

Public-Key Cryptography

Lecture 12

CCA Secure PKE

CCA Secure PKE

- In SKE, to get CCA security, we used a MAC
 - Bob would accept only messages from Alice
- But in PKE, Bob wants to receive messages from Eve as well!
 - But only if it is indeed Eve's own message: she should know her own message!

Chosen Ciphertext Attack

- Suppose Enc SIM-CPA secure
 - Suppose encrypts a character at a time (still secure)

Alice → Bob: $\text{Enc}(m)$


Eve: $\text{Hack}(\text{Enc}(m)) = \text{Enc}(m^*)$
(where $m^* = \text{Reverse of } m$)

Eve → Bob: $\text{Enc}(m^*)$

Bob → Eve: "what's this: m^* ?"

Eve: Reverse m^* to find m !

A subtle
e-mail attack

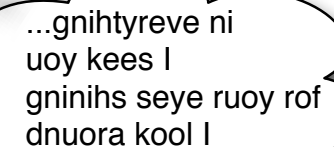


I look around
for your eyes shining
I seek you
in everything... !




Hey Eve,

What's this that you
sent me?



...gnihtyreve ni
uoy kees I
gninihs seye ruoy rof
dnuora kool I



I look around
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I seek you
in everything...

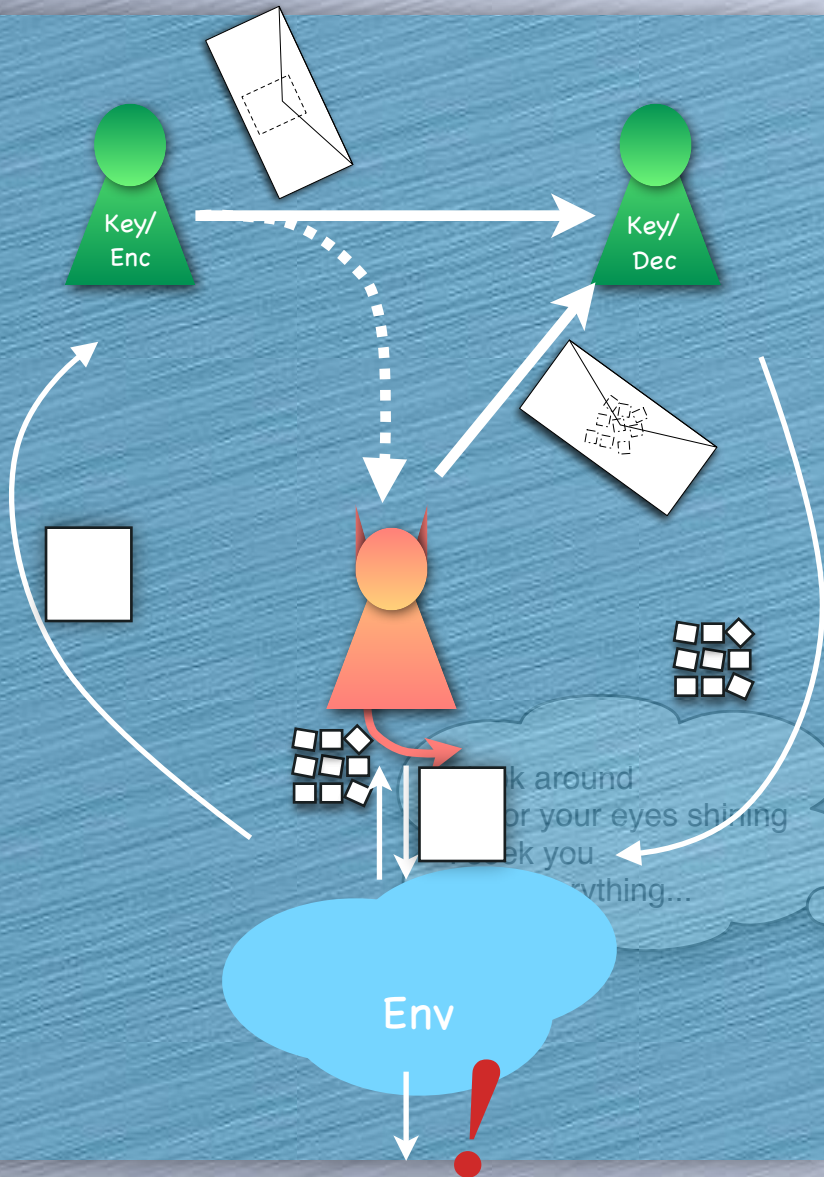
Malleability

- Malleability: Eve can “malleate” a ciphertext (without having to decrypt it) to produce a new ciphertext that would decrypt to a “related” message
- E.g.: Malleability of El Gamal
 - Recall: $\text{Enc}_{(G,g,Y)}(m) = (g^x, M \cdot Y^x)$
 - Given (X, C) change it to (X, TC) : will decrypt to TM
 - Or change (X, C) to (X^a, C^a) : will decrypt to M^a
- If chosen-ciphertext attack possible
 - i.e., Eve can get a ciphertext of her choice decrypted
 - Then Eve can exploit malleability to learn something “related to” Alice’s messages

More subtly, the 1 bit - valid or invalid - may leak information on message or SK

Chosen Ciphertext Attack

- SIM-CCA: does capture this attack



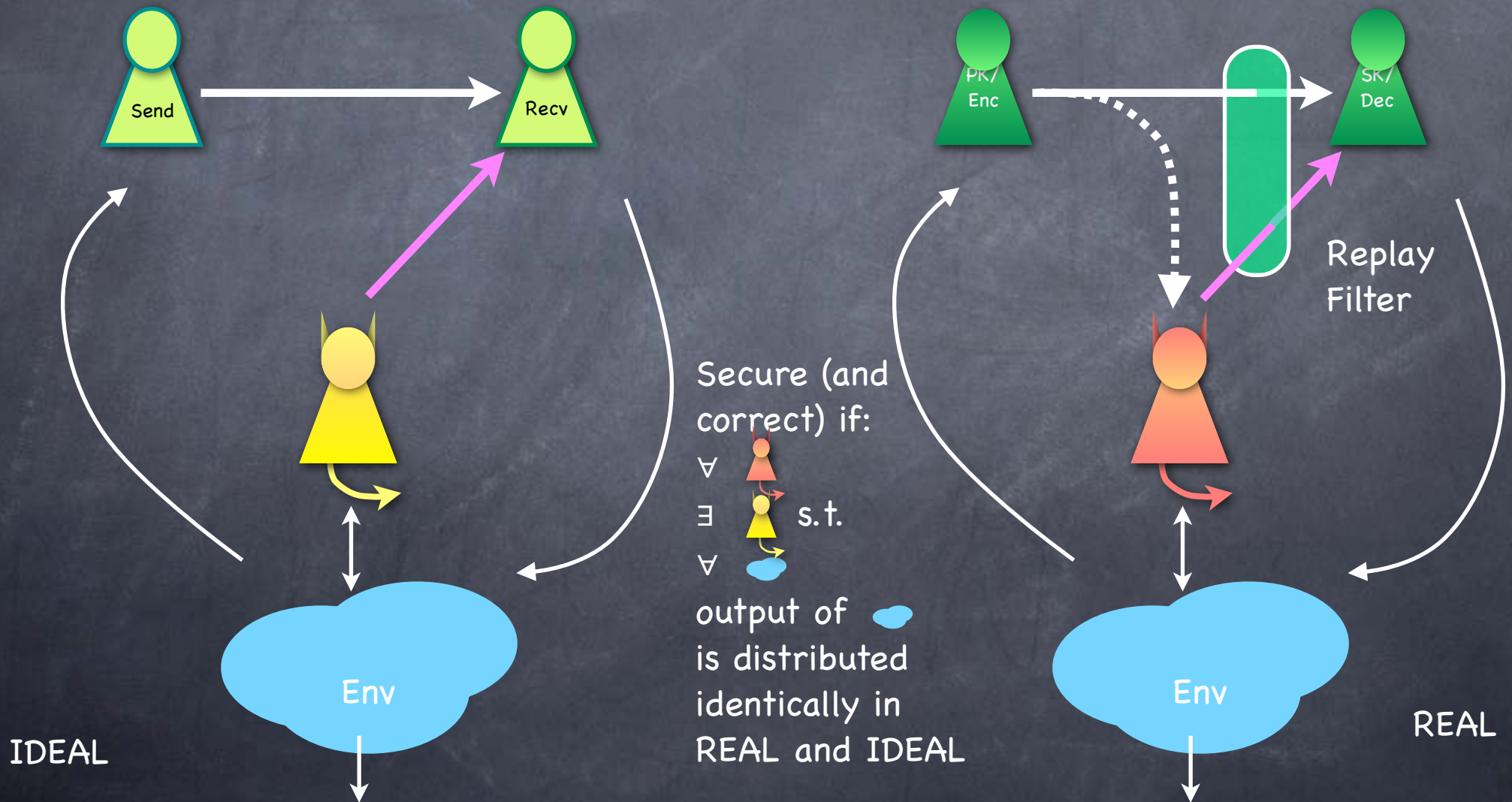
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SIM-CCA Security (PKE)



CCA Secure PKE Schemes

- Several schemes in the heuristic "Random Oracle Model"
 - RSA-OAEP
 - Fujisaki-Okamoto
 - DHIES (doesn't need the full power of ROM)
- Cramer-Shoup Encryption: Provably secure CCA scheme, under DDH assumption (next time)
- Hybrid Encryption schemes: Improving the efficiency of PKE

Random Oracle Model

- **Random Oracle:** a mythical oracle that, when initialized, picks a random function $R:\{0,1\}^* \rightarrow \{0,1\}^{n(k)}$ and when queried with x , returns $R(x)$
 - All parties have access to the same RO
- In ROM, evaluating some “hash function” H would be modeled as accessing an RO
 - Hope: the code for H has “no simple structure” and only way to get anything useful from it is to evaluate it on an input
- Sometimes security definitions need to be adapted for ROM
- Rigorous proofs of security, after moving to the ROM

Random Oracle Model

- **There is no Pseudo-RO**

- Unlike PRF, RO must be locally evaluable for all parties.
(think: giving out the seed of a PRF)

- **There are schemes secure in ROM, such that for any instantiation of the RO, the scheme is insecure!**

- Also natural constructs/primitives which are realizable in ROM, but not in the standard model!

- What does a proof in ROM tell us?

- Secure against attacks that treat H as a blackbox (and for which H is pseudorandom)

RSA-OAEP

- RSA-OAEP

- “Text-book RSA encryption” (i.e., f_{RSA} , the Trapdoor OWP candidate) applied to an “encoding” of the message
 - Encoding is randomized
 - Encoding uses a hash function modeled as a Random Oracle
 - Security in the RO Model, assuming f_{RSA} a OWP
- Part of **RSA Cryptography Standard** (PKCS#1 Ver 2.1).
Commonly used in SSL/TLS implementations

Hybrid Encryption

- PKE is far less efficient compared to SKE (even in ROM)
 - SKE using Block Ciphers (e.g. AES) and MAC is very fast
 - RSA-OAEP uses modular exponentiations (Cramer-Shoup even more)
- **Hybrid encryption:** Use (CCA secure) PKE to transfer a key for the (CCA secure) SKE. Use SKE with this key for sending data
 - Hopefully the combination remains CCA secure
 - Note: PKE used to encrypt only a (short) key for the SKE
 - Relatively low overhead on top of the (fast) SKE encryption

Hybrid Encryption

Or to
generate a
key

- Hybrid Encryption: KEM/DEM paradigm
 - Key Encapsulation Method: a public-key scheme to transfer a key
 - Data Encapsulation Method: a symmetric-key scheme (using the key transferred using KEM)
- For what KEM/DEM is a hybrid encryption scheme CCA secure?
 - Works if KEM is a SIM-CCA secure PKE scheme and DEM is a SIM-CCA secure SKE scheme
 - Easy to prove using “composition” properties of the SIM definition
 - Less security sufficient: KEM used to transfer a random key; DEM uses a new key every time.

Another PKE Scheme: CCA Secure in RO Model

- Fujisaki-Okamoto Hybrid scheme
 - KEM encrypts random x , using random coins derived as $H(m,x)$, where m is the message and H a "random oracle"
 - DEM encrypts m with key $K = G(x)$, where G is another "random oracle"
 - Decryption decrypts x , then m , and then checks if KEM was correct
 - Very weak security sufficient for encryptions used in KEM and DEM (but only with H, G modelled as random oracles)

CCA Secure PKE: DHIES

- Diffie-Hellman Integrated Encryption Scheme
 - Part of some standards
- Essentially a hybrid scheme
 - Data Encapsulation: CPA secure SKE, and MAC
 - Key Encapsulation: $X=g^x$. Let $K=Y^x$, where Y is the PK (as in El Gamal), and $(K_{SKE}, K_{MAC}) = \text{Hash}(K)$ (where $K=Y^x=Xy$)
- CCA security based on a complex (non-standard) assumption involving **Hash** and the group: “**Oracle Diffie-Hellman Assumption**”