/2)

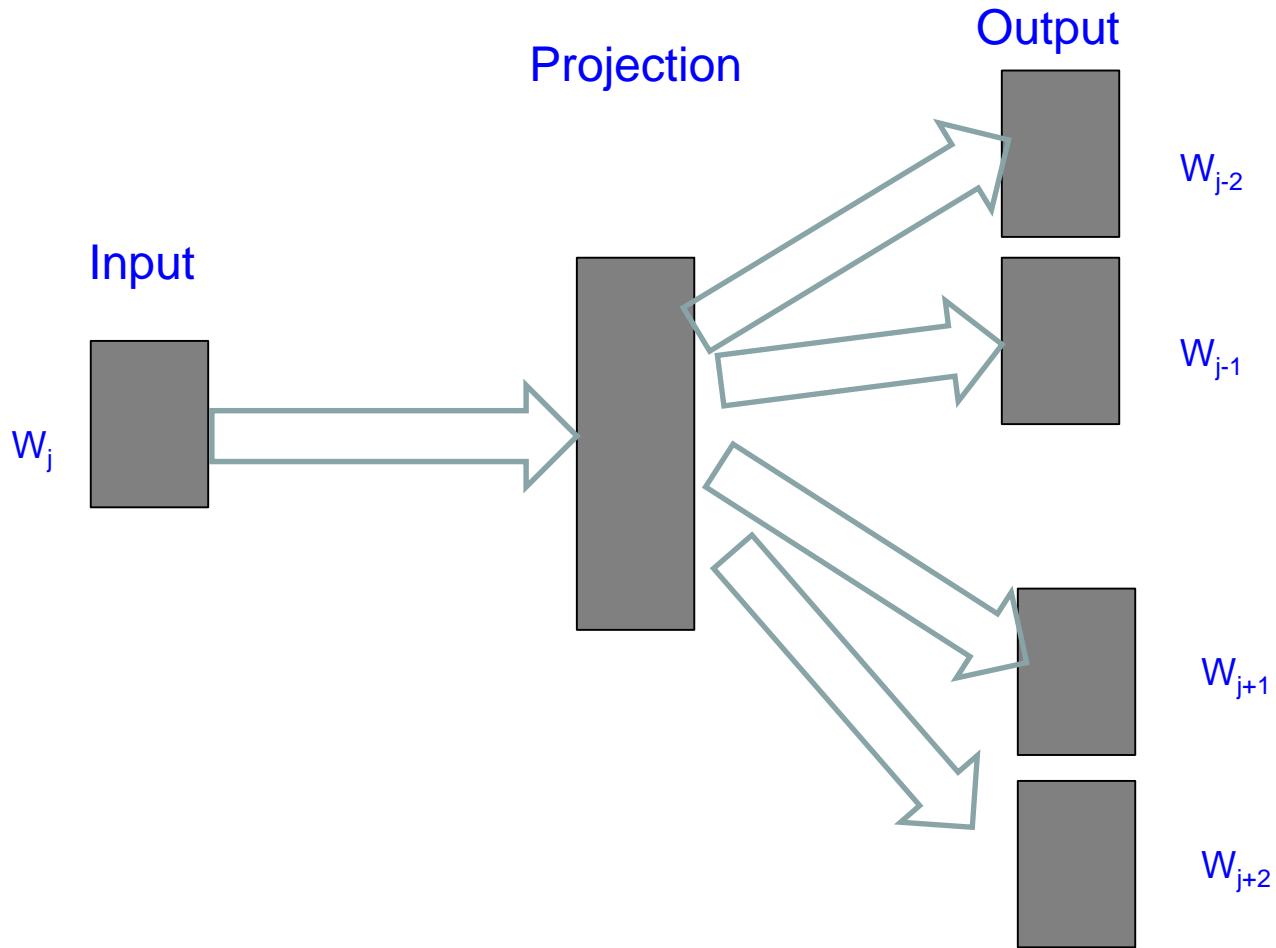
- To model the probability, first compute dot product of  $u_{dog}$  and  $v_{bark}$
- Exponentiate the dot product
- Take softmax over all dot products over the whole vocabulary

$$P('bark'|'dog') = \frac{\exp(u_{dog}^T v_{bark})}{\sum_{v_k \in \text{Vocabulary}} \exp(u_{dog}^T v_k)}$$

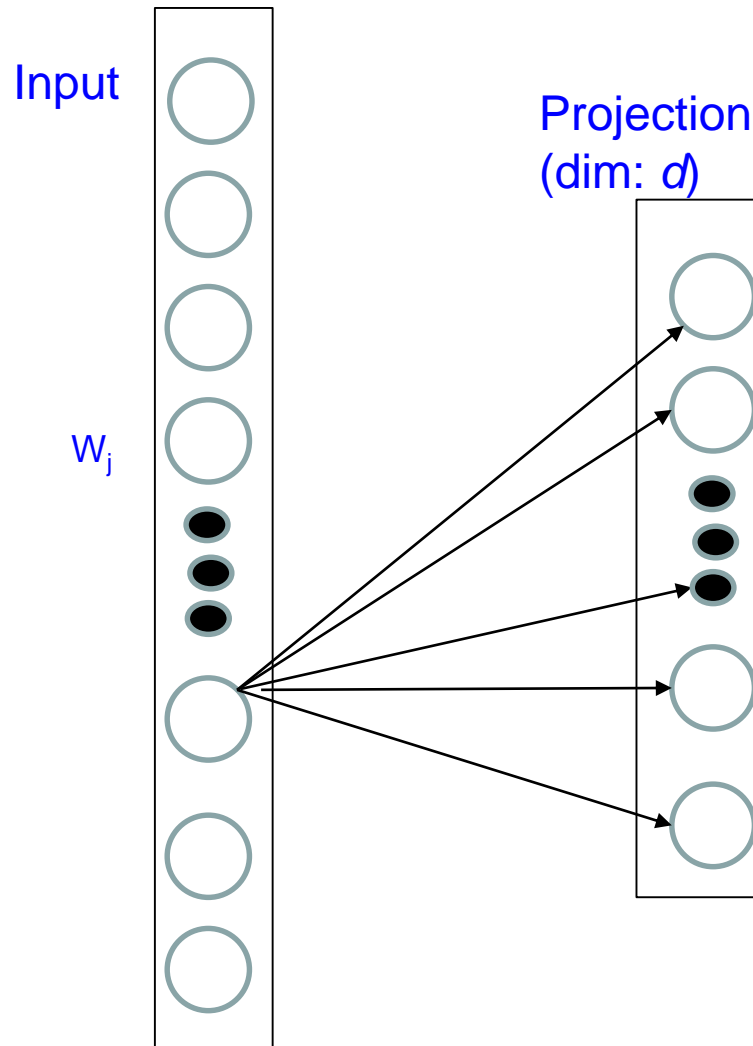
# Exercise

- Why cannot you model  $P(\text{'bark'}|\text{'dog'})$  as the ratio of counts of  $\langle \text{bark, dog} \rangle$  and  $\langle \text{dog} \rangle$  in the corpus?
- Why this way of modelling probability through dot product of weight vectors of input and output words, exponentiation and soft-maxing works?

# Modelling $p(w_{t+j}/w_t)$



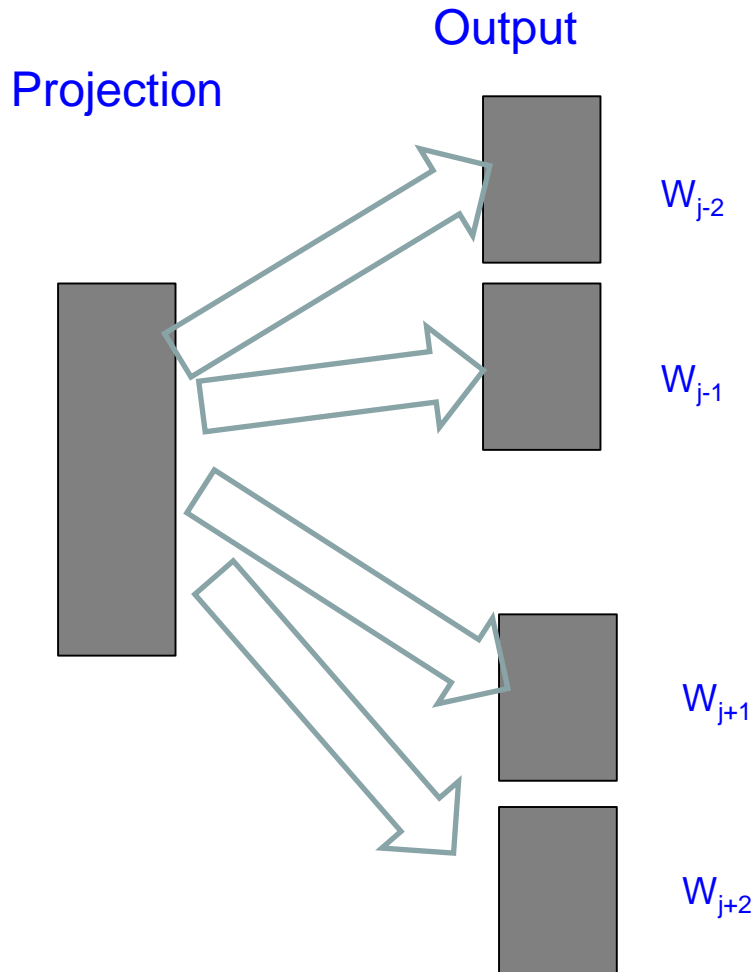
# Input to Projection (shown for one neuron only)



- From each input neuron, a weight vector of dim  $d$
- Input vector is of dim  $V$ , where  $V$  is the vocab size
- Input to projection we have a weight matrix  $W$  which is  $V \times d$
- Each row gives the weight vector of dim  $d$  REPRESENTING that word
- E.g., rows for 'dog', 'cat', 'lamp', 'table' etc.



# Projection to output



- From the whole projection layer a weight vector of dim  $d$  to each neuron in each compartment, where the compartment represents a context word
- Each fat arrow is a  $d \times V$  matrix

# Capturing word association

# Basic concept: Co-occurrence Matrix

Corpora: I enjoy cricket. I like music. I like deep learning

	<b>I</b>	<b>enjoy</b>	<b>cricket</b>	<b>like</b>	<b>music</b>	<b>deep</b>	<b>learning</b>
<b>I</b>	-	1	1	2	1	1	1
<b>enjoy</b>	1	-	1	0	0	0	0
<b>cricket</b>	1	1	-	0	0	0	0
<b>like</b>	2	0	0	-	1	1	1
<b>music</b>	1	0	0	1	-	0	0
<b>deep</b>	1	0	0	1	0	-	1
<b>learning</b>	1	0	0	1	0	1	-

# Co-occurrence Matrix

Fundamental to NLP

Also called **Lexical Semantic Association (LSA)**

Very sparse, many 0s in each row

Apply Principal Component Analysis (PCA) or Singular Value Decomposition (SVD)

Do Dimensionality Reduction; merge columns with high internal affinity (e.g., *cricket* and *bat*)

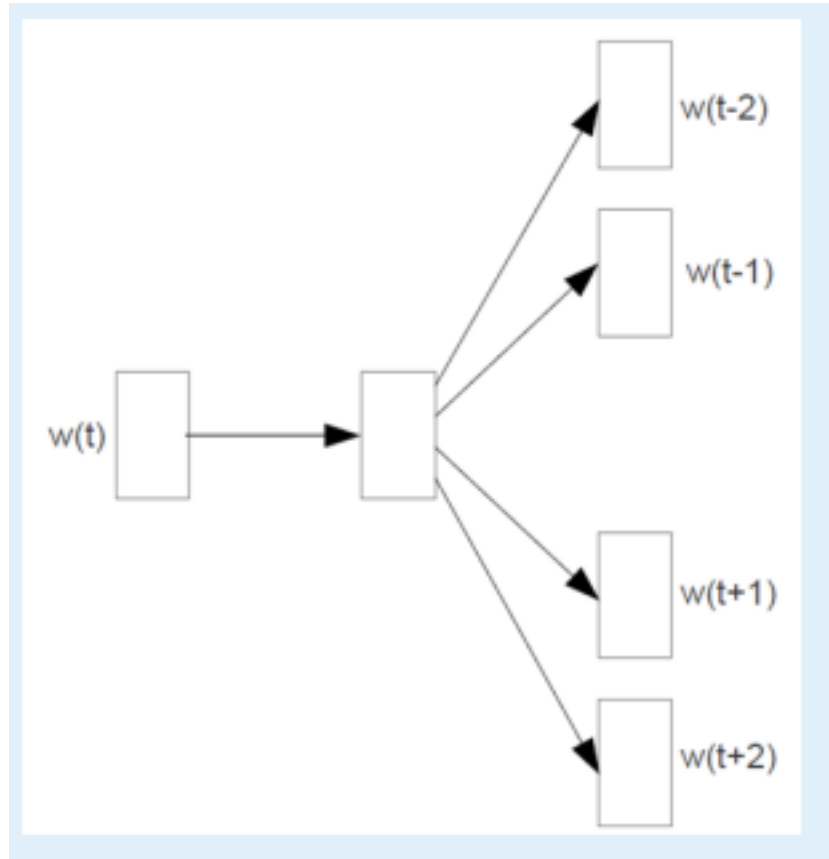
Compression achieves better semantics capture

# Linguistic foundation of word representation by vectors

# “Linguistics is the eye”: Harris Distributional Hypothesis

- Words with similar distributional properties have similar meanings. (Harris 1970)
- 1950s: Firth- “A word is known by the company its keeps”
- Model **differences** in meaning rather than the proper meaning itself

# “Computation is the body”: Skip gram- predict context from word



For CBOW:

Just reverse the  
Input-Output

# Dog – Cat - Lamp



{bark, police, thief,  
vigilance, faithful, friend,  
animal, milk, carnivore}



{mew, comfort, mice, furry,  
guttural, purr, carnivore, milk}

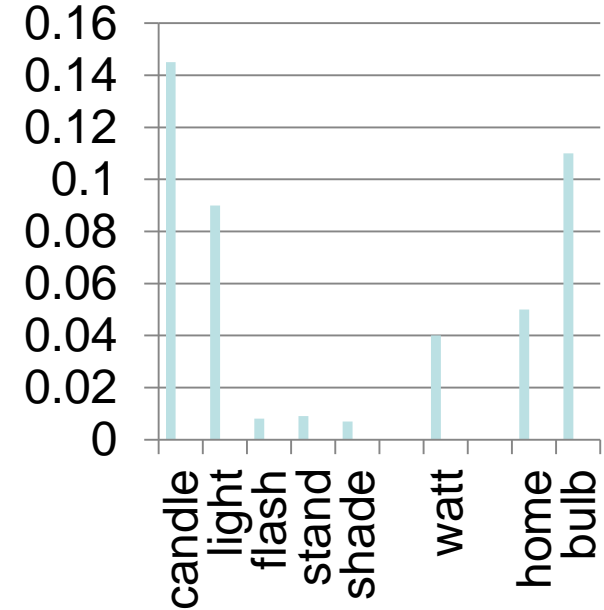
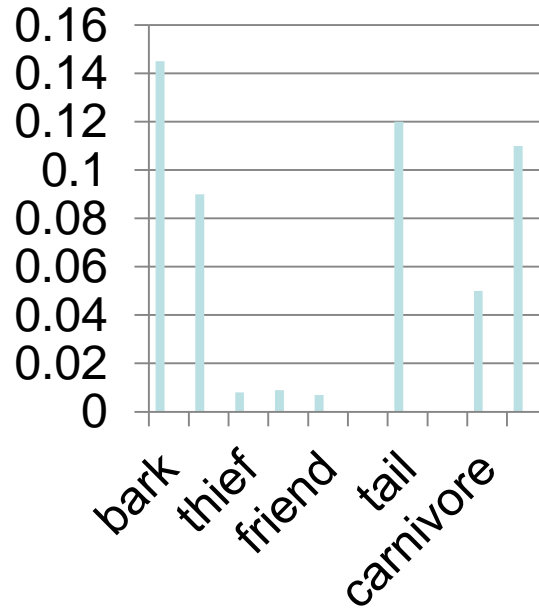
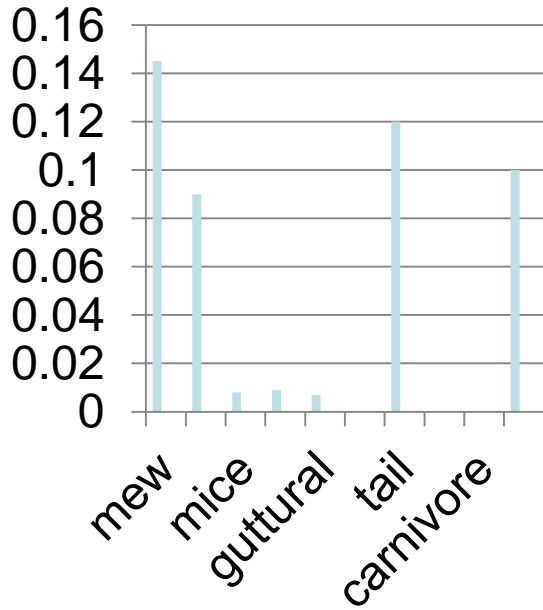


{candle, light, flash, stand, shade,  
Halogen}



# Probability distributions of context words

## CE(dog, lamp) > CE(dog, cat)



# Test of representation

- **Similarity**

- ‘Dog’ more similar to ‘Cat’ than ‘Lamp’, because
- Input- vector(‘dog’), output- vectors of associated words
- More similar to output from vector(‘cat’) than from vector(‘lamp’)

“Linguistics is the eye, Computation  
is the body”

The encode-decoder deep learning  
network is nothing but

the *implementation* of

Harris’s Distributional Hypothesis

# Fine point in Harris Distributional Hypothesis

- Words with similar distributional properties have similar meanings. (Harris 1970)
- Harris does mention that distributional approaches can model differences in meaning rather than the proper meaning itself

# Representation Learning

# Basics

- What is a good representation? At what granularity: words, n-grams, phrases, sentences
- Sentence is important- (a) *I bank with SBI;* (b) *I took a stroll on the river bank;* (c) *this bank sanctions loans quickly*
- Each 'bank' should have a different representation
- We have to LEARN these representations

# Principle behind representation

- Proverb: “A man is known by the company he keeps”
- Similarly: “A word is known/**represented** by the company it keeps”
- “Company” → Distributional Similarity

# Starting point: 1-hot representation

- Arrange the words in lexicographic order
- Define a vector  $V$  of size  $|L|$ , where  $L$  is the lexicon
- For word  $w_i$  in the  $i^{th}$  position, set the  $i$ th bit to 1, all other bits being 0.
- Problem: cosine similarity of ANY pair is 0; wrong picture!!



# Representation: to learn or not learn?

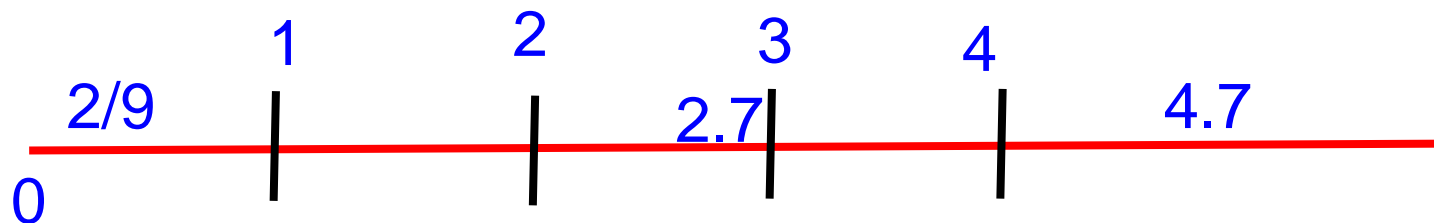
- **1-hot** representation does not capture many nuances, e.g., semantic similarity
  - But is a good starting point
- **Co-occurrences** also do not fully capture all the facets
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# So learn the representation...

- Learning Objective
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# Foundations-1: Embedding

- Way of taking a discrete entity to a continuous space
- E.g., 1, 2, 3, 2.7,  $2/9$ ,  $22^{1/2}$ , ... are numerical symbols
- But they are points on the real line
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# Foundations-2: Purpose of Embedding

- Enter geometric space
- Take advantage of “distance measures”- Euclidean distance, Riemannian distance and so on
- “Distance” gives a way of computing similarity

# Foundations-3: Similarity and difference

- Recognizing similarity and difference-  
foundation of intelligence
- Lot of Pattern Recognition is devoted to this task (Duda, Hart, Stork, 2<sup>nd</sup> Edition, 2000)
- Lot of NLP is based on Text Similarity
- Words, phrases, sentences, paras and so on (verticals)
- Lexical, Syntactic, Semantic, Pragmatic (Horizontal)

# Similarity study in MT

English:

*This blanket is very soft*

Hindi:

*yaha kambal bahut naram hai*

Bangla:

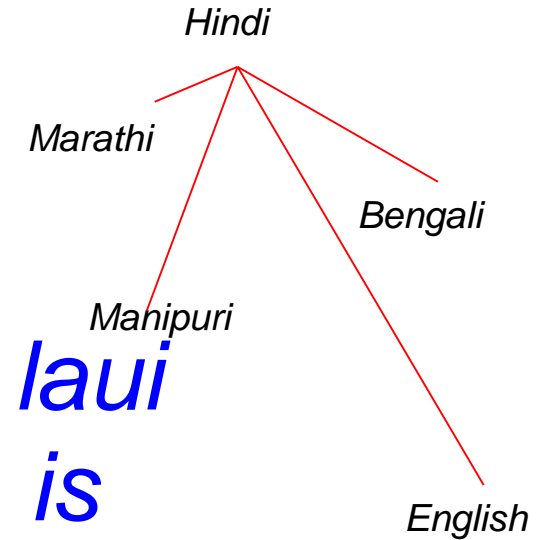
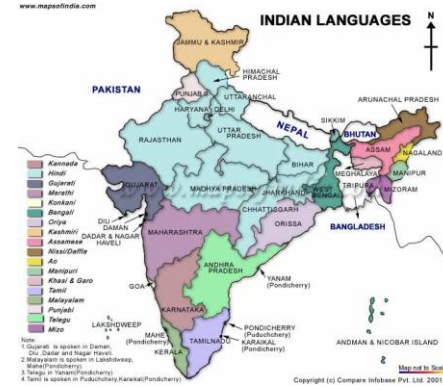
*ei kambal ti khub naram <null>*

Marathi:

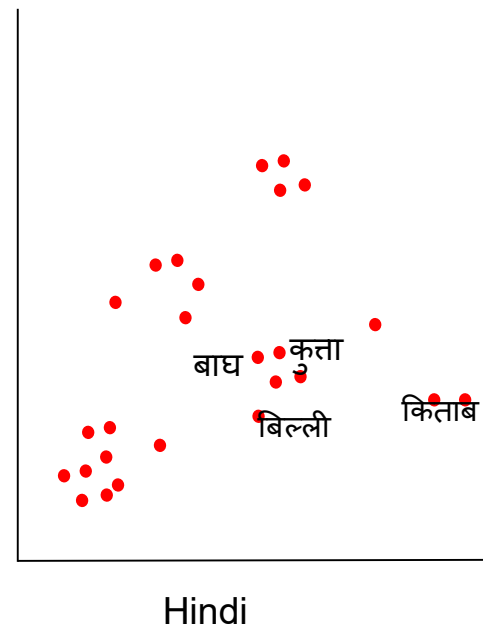
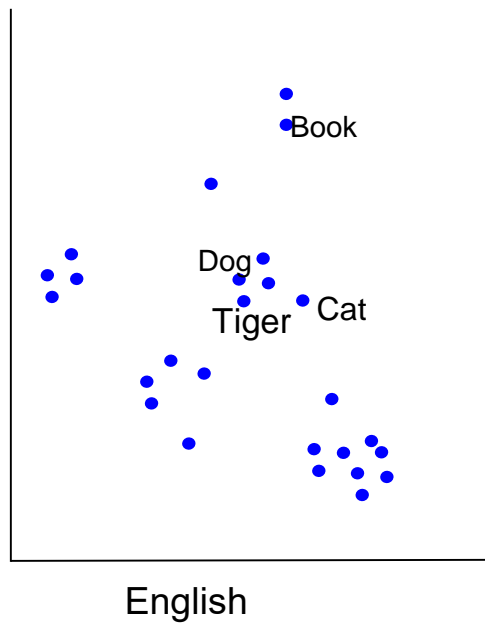
*haa kambal khup naram aahe*

Manipuri:

*kampor asi mon mon laui*  
*blanket this soft soft is*



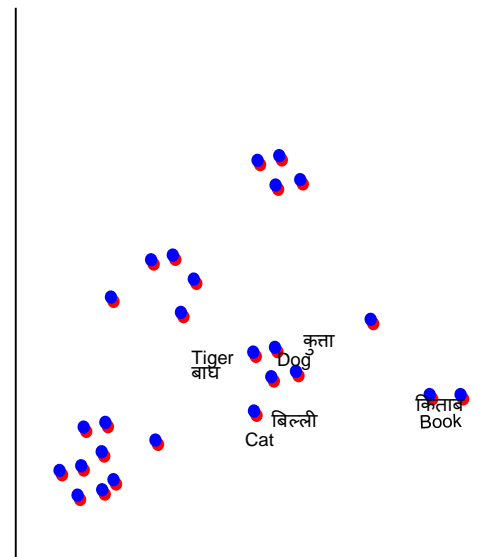
# ISO-Metricity



# Across Cross-lingual Mapping

This involves strong assumption that embedding spaces across languages are isomorphic, which is not true specifically for distance languages (Søgaard et al. 2018). However, without this assumption unsupervised NMT is not possible.

Søgaard, Anders, Sebastian Ruder, and Ivan Vulić. 2018. On the limitations of unsupervised bilingual dictionary induction. ACL

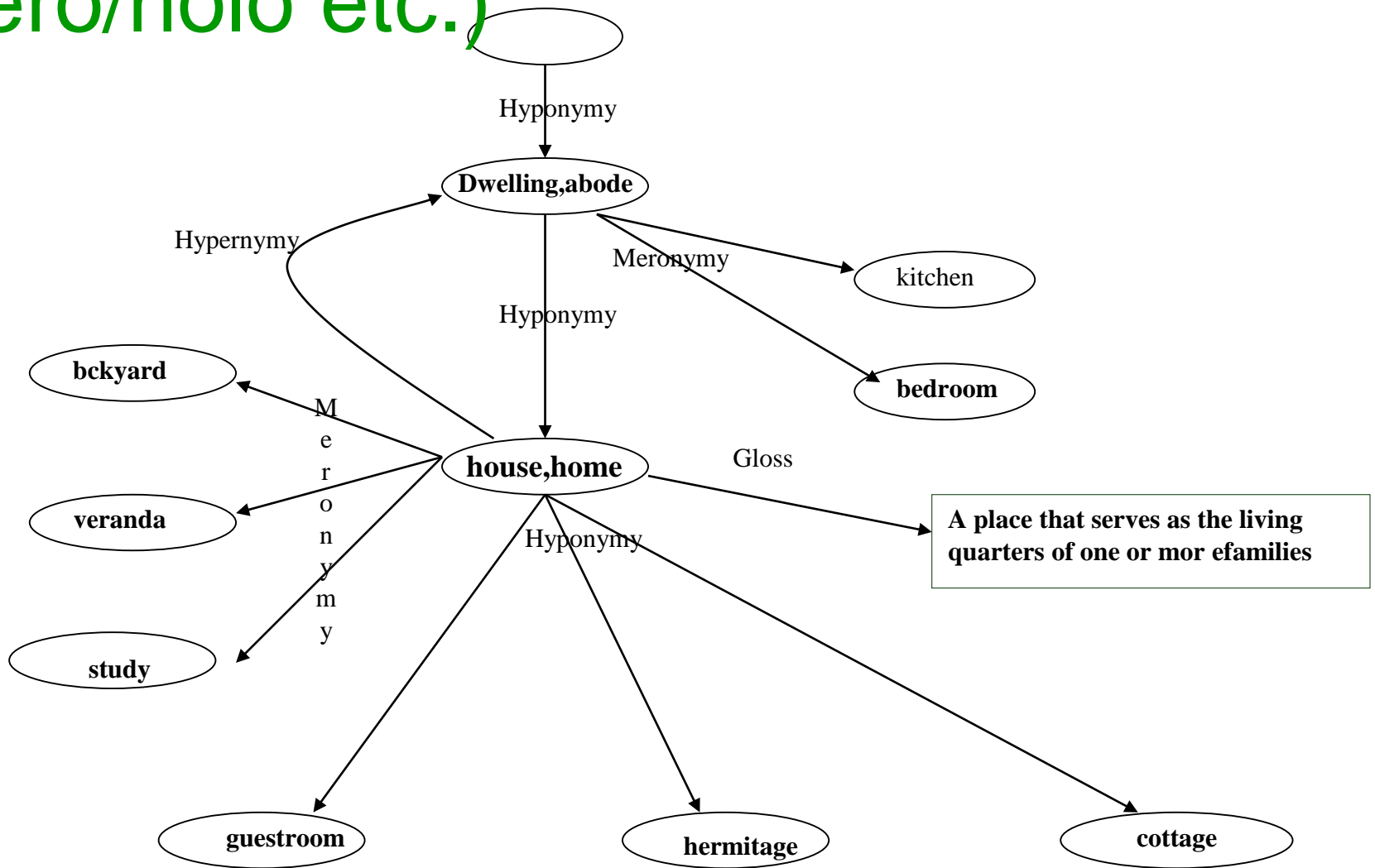




# Foundations-4: Syntagmatic and Paradigmatic Relations

- Syntagmatic and paradigmatic relations
  - Lexico-semantic relations: synonymy, antonymy, hypernymy, meronymy, troponymy etc. **CAT is-a ANIMAL**
  - Cooccurrence: **CATS MEW**
- Wordnet: primarily paradigmatic relations
- ConceptNet: primarily Syntagmatic Relations

# WordNet Sub-Graph with lexico-semantic relations (hyper/hypo, mero/holo etc.)



# Lexical and Semantic relations in wordnet

1. Synonymy (e.g., *house, home*)
  2. Hypernymy / Hyponymy (kind-of, e.g., *cat*  $\leftrightarrow$  *animal*)
  3. Antonymy (e.g., *white and black*)
  4. Meronymy / Holonymy (part of, e.g., *cat and tail*)
  5. Gradation (e.g., *sleep*  $\rightarrow$  *doze*  $\rightarrow$  *wake up*)
  6. Entailment (e.g., *snoring*  $\rightarrow$  *sleeping*)
  7. Troponymy (manner of, e.g., *whispering and talking*)
- 1, 3 and 5 are lexical (*word to word*), rest are semantic (*synset to synset*).

# 'Paradigmatic Relations' and 'Substitutability'

- Words in paradigmatic relations can substitute each other in the sentential context
- E.g., 'The cat is drinking milk' → 'The animal is drinking milk'
- Substitutability is a foundational concept in linguistics and NLP

# Foundations-5: Learning and Learning Objective

- Probability of getting the context words given the target should be maximized (skip gram)
- Probability of getting the target given context words should be maximized (CBOW)

# Learning objective (skip gram)

$$J'(\theta) = \frac{1}{T} \prod_{t=1}^T \prod_{\substack{-m \leq j \leq m \\ j \neq 0}} p(w_{t+j} | w_t; \theta)$$

$$J(\theta) = -\frac{1}{T} \prod_{t=1}^T \prod_{\substack{-m \leq j \leq m \\ j \neq 0}} p(w_{t+j} | w_t; \theta)$$

$$\text{Minimize } L = -\sum_{t=1}^T \sum_{\substack{-m \leq j \leq m \\ j \neq 0}} \log[p(w_{t+j} | w_t; \theta)]$$

# Modelling $P(\text{context word}|\text{input word})$ (1/2)

- We want, say,  $P(\text{'bark'}|\text{'dog'})$
- Take the weight vector **FROM** 'dog' neuron **TO** projection layer (call this  $u_{dog}$ )
- Take the weight vector **TO** 'bark' neuron **FROM** projection layer (call this  $v_{bark}$ )
- When initialized  $u_{dog}$  and  $v_{bark}$  give the initial estimates of word vectors of 'dog' and 'bark'
- The weights and therefore the word vectors get fixed by back propagation

# Modelling $P(\text{context word}|\text{input word})$

## (2/2)

- To model the probability, first compute dot product of  $u_{dog}$  and  $v_{bark}$
- Exponentiate the dot product
- Take softmax over all dot products over the whole vocabulary

$$P('bark'|'dog') = \frac{\exp(u_{dog}^T v_{bark})}{\sum_{v_k \in \text{Vocabulary}} \exp(u_{dog}^T v_k)}$$



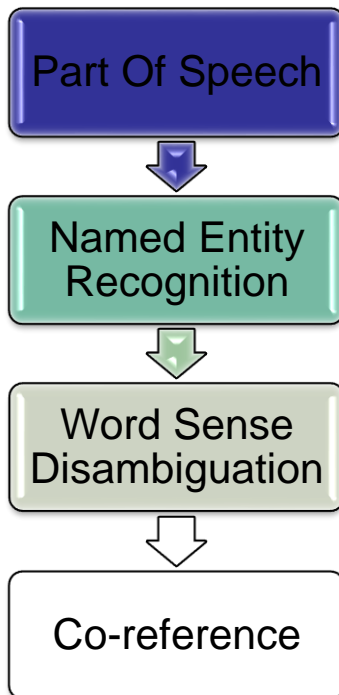
# Exercise

- Why cannot you model  $P(\text{'bark'}|\text{'dog'})$  as the ratio of counts of  $\langle \text{bark, dog} \rangle$  and  $\langle \text{dog} \rangle$  in the corpus?
- Why this way of modelling probability through dot product of weight vectors of input and output words, exponentiation and soft-maxing works?

# Possible project ideas

# Semantics Extraction using Universal Networking Language

**Sentence:** *I went with my friend, John, to the bank to withdraw some money but was disappointed to find it closed.*



*Current work:*

*Combine Machine learning with rule Based technique (Janardhan)*

*Agt(go,I)  
Ptn(go,friend)  
Nam(friend,John)  
Plt(go,bank)  
Pur(go, withdraw)  
Obj(withdraw,money0  
Mod(money,some)  
And(go,disappoint)*

# Sentiment Analysis

“The water is boiling.”: Objective

“He is boiling with anger.”: Negative

*Current work:*

- 1. Tweet and Blog Sentiment*
- 2. Indian Language Sentiment Analysis*
- 3. Word Sense and Sentiment*
- 4. Thwarting and*  
(Subhabrata and Akshat, Balamurali)

# Text Entailment

	<b>TEXT</b>	<b>HYPOTHESIS</b>	<b>ENTAILMENT</b>
1	<i>. The Hubble is the only large visible light and ultra-violet space telescope we have in operation.</i>	<i>Hubble is a Space telescope.</i>	True
2	<i>Google files for its long awaited IPO.</i>	<i>Google goes public.</i>	True
3	<i>After the deal closes, Teva will earn about \$7 billion a year, the company said.</i>	<i>Teva earns \$7 billion a year.</i>	False

*Current work: Do entailment from Semantic Graphs (Arindam, Janradhan)*

# Indowordnet and Multilingual Word Sense Disambiguation

The screenshot displays the Indowordnet interface for the synset ID 4496, which is a noun. The main content area shows the word 'अर्जुन' (Arjuna) in Hindi, along with its synonyms, gloss, and an example statement. The interface also features a search bar, a list of relations, and a list of words in other languages.

**Synset ID : 4496 POS : noun**

**Synonyms :** अर्जुन, धर्मजय, धर्मजय, पार्थ, पाकशासनि, अनीलबाजी, लव्यसाथी, अनघ, ऐंद्र, ऐन्द्र, किरोटमाली, कौनोंय, कौटिष, भारत, पंवी, धन्वी, श्वेतवाह, श्वेतवाहन, बासवी, शङ्खान्धज, शङ्खंदन, शङ्खनन्दन, सुनर, नर,

**Gloss :** पांडु का शैलस पुत्र

**Example statement :** "अर्जुन बहुत बड़े धनुर्धर थे"

**Gloss in Hindi :** पांडु का शैलस पुत्र

**Gloss in English :** (Hindu mythology) the warrior prince in the Bhagavad-Gita to whom Krishna explains the nature of being and of God and how humans can come to know God

**Relations**

- hypernymy •
- hyponymy •
- holonymy •
- meronymy •
- antonymy •
- Onto tree •
- noun relation •
- verb relation •
- derived from •
- modifies •

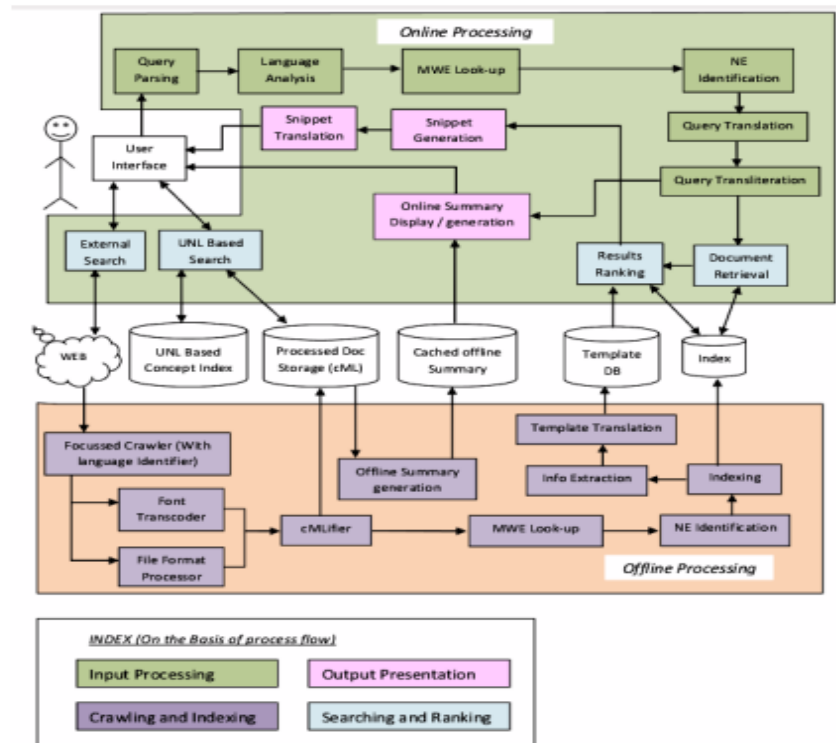
**Words in other language**

- हिन्दी Hindi •
- English •
- Assamী (Assamese) •
- বাংলা (Bengali) •
- bodo •
- ગુજરાતી (Gujarati) •
- ಕನ್ನಡ (Kannada) •
- کٔشٔمیری (Kashmiri) •
- konkani •
- മലയാളം (Malayalam) •
- manipuri •
- मराठी (Marathi) •
- नेपाली (Nepali) •
- संस्कृत (Sanskrit) •
- தமிழ் (Tamil) •

Current work: Linking wordnets with SUMO Ontology; using resources of one Language for another for WSD (Salil Joshi, Arindam Chatterjee, Brijesh, Mitesh)

# Cross Lingual Information Retrieval

## Architecture of Sandhan



Current work: Performance Enhancement; Query expansion and disambiguation (Yogesh, Arjun, Swapnil)

# Machine Translation

Large Projects funded by  
Yahoo, Xerox, Ministry of IT

*Current work:*

- 1. Indian Language to Indian Language*
- 2. Statistical MT*
- 3. Crowdsourcing and MT*
- 4. Semantics and SMT*

(Mitesh, Anoop, Victor, Somya, Abhijit, Raj,  
Rahul)



Sites:

<http://www.cse.iitb.ac.in/~pb>

<http://www.cfilt.iitb.ac.in>