Advanced Tools from Modern Cryptography

Lecture 9 MPC: Security Against Active Corruption

Handling Active Corruption

Need to ensure that there is a well-defined input for the adversary

Simulator should be able to "extract" the corrupt parties' inputs

Should make sure that the adversary cannot change the outcome

 Secrecy should hold even if the corrupt parties deviate from the protocol

General idea: catch deviations.

On catching a deviation an honest party may abort the protocol (if adversarial abort is allowed in the ideal world)

Or "deactivate" (potentially) corrupt players and continue the protocol. Possible when there is a large enough honest-majority

Note: Catching itself shouldn't reveal information about inputs

GMW Paradigm

Run a passive-secure protocol II, but let each party "verify" that the others are following the protocol correctly

- Correctly: pick arbitrary inputs and arbitrary randomness first, but then follow the specified program
- Verification should not reveal information: then cannot rely on passive security of Π any more!
 - How to verify without learning any information?
 - Zero-Knowledge Proofs!

Zero-Knowledge Proofs

Suppose Alice wants to convince Bob that a boolean formula in n-variables f(x₁,...,x_n) is satisfiable

I.e., ∃ values (v₁,...,v_n) such that $f(v_1,...,v_n) = 1$

- But doesn't want to reveal any "knowledge" about the solution to Bob (even if solution fully determined by f)
- Zero-Knowledge Proof functionality: F_{ZK}
 - Alice sends (f, (v₁,...,v_n)) to F_{ZK}, which sends f to Bob if f(v₁,...,v_n)=1
- Zero-Knowledge protocol: a 2-party secure computation protocol for the functionality F_{ZK}
 - Not interesting for passive corruption (of prover)

A ZK Proof for Graph Colorability

colors

G, coloring

revealedse

edge

Uses a commitment protocol as a subroutine At least 1/m probability of catching a wrong proof Soundness amplification: Repeat say mk times (with independent color permutations) Use random

pick random edge

> distinct colors?

Zero-Knowledge Proofs

- Traditional definition of ZK proofs is somewhat different
 - Simulation-based security for actively corrupt (standalone) verifier only
 - Security against prover: Soundness
 - Allows computationally unbounded corrupt provers
 - A corrupt prover should have negligible probability of getting the honest verifier to accept a false statement
- Our definition of ZK proofs corresponds to "Proof/Argument of Knowledge"
 - Argument: Soundness only against PPT prover
 - Showledge: Prover "knows" v s.t. f(v)=1

Zero Knowledge Proofs From Passive, Honest-Majority MPC "in the head"

- Consider an honest-majority, passive and perfectly secure MPC protocol II, using servers P₁,..,P_n, for a functionality which takes (f,v) from client C_{in} and gives (f,f(v)) to client C_{out}
- ${\, \ensuremath{ \circ }}$ Alice carries out the execution of a session of Π with her inputs (f,v) as the input of C_{in}
- Alice sends the view of C_{out}, View(C_{out}) to Bob and commits to the view of the ith server, View(P_i), for every i, to Bob
- Bob sends a random subset S ⊆ [n], |S| < n/2 to Alice. Alice opens
 View(P_i) for all i∈S.
- Bob accepts the proof (and outputs f), if every pair of views it got is consistent, and View(Cout) has the output (f,1)

View has incoming messages and randomness. Outgoing messages are computed using Π

Zero Knowledge Proofs From Passive, Honest-Majority MPC "in the head"

- Security against corrupt Bob: Bob's view consists solely of View(Cout) and View(Pi) for i∈S where S is chosen by Bob (after seeing View(Cout))
 - Since |S|<n/2, can be simulated just based on f, by the passive (adaptive) security of II
- Security against corrupt Alice: Simulator can see what Alice commits to, but these views may not be consistent
 - If there is a vertex cover of < n/2 server views covering "inconsistent edges", then execution corresponds to one with < n/2 corrupt parties. If ∏ is perfectly correct, simulator for ∏ can extract v from the view of the honest parties.
 - If no such vertex cover, too many independent inconsistent edges and S will contain at least one such pair except with negligible probability