Advanced Tools from Modern Cryptography

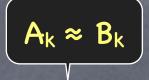
Lecture 8
Computational Security:
Indistinguishability, Simulation

Security Definitions

- So far: Perfect secrecy
 - Achieved in Shamir secret-sharing, passive BGW and passive GMW (given a trusted party for OT)
- But for 2PC using Yao's Garbled circuit (even given a trusted party for OT) security only against computationally bounded adversary
 - We haven't defined such security yet!
- @ Plan
 - Computational Indistinguishability
 - Simulation-based security

Because, the obvious definition obtained by replacing perfect secrecy by computational secrecy turns out to be weak

Indistinguishability



Distribution ensembles {A_k}, {B_k} computationally indistinguishable if ∃ negligible v(k) ∀ PPT tests T, ∀ sufficiently large k,
| Pr_{x←A_k}[T(x)=1] - Pr_{x←B_k}[T(x)=1] | ≤ v(k)

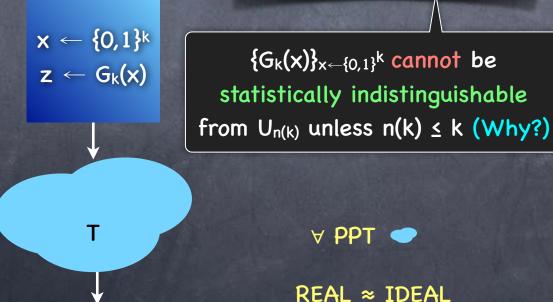


Pseudorandomness Generator (PRG)

Takes a short seed and (deterministically) outputs a long string

3 G_k:
$$\{0,1\}^{k} \rightarrow \{0,1\}^{n(k)}$$
 where $n(k) > k$



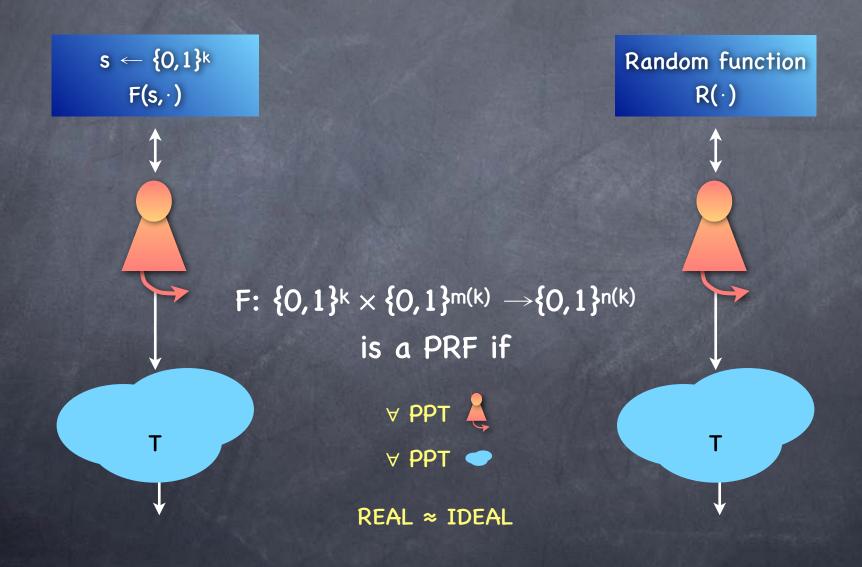




REAL

IDEAL

Pseudorandom Function (PRF)



REAL

IDEAL

Security for MPC

- Recall: For passive security, secrecy is all the matters
- For a 2-party functionality f, with only Bob getting the output, perfect secrecy against corrupt Bob:

i.e.,
$$\forall x, x', y \text{ s.t.}$$
, $f(x,y) = f(x',y)$, $view_{Bob}(x,y) = view_{Bob}(x',y)$

- In particular, if (y, f(x,y)) uniquely determines x (i.e., if $f(x',y)=f(x,y) \Rightarrow x'=x$), then OK for view to reveal x
- In the computational setting, just replace = with ≈?
 - We should ask for more!

Makes sense only for the view, not f

- E.g., f is a decryption algorithm, with key x and ciphertext y
- Often, a (long enough) ciphertext and message uniquely determines the key
 Because.
 - But not OK to reveal the key to Bob!

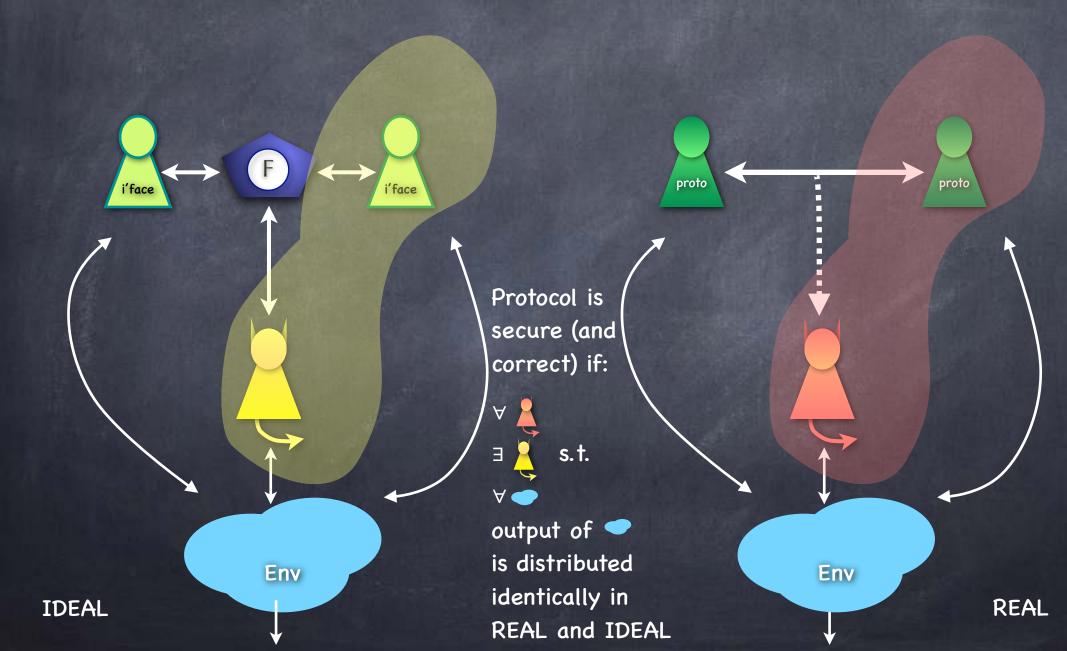
Because,
uniquely determines

≠ reveals!

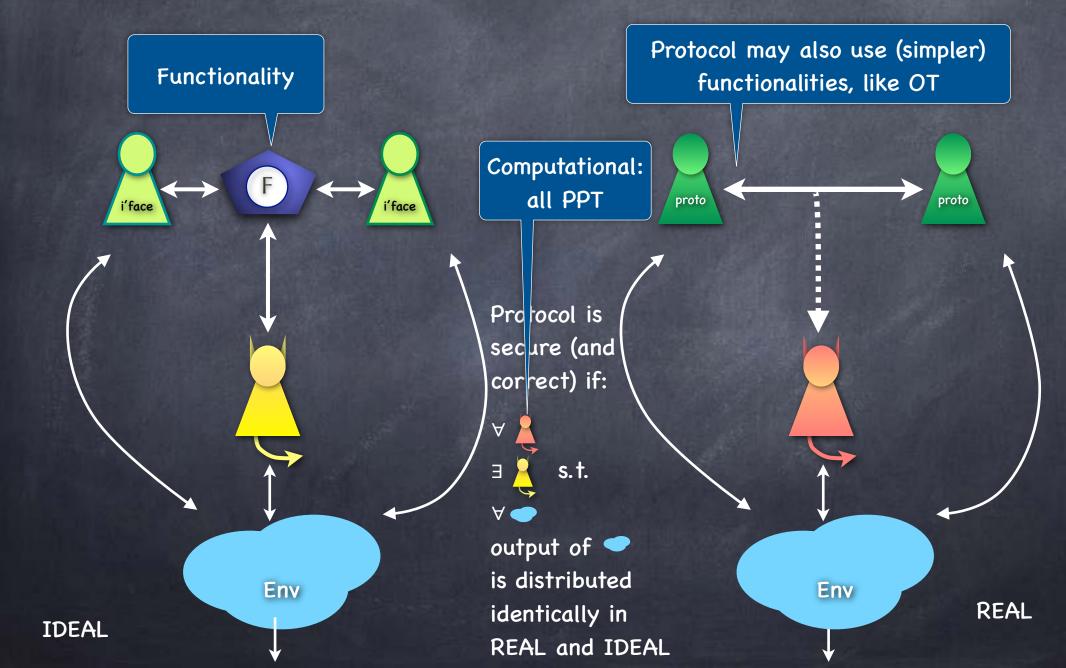
Security for MPC

- Compare the protocol execution with an "ideal" execution involving an incorruptible trusted party
 - Trusted party collects all inputs, carries out all computation and delivers the outputs (over private channels)
 - Ideal is the best we can hope for
- If anything that could "go wrong" with the protocol execution could happen with the ideal execution too, then it is not the protocol's fault
 - Applies to active, as well as passive corruption
 - Applies to computational as well as information-theoretic security

Simulation-Based Security



Simulation-Based Security



Variants of Security

- Same definitional framework to define various levels of security!
 - Passive adversary: corrupt parties stick to the protocol
 - Will require corrupt parties in the ideal world also to use the correct inputs/outputs
 - Universally Composable security: Active adversary interacting with the environment arbitrarily
 - Standalone security: environment is not "live." Interacts with the adversary before and after (but not during) the protocol
 - Super-PPT simulation: meaningful when the "security" of ideal world is information-theoretic
- Aside: Non-simulation-based security definitions for MPC are also useful for intermediate tools, but often too subtle for final applications

Example: Coin-Tossing

- Functionality F_{coin} samples a uniform random bit and sends it to all parties. (Adversary allowed to block the output to others, possibly after seeing its own output.)
- Security against passive corruption is trivial (Why?)
- Fact: Impossible to (even stand-alone) securely realise against computationally unbounded active adversaries
- Protocol for stand-alone security against PPT adversaries using commitment
 - If given ideal commitment functionality, information-theoretic security

Commitment

Commit now, reveal later

Intuitive properties: hiding and binding

COMMIT:

m
commit
m
NEXT DAY
REVEAL:

reveal
m
m
commit



Example: Coin-Tossing

- \odot Alice sends $a \in \{0,1\}$ to F_{com} . (Bob gets "committed" from F_{com})
- **3** Bob sends $b \in \{0,1\}$ to Alice
- Alice sends "open" to F_{com}. (Bob gets a from F_{com})
- Both output c=a⊕b
- Simulator:
 - $\ensuremath{\circ}$ Will get a bit c from F_{coin} . Needs to simulate the corrupt party's view in the protocol, including the interaction with F_{com}
 - If Alice corrupt: Get a from Alice. Send $b = a \oplus c$. (Block output if Alice doesn't send "open" to F_{com} .)
 - If Bob corrupt: Send "committed". Get b. Send a = b⊕c.
- Perfect simulation: Environment + Adversary's view is identically distributed in REAL and IDEAL (verify!), and hence so is Environment's output