## A Logical Characterization for Dense-Time Visibly Pushdown Automata

<u>Devendra Bhave</u><sup>1</sup> Vrunda Dave<sup>1</sup> Shankara Narayanan Krishna<sup>1</sup> Ramchandra Phawade<sup>1</sup> Ashutosh Trivedi<sup>1,2</sup>

<sup>1</sup>Indian Institute of Technology Bombay

<sup>2</sup>University of Colorado Boulder

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Correctness of real-time systems depends on two factors

- Functional correctness
- Timing correctness

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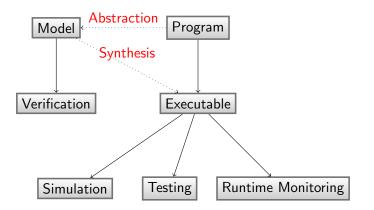
```
while(guard == true) {
    int e;
    e = getEvent();
    handleEvent(e);
}
```

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```
while(guard == true) {
    int e;
    e = getEvent();
    handleEvent(e); // Deadline: 10 Units
}
```

```
while(guard == true) {
    int e;
    e = getEvent();
    try {
        handleEvent(e) within 0 to 10;
    }
    catch (TimeoutException ex) {
        // Exception handler
    }
}
```



We need:

- Stack: To support functions call and return Pushdown Automaton
- Clock: Time measurement and checking Timed Automaton
- Good properties: Complementable, Determinizable

### Dense Time Visibly Pushdown Automata

start 
$$\rightarrow$$
  $l_0$   $b$   $l_1$   $c, x_b \le 1, \text{ pop}(\alpha) \in [1, 1]$   $l_2$   $c, \text{ pop}(\alpha) \in [2, 2]$   $l_3$   
 $d, \text{ pop}(\perp)$   
Accepted language:  $a^n b c^n d$   
 $a$   $a$   $\cdots$   $a$   $b \stackrel{\leq 1}{=} c$   $\cdots$   $c$   $c$   $d$   
 $=1$   
 $(1,2)$ 

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## Properties of dtVPA

#### Main results:

- Union closure
- Intersection closure
- Determinizable
- Complementable
- Emptiness checking: Decidable
- Inclusion, universality: Decidable

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• Logical formula = Automaton

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