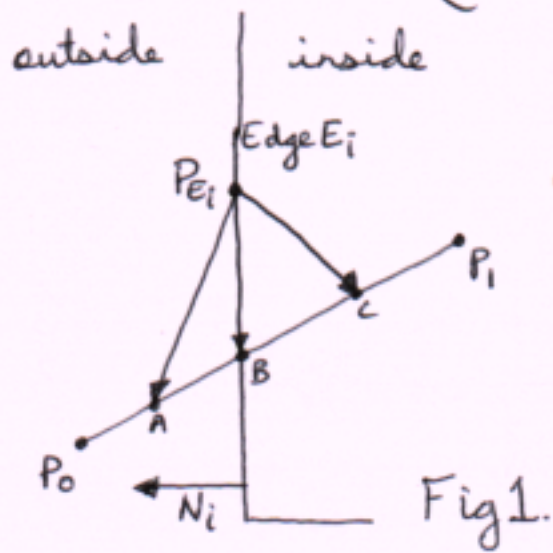


CYRUS-BECK (LIANG-BARSKY) CLIPPING



Let E_i be the edge against which we are trying to clip the line segment

$$P(t) = P_0 + (P_1 - P_0)t$$

Let N_i be the outward normal to the edge.

Then at point A, B, C on the line: (See Fig 1.)

$$\text{At A : } N_i \cdot [P(t) - P_{E_i}] > 0$$

$$\text{At B : } N_i \cdot [P(t) - P_{E_i}] = 0$$

$$\text{At C : } N_i \cdot [P(t) - P_{E_i}] < 0$$

⇒ To calculate the 't' at which the line intersects the edge we solve.

$$N_i \cdot [P(t) - P_{E_i}] = 0$$

$$\Rightarrow N_i \cdot [P_0 + (P_1 - P_0)t - P_{E_i}] = 0$$

$$\Rightarrow t = \frac{N_i \cdot [P_0 - P_{E_i}]}{-N_i \cdot D} \quad (\text{with } D = P_1 - P_0) \quad \text{--- (1)}$$

We get a valid value of 't' only if $N_i \neq 0$, $D \neq 0$ and $N_i \cdot D \neq 0$ (i.e., line is not parallel to the clip edge.)

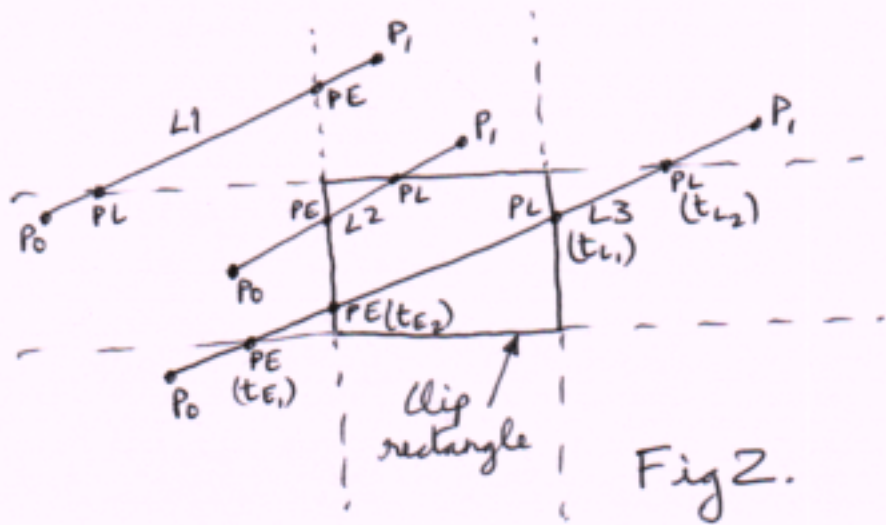


Fig 2.

If we consider infinite extents of the clip edges, a line segment can intersect each of the four edges once, given a rectangular clipping window.

So we compute these 't' values

for each intersection using equation (1) and corresponding

N_i and PE_i for each edge. Retain only those t values that are between 0 and 1.

NOW,

- We say a 't' is a Potentially Entering (PE) intersection if at that 't', $N_i \cdot D < 0$

- We say a 't' is a Potentially Leaving (PL) intersection if at that 't', $N_i \cdot D > 0$

Now if the t value corresponding to PE, i.e., t_E is greater than the t value corresponding to PL, i.e., t_L - then the intersections lie outside the clip rectangle (as is the case with L1 in Fig 2.)

If however, $t_E < t_L$, then the maximum t_E and minimum t_L values will be the intersections with the clip rectangle.

Note, that there can be multiple t_E and t_L values (as for L3 in Fig 2). That is why the maximum t_E and minimum t_L are considered.

Pseudocode for CYRUS-BECK CLIPPING

Given N_i and PE_i for each edge.

for (each line segment to be clipped) do

{
if ($P_1 == P_0$)

then line is degenerate so clip as a point;

else {

$t_E = 0$; $t_L = 1$;

for (each candidate intersection with a clip edge) do

{
if ($N_i \cdot D \neq 0$)

then {

calculate t using ①;

Use sign of $N_i \cdot D$ to categorize as PE or PL;

if (PE) then $t_E = \max(t_E, t)$;

if (PL) then $t_L = \min(t_L, t)$;

}

}

if ($t_E > t_L$) ^{then} return no intersection;

else

return $P(t_E)$ and $P(t_L)$ as intersections;

}

}