

*Rule W1*

After sending a basic message to a process  $P_i$  :

$$\begin{aligned} CTR_w &= CTR_w + 1; \\ NB_w &= NB_w \cup \{P_i\}; \end{aligned}$$

(e)  $(P_s, (ACK, Seq_s), P_w)$  :

$$\begin{aligned} CTR_w &= CTR_w - 1; \\ Seq_w &= \max(Seq_w, Seq_s); \end{aligned}$$

(f) Otherwise :

Ignore the message.

*Rule W2*

Upon receipt of a message from  $P_s$  :  
CASE message of

(a) basic message :

```
if (NOTDEL = TRUE) then
    /* basic message is returned */
    CTR_w = CTR_w - 1;
    NB_w = NB_w - {P_s};
else
    SEND(P_w, (ACK, Seq_w), P_s);
    NB_w = NB_w ∪ {P_s};
```

(b)  $(P_s, (TD, PI_j, BS_s), P_w)$  :
 $Seq_w = \max(Seq_w, PI_j.Seq);$

(c)  $(P_s, (KM, PI_s, S_s, NB_s), P_w)$  :
 $Seq_w = \max(Seq_w, PI_s.Seq);$ 
 $NB_w = NB_w ∪ {S_s} - \{P_s\}$ ;
if ( $P_w \in PMSET$ ) then
 /\*  $P_w$  is a permanent process \*/
 Deadset\_w = Deadset\_w ∪ {P\_s};
if ( $P_w = S_s$ ) then
  $NB_w = NB_w ∪$ 
 $NB_s - \{P_w\} - Deadset_w;$

(d)  $(P_s, (KP, PI_s), P_w)$  :
while ( $CTR_w \neq 0$ ); /\* wait! \*/
 $Seq_w = \max(Seq_w, PI_s.Seq);$ 
 $\forall P_j \in NB_w \cup PMSET,$ 
 $SEND(P_w, (KM, PI_w, S_w, NB_w),$ 
 $P_j);$ 
(KILL  $P_w$ );

*Rule W3*

Upon creating a process  $P_c$  :

$$\begin{aligned} NB_w &= NB_w \cup \{P_c\}; \\ NB_c &= \{P_w\}; \\ Seq_c &= Seq_w; \\ S_c &= S_w; \end{aligned}$$

*Rule W4*

Upon deciding to kill a process  $P_v$  :

SEND( $P_w, (KP, PI_w), P_v$ );

*Rule W5*

Upon deciding to kill itself :

```
while ( $CTR_w \neq 0$ ); /* wait! */
 $\forall P_j \in NB_w \cup PMSET,$ 
    SEND( $P_w, (KM, PI_w, S_w, NB_w), P_j$ );
(KILL  $P_w$ );
```

*Rule W6*

Upon completing its basic computation :

```
while ( $CTR_w \neq 0$ ); /* wait! */
if ( $NB_w = \phi$ ) then (TERMINATE);
 $Seq_w = Seq_w + 1;$ 
 $LPI_w = <Seq_w, w>;$ 
 $CLR_w = black;$ 
 $PAR_w = nil;$ 
 $TDSET_w = NB_w;$ 
 $\forall P_j \in TDSET_w,$ 
    SEND( $P_w, (TD, LPI_w, NB_w \cup \{P_w\}),$ 
         $P_j$ );
```

Figure 2: Rules for a *white* process  $P_w$

*Rule B1*

Upon receipt of a basic message from  $P_s$  :  
 $\text{SEND}(P_b, (\text{ACK}, \text{Seq}_b), P_s);$   
 $NB_b = NB_b \cup \{P_s\};$   
 $CLR_b = \text{white};$

*Rule B2*

Upon receipt of a  $(P_s, (TD, PI_j, BS_s), P_b)$  :  
if  $(PI_j > LPI_b)$  then  
 $LPI_b = PI_j;$   
 $\text{Seq}_b = \max(\text{Seq}_b, PI_j.\text{Seq});$   
 $PAR_b = P_s;$   
if  $((NB_b - BS_s) = \phi)$  then  
 $\text{SEND}(P_b, (RT, PI_j), P_s);$   
 $CLR_b = \text{red} ;$   
else /\* propagate the TD \*/  
 $TDSET_b = NB_b - BS_s;$   
 $\forall P_k \in TDSET_b,$   
 $\text{SEND}(P_b, (TD, PI_j, BS_s \cup NB_b),$   
 $P_k);$   
else /\*  $PI_j \leq LPI_b$  \*/  
if  $(PI_j = LPI_b)$  then  
 $\text{SEND}(P_b, (RT, PI_j), P_s);$

*Rule B3*

Upon receipt of a  $(P_s, (RT, PI_j), P_b)$  :  
if  $(PI_j = LPI_b)$  then  
/\* Reply to the latest TD sent \*/  
if  $(P_s \in NB_b)$  then  
 $TDSET_b = TDSET_b - \{P_b\};$   
if  $(TDSET_b = \phi)$  then  
if  $(PAR_b = \text{nil})$  then  
/\* Termination detected ! \*/  
 $\forall P_k \in NB_b,$   
 $\text{SEND}(P_b, (\text{TER}, NB_b \cup \{P_b\}),$   
 $P_k);$   
(TERMINATE);  
else /\*  $PAR_b \neq \text{nil}$  \*/  
 $\text{SEND}(P_b, (RT, PI_j), PAR_b);$   
 $CLR_b = \text{red};$

*Rule B4*

Upon receipt of a  $(P_s, (KP, PI_s), P_b)$  :  
 $\text{Seq}_b = \max(\text{Seq}_b, PI_s.\text{Seq});$   
 $\forall P_j \in NB_b \cup PMSET,$   
 $\text{SEND}(P_b, (KM, PI_b, S_b, NB_b), P_j);$   
(KILL  $P_b$ );

*Rule B5*

Upon receipt of a  $(P_s, (KM, PI_s, S_s, NB_s), P_b)$  :  
if  $(PAR_b = P_s)$  then  $PAR_b = S_s;$   
if  $(P_b \in PMSET)$  then  
/\*  $P_b$  is a permanent process \*/  
 $Deadset_b = Deadset_b \cup \{P_s\};$   
 $NB_b = NB_b - \{P_s\};$   
if  $(P_b = S_s)$  then  
 $NB_b = NB_b \cup NB_s - \{P_b\} - Deadset_b;$   
else /\*  $P_b$  is not permanent \*/  
 $NB_b = NB_b \cup \{S_s\} - \{P_s\};$   
if  $(NB_b = \phi)$  then (TERMINATE);  
else  
/\* Initiate new TD \*/  
 $\text{Seq}_b = \max(\text{Seq}_b, PI_s.\text{Seq}) + 1;$   
 $LPI_b = <\text{Seq}_b, b>;$   
 $PAR_b = \text{nil};$   
 $TDSET_b = NB_b;$   
 $\forall P_k \in TDSET_b,$   
 $\text{SEND}(P_b, (TD, LPI_b, NB_b \cup \{P_b\}),$   
 $P_k);$

Figure 3: Rules for a *black* process  $P_b$

*Rule R1*

Upon receipt of a basic message from  $P_s$  :  
 $\text{SEND}(P_r, (\text{ACK}, \text{Seq}_r), P_s);$   
 $NB_r = NB_r \cup \{P_s\};$   
 $CLR_r = \text{white};$

*Rule R2*

Upon receipt of a  $(P_s, (TD, PI_j, BS_s), P_r)$  :  
if  $(PI_j > LPI_r)$  then  
 $LPI_r = PI_j;$   
 $\text{Seq}_r = \max(\text{Seq}_r, PI_j.\text{Seq});$   
 $PAR_r = P_s;$   
if  $((NB_r - BS_s) = \emptyset)$  then  
 $\text{SEND}(P_r, (RT, PI_j), P_s);$   
else /\* propagate the TD \*/  
 $TDSET_r = NB_r - BS_s;$   
 $\forall P_k \in TDSET_r,$   
 $\text{SEND}(P_r, (TD, PI_j, BS_s \cup NB_r), P_k);$   
 $CLR_r = \text{black};$   
else /\*  $PI_j \leq LPI_r$  \*/  
if  $(PI_j = LPI_r)$  then  
 $\text{SEND}(P_r, (RT, PI_j), P_s);$

*Rule R3*

Upon receipt of a  $(P_s, (RT, PI_j), P_r)$  :  
Ignore the message;

*Rule R4*

Upon receipt of a  $(P_s, (KP, PI_s), P_r)$  :  
 $\text{Seq}_r = \max(\text{Seq}_r, PI_s.\text{Seq});$   
 $\forall P_j \in NB_r \cup PMSET,$   
 $\text{SEND}(P_r, (KM, PI_r, S_r, NB_r), P_j);$   
(KILL  $P_r$ );

*Rule R5*

Upon receipt of a  $(P_s, (KM, PI_s, S_s, NB_s), P_r)$  :  
if  $(PAR_r = P_s)$  then  $PAR_r = S_s;$   
if  $(P_r \in PMSET)$  then  
/\*  $P_r$  is a permanent process \*/  
 $Deadset_r = Deadset_r \cup \{P_s\};$   
 $NB_r = NB_r - \{P_s\};$   
if  $(P_r = S_s)$  then  
 $NB_r = NB_r \cup NB_s - \{P_r\} - Deadset_r;$   
else /\*  $P_r$  is not permanent \*/  
 $NB_b = NB_b \cup \{S_s\} - \{P_s\};$   
if  $(NB_b = \emptyset)$  then (TERMINATE);  
 $\text{Seq}_r = \max(\text{Seq}_r, PI_s.\text{Seq}) + 1;$   
 $LPI_r = <\text{Seq}_r, r>;$   
 $PAR_r = \text{nil};$   
 $TDSET_r = NB_r;$   
 $\forall P_k \in TDSET_r,$   
 $\text{SEND}(P_r, (TD, LPI_r, NB_r \cup \{P_r\}), P_k);$   
 $CLR_r = \text{black};$

*Rule R6*

Upon receipt of a  $(P_s, (TER, BS_s), P_r)$  :  
 $\forall P_k \in (NB_r - BS_s),$   
 $\text{SEND}(P_r, (TER, NB_r \cup BS_s), P_k);$   
(TERMINATE);

Figure 4: Rules for a *red* process  $P_r$