

# Optimizing Multivariate Performance Measures for Learning Relation Extraction Models

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# Outline

Introduction

Preliminaries

Max-margin method for Optimizing Multi-variate Performance Measures

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## Relation Extraction

*Xerox Corporation is an American multinational company headquartered in Norwalk, Connecticut. On May 21, 2009, it was announced that Ursula Burns would be the CEO of Xerox.*

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Can we leverage already existing high quality databases (e.g. Freebase) to learn good relation extractors ?



# Distant Supervision for Relation Extraction

Mintz et al. (2009)

## Knowledge base

$r$	$e_1$	$e_2$
BornIn	Barack Obama	U. S.
PresidentOf	Barack Obama	U. S.

## Sentences

- *Barack Obama* was born in Honolulu, Hawaii, *United States*.
- *Obama* left *United States* this Saturday for a UN summit in Geneva.
- President *Obama* defended his administrations' collection of phone records in the *U.S.*

# Distant Supervision based Relation Extraction

Mintz et al. (2009)

Knowledge base		
$r$	$e_1$	$e_2$
BornIn	Barack Obama	U. S.
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## Sentences

## Latent Label

- *Barack Obama* was born in Honolulu, Hawaii, *United States*. *BornIn*
- *Obama* left *United States* this Saturday for a UN summit in Geneva. *none*
- President *Obama* defended his administrations' collection of phone records in the *U.S.* *PresidentOf*

## Multiple instance, multiple label

Riedel et al. (2010); Hoffmann et al. (2011); Surdeanu et al. (2012)

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- ▶ However, these are not directly related to evaluation measures (e.g.: F1-score, area under ROC curve)
- ▶ **Training Objective**  $\Leftrightarrow$  **Evaluation Measure**

## Motivation (cont.)

- ▶ Can we train better models by directly optimizing task specific performance measures while allowing latent variables to adapt their values

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- ▶ Further, can we provide a knob in the training algorithm to favor *precision* more than *recall*



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  - ▶ CCCP : used to populate latent variables
  - ▶ Dual decomposition: factorizes the hard optimization problem (during training) into independent sub-problems
  - ▶ We present linear programming (LP) and local search methods to solve the sub-problems

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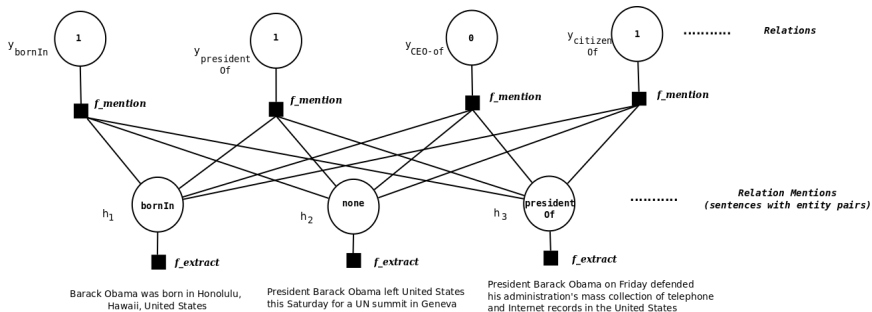
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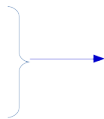
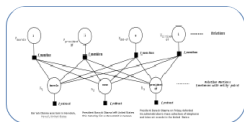
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# Preliminaries



**Figure:** Graphical model instantiated for entity pair  $x := (\text{Barack Obama, United States})$

## Preliminaries



*one data-point*

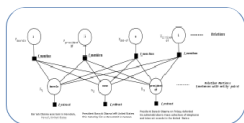
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$y$ : relation labels

$h$ : latent mention labels



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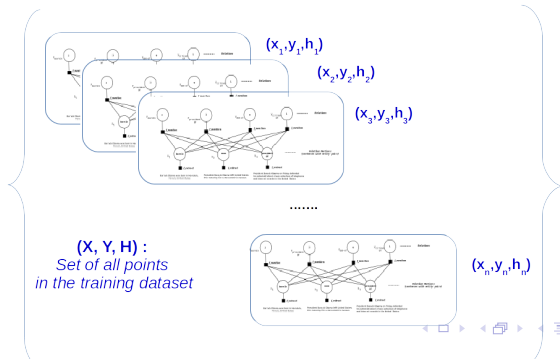


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## Structured Prediction Learning

- ▶ Goal: To find  $\mathbf{w} \in R^d$  that minimizes risk

$$R_{f_{\mathbf{w}}}^{\Delta} := \Delta\left(\left(f_{\mathbf{w}}(\mathbf{x}_1), \dots, f_{\mathbf{w}}(\mathbf{x}_N)\right), \left(\mathbf{y}_1, \dots, \mathbf{y}_N\right)\right)$$

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- ▶ Most large margin learning algorithms assume that loss is decomposable. So  $R_{f_{\mathbf{w}}}^{\Delta}$  is simplified to,

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- ▶ However, for non-decomposable loss functions like  $-F_1$ ,  $\Delta$  cannot be expressed in terms of  $\delta$

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- ▶ In decomposable structure prediction task, our aim is to learn  $\mathbf{w} \in \mathbb{R}^d$  such that for a new entity pair  $\mathbf{x}$ , we can find:

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- ▶ Instead of learning a mapping function from an individual instance to its label, we learn a mapping from all instances to their labels
- ▶ We define the best labeling using the following linear discriminant function

$$\mathbf{f}(\mathbf{X}) := \arg \max_{\mathbf{Y}' \in \mathcal{Y}} \max_{\mathbf{H} \in \mathcal{H}} \left\{ \mathbf{w} \cdot \Psi(\mathbf{X}, \mathbf{H}, \mathbf{Y}') \right\}$$

where  $\Psi(\mathbf{X}, \mathbf{H}, \mathbf{Y}') := \sum_{i=1}^N \Phi(\mathbf{x}_i, \mathbf{h}_i, \mathbf{y}'_i)$

## Training Objective

- ▶ Based on margin re-scaling formulation of structured prediction problems, our training objective is:

$$\min_{\mathbf{w}} \frac{1}{2} \|\mathbf{w}\|_2^2 + C \max_{\mathbf{y}'_1, \dots, \mathbf{y}'_N} \left\{ \Delta \left( (\mathbf{y}_1, \dots, \mathbf{y}_N), (\mathbf{y}'_1, \dots, \mathbf{y}'_N) \right) \right. \\ \left. + \sum_{i=1}^N \max_{\mathbf{h}} \mathbf{w} \cdot \Phi(\mathbf{x}_i, \mathbf{h}, \mathbf{y}'_i) - \sum_{i=1}^N \max_{\mathbf{h}} \mathbf{w} \cdot \Phi(\mathbf{x}_i, \mathbf{h}, \mathbf{y}_i) \right\}$$

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- ▶ The above objective is non-convex since it is the difference of two convex functions

## Convex-concave Procedure (CCCP)

- ▶ Refer to Yuille and Rangarajan (2001) and Sriperumbudur and Lanckriet (2012)
- ▶ CCCP is a special example of Majorization-Minimization (class of) algorithm(s)
- ▶ Elaborate Convergence proof for constrained version by Sriperumbudur and Lanckriet (2012) using Zangwill's global convergence framework

$$\text{Training Objective} \quad \min_{\mathbf{w}} \frac{1}{2} \|\mathbf{w}\|_2^2 + C \max_{\mathbf{y}'_1, \dots, \mathbf{y}'_N} \left\{ \Delta \left( (\mathbf{y}_1, \dots, \mathbf{y}_N), (\mathbf{y}'_1, \dots, \mathbf{y}'_N) \right) \right.$$

$$\left. + \sum_{i=1}^N \max_{\mathbf{h}} \mathbf{w} \cdot \Phi(\mathbf{x}_i, \mathbf{h}, \mathbf{y}'_i) - \sum_{i=1}^N \max_{\mathbf{h}} \mathbf{w} \cdot \Phi(\mathbf{x}_i, \mathbf{h}, \mathbf{y}_i) \right\}$$

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**Algorithm 1** The Training Algorithm

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- 1: **procedure** OPT-LATENTSVM( $\mathbf{X}, \mathbf{Y}$ )
- 2:     Initialize  $\mathbf{w}^{(0)}$  and set  $t = 0$
- 3:     **repeat**
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  - 5:        $\mathbf{h}_i^* := \arg \max_{\mathbf{h}} \mathbf{w}^{(t)} \cdot \Phi(\mathbf{x}_i, \mathbf{h}, \mathbf{y}_i)$
  - 6:       **Convex Step:**
  - 7:       Given the best assignment of latent variables,  
Solve for  $\mathbf{w}$  (via cutting plane algorithm)
  - 8:   **until** some stopping condition is met
  - 9:   **return**  $\mathbf{w}^{(t)}$
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        // Optimizing Eq 12
6:        $\mathbf{w}^{(t+1)} := \text{optSVM}(\mathbf{X}, \mathbf{H}^*, \mathbf{Y})$ 
7:        $t := t + 1$ 
8:   until some stopping condition is met
9:   return  $\mathbf{w}^{(t)}$ 

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## Convex Step: Loss Augmented Inference

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- ▶ We employ dual decomposition to decouple the two terms and efficiently find an approximate solution

## Dual Decomposition

$$\begin{aligned} \max_{\mathbf{y}'_1, \dots, \mathbf{y}'_N} \quad & \Delta \left( (\mathbf{y}_1, \dots, \mathbf{y}_N), (\mathbf{y}'_1, \dots, \mathbf{y}'_N) \right) \\ & + \sum_{i=1}^N \max_{\mathbf{h}} \mathbf{w} \cdot \Phi(\mathbf{x}_i, \mathbf{h}, \mathbf{y}'_i) \end{aligned}$$

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$$\underbrace{\max_{\mathbf{y}'_1, \dots, \mathbf{y}'_N, \mathbf{y}''_1, \dots, \mathbf{y}''_N} \Delta \left( (\mathbf{y}_1, \dots, \mathbf{y}_N), (\mathbf{y}'_1, \dots, \mathbf{y}'_N) \right)}_{\text{}} \quad \left. \vphantom{\max} \right\} \rightarrow$$

$$+ \sum_{i=1}^N \max_{\mathbf{h}} \mathbf{w} \cdot \Phi(\mathbf{x}_i, \mathbf{h}, \mathbf{y}''_i) \quad \left. \vphantom{\sum} \right\} \rightarrow$$

subject to

$$\forall i \in \{1, \dots, N\}, \forall \ell \in \{1, \dots, L\}, \quad y'_{i,\ell} = y''_{i,\ell}$$

**Two Independent Sub-problems**

## Dual Decomposition (cont.)

- ▶ After forming lagrangian, the dual objective function is derived as:

$$L(\Lambda) := \max_{\mathbf{Y}'} \Delta(\mathbf{Y}, \mathbf{Y}') + \sum_i \sum_{\ell} \lambda_i(\ell) y'_{i,\ell} \quad \left. \vphantom{\sum_i \sum_{\ell} \lambda_i(\ell) y'_{i,\ell}} \right\} \rightarrow \text{"loss-lagrangian"}$$

$$\max_{\mathbf{Y}''} \sum_{i=1}^N \max_{\mathbf{h}} \mathbf{w} \cdot \Phi(\mathbf{x}_i, \mathbf{h}, \mathbf{y}_i'') - \sum_i \sum_{\ell} \lambda_i(\ell) y''_{i,\ell} \quad \left. \vphantom{\sum_i \sum_{\ell} \lambda_i(\ell) y''_{i,\ell}} \right\} \rightarrow \text{"model-lagrangian"}$$

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- ▶ Since  $L(\Lambda)$  is an upper-bound on the original loss-augmented inference, we find the tightest upper-bound as an approximate solution:  $\min_{\Lambda} L(\Lambda)$
- ▶ This is solved via sub-gradient descent method

## Optimization of the Dual - Multivariate Loss

$$\mathbf{Y}'_* := \arg \max_{\mathbf{Y}'} \Delta(\mathbf{Y}, \mathbf{Y}') + \sum_i \sum_{\ell} \lambda_i^{(t-1)}(\ell) y'_{i,\ell}$$

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- ▶ However, loss term can be expressed in terms of aggregate statistics over  $\mathbf{Y}'$  (false positives (FPs) and false negatives (FNs) )



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- ▶ However, loss term can be expressed in terms of aggregate statistics over  $\mathbf{Y}'$  (false positives (FPs) and false negatives (FNs) )
- ▶ Since FPs and FNs are integral it can take finite values which can be represented on a two-dimensional grid and efficiently searched via a local search algorithm

## Local Search Algorithm

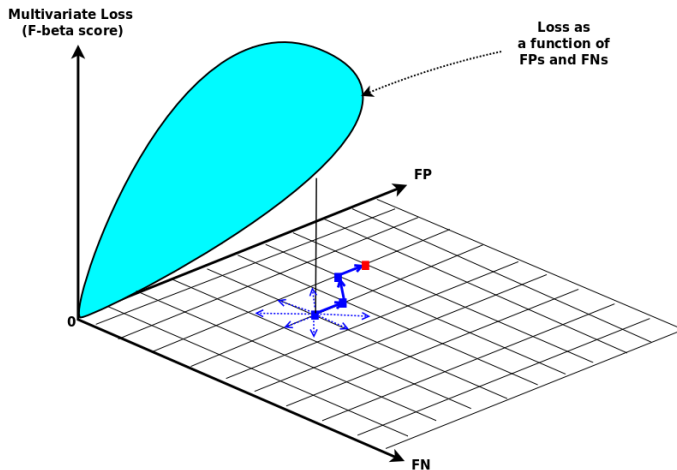


Figure: Local Search Algorithm : An Illustration

## Optimization of the Dual - Model Lagrangian

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- ▶ This problem is as difficult as the MAP inference in the underlying graphical model (NP-hard for loopy graphs)
- ▶ We use ILP formulations (relaxed to LP) to solve this

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- ▶ Dataset: We used the benchmark dataset created by Riedel et. al. (2010)
- ▶ Baseline: Hoffmann et. al.'s (2011) state-of-the-art distantly supervised relation extractor
- ▶ Our approaches:
  - ▶ Max-margin which optimizes simple decomposable (Hamming) loss
  - ▶ Max-margin which optimizes non-decomposable  $-F_\beta$  loss

$$F_\beta := \frac{1}{\frac{\beta}{\text{Precision}} + \frac{1-\beta}{\text{Recall}}}$$

## Training on sub-samples of data

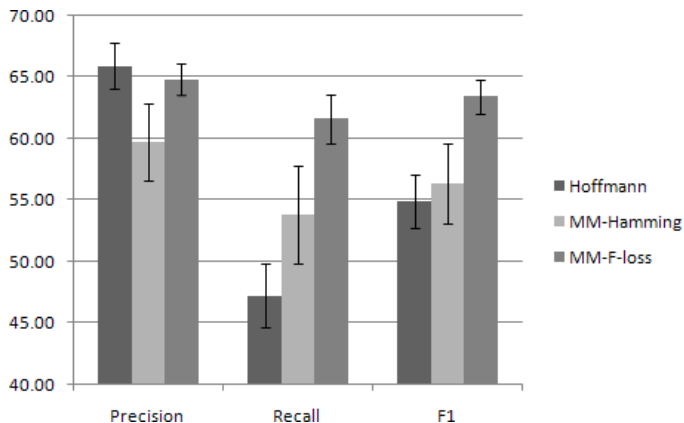


Figure: Experiments on 10% Riedel datasets.

## Tuning towards Precision/Recall

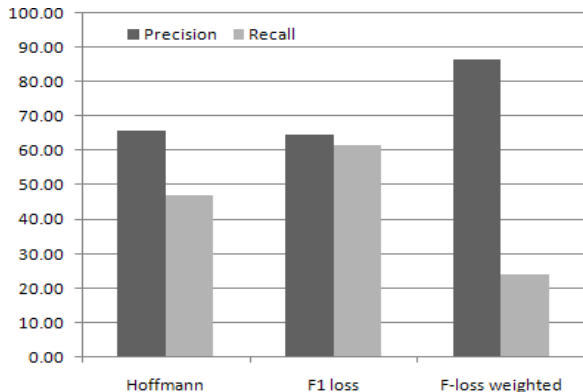


Figure: Weighting of Precision and Recall ( $\beta = 0.833$ )

## Accuracies on the entire dataset

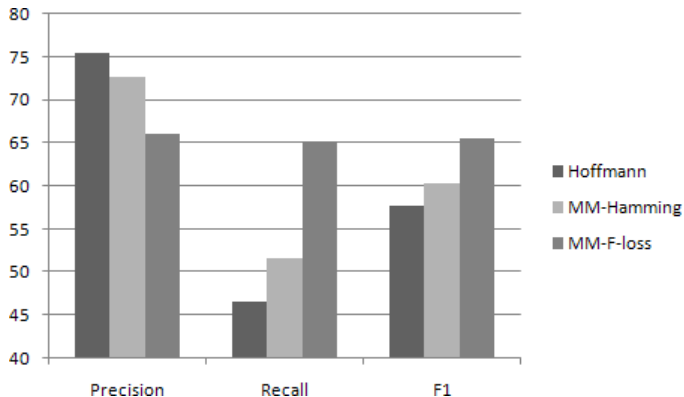


Figure: Overall accuracies Riedel dataset

# Outline

Introduction

Preliminaries

Max-margin method for Optimizing Multi-variate Performance Measures

Experiments

Conclusion

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- ▶ Described a novel max-margin approach to optimize non-linear performance measures, such as  $F_\beta$ , in distant supervision of information extraction models
- ▶ Our approach is general and can be applied to other latent variable models in NLP
- ▶ Our approach involves solving the hard-optimization problem in learning by interleaving Concave-Convex Procedure with dual decomposition



## Conclusion

- ▶ Under several conditions, we have shown our technique outperforms very strong baselines, and results in up to 8.5% improvement in  $F_1$ -score

## Conclusion

- ▶ Under several conditions, we have shown our technique outperforms very strong baselines, and results in up to 8.5% improvement in  $F_1$ -score
- ▶ For future work:
  - ▶ Maximize other performance measures, such as area under the curve, for information extraction models
  - ▶ Explore our approach for other latent variable models in NLP, such as those in machine translation

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- ▶ National ICT Australia (**NICTA**) for their generous funding, as part of the Machine Learning Collaborative Research Projects.
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## Conclusion

Thank You!

*Code present at :*

[https://github.com/ajaynagesh/lsvm\\_relationextraction](https://github.com/ajaynagesh/lsvm_relationextraction)

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