

*Home Page*

*Title Page*

*Contents*



Page 1 of 19

*Go Back*

*Full Screen*

*Close*

*Quit*

# Railway Time-Tabling Effort

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Home Page

Title Page

Contents



Page 2 of 19

Go Back

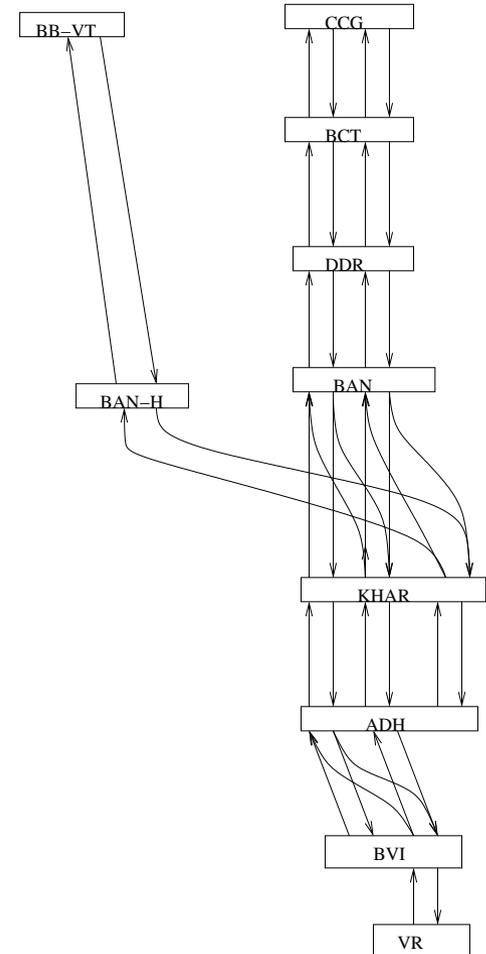
Full Screen

Close

Quit

## The WR Network

- 28 stations
- Over 200 track segments
- around 1000 services daily
- 67 rakes (physical trains)
- over 300 junctions/points



Home Page

Title Page

Contents



Page 3 of 19

Go Back

Full Screen

Close

Quit

## Objectives

### Inputs

- The Physical Network  
stations, lines, platforms.
- Operational Norms  
Headway, turn-around times.
- Patterns of Operation  
such as CCG-VR fast
- Requirements  
Specific as well as aggregates

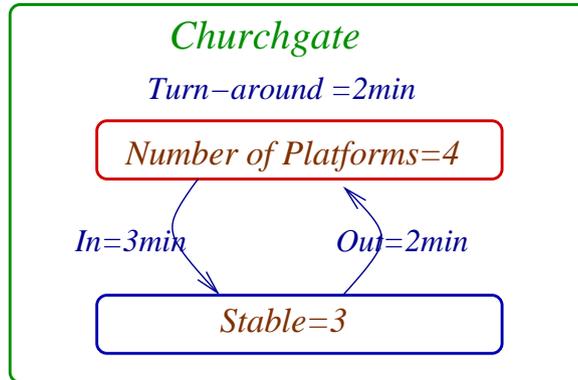
### Outputs

- TimeTable  
detailed timings.
- Rake-Links  
alloting physical EMUs.
- Platform Charts.

## The Network

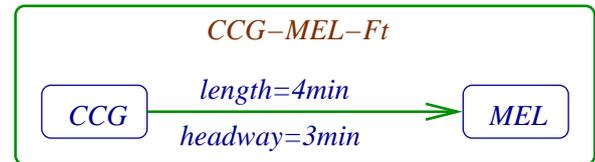
### Stations

- Name
- No. of Platforms
- No. of Stables
- Turn-around Time
- Push-In/Pull-Out Time



### Lines-unidirectional

- Start/End Station
- Duration (time)
- Headway (time)
- Fork/Join List



Home Page

Title Page

Contents



Page 5 of 19

Go Back

Full Screen

Close

Quit

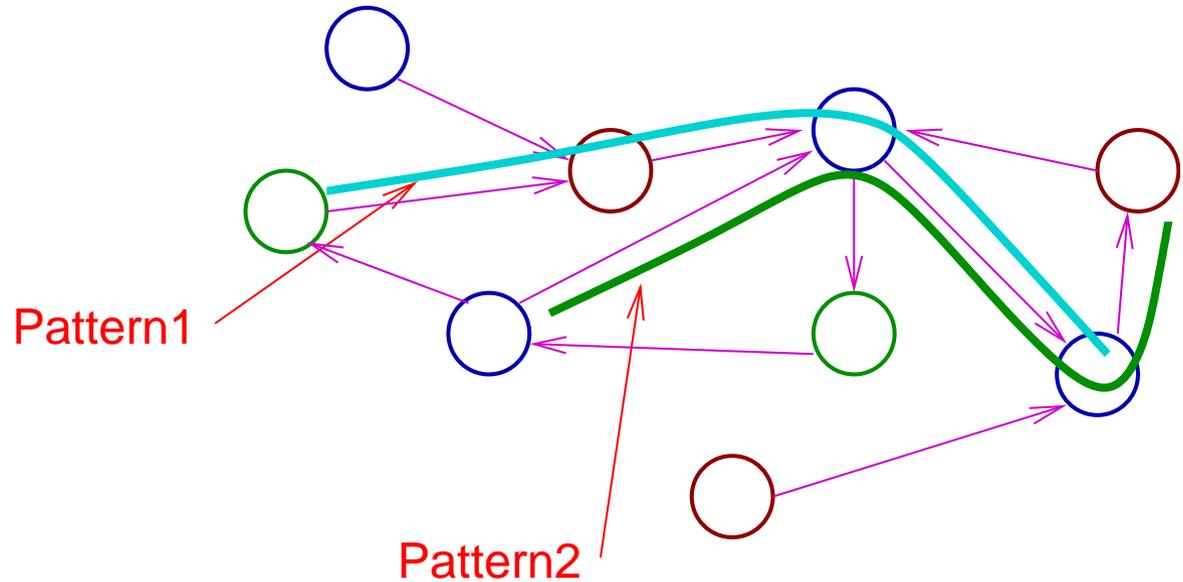
## Pattern

This encapsulates a typical and repeating pattern of operation.

pattern-id		
9-CCG-BVI-Ft		
Station	Stoppage	Line
Churchgate	-	CCG-BCT-Thru
BombayCT	[1,1]	BCT-DDR-Thru
Dadar	[1,2]	DDR-BAN-Thru
Bandra	[1,1]	BAN-KHR-Thru
Khar	[0,0]	KHR-ADH-Thru
Andheri	[1,4]	ADH-BVI-Cross
Borivili	-	-

## A Picture

Thus, **pattern** is a path with time prescribed flexibility in the network.



## The *vptt*

The *vptt* is the input as well as the output. Fields are

- (i) service-id and desired pattern
- (ii) required start-time interval
- (iii) actual start and end-times
- (iv) rake-links

service-id	BVI-647		PROP-3		ADH-751	
pattern-id	9-CCG-BVI-Ft		9-BVI-CCG-Su		9-CCG-ADH-Sw	
start-time	18:20	18:26	19:24	19:30	20:19	20:24
start	CCG	18:23	BVI	19:30	CCG	
end	BVI	19:24	CCG	20:27	ADH	
rake-link	PROP-3		ADH-751			

Home Page

Title Page

Contents



Page 8 of 19

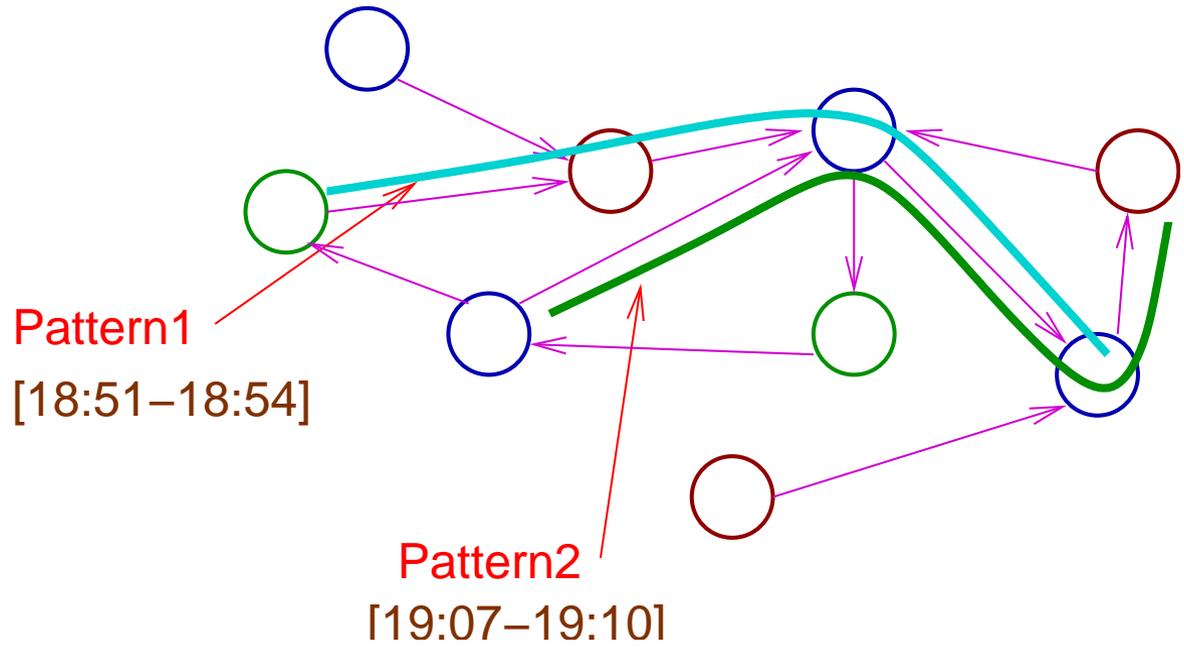
Go Back

Full Screen

Close

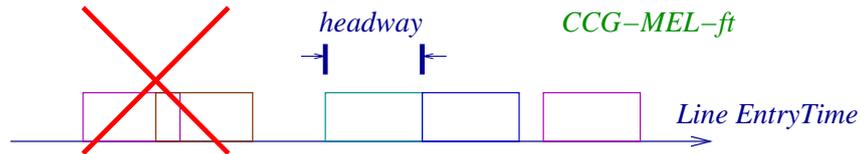
Quit

## A Picture

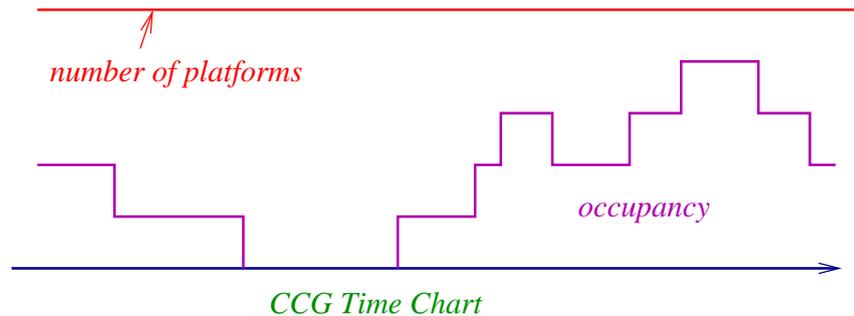


## The Constraints

- **line constraints**-services using the same track must be headway apart.



- **platform constraints**-these must be available for halts at stations.

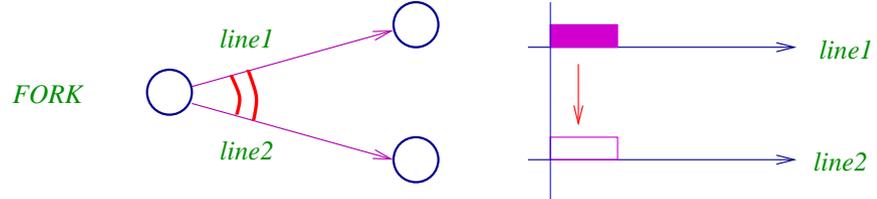


- **continuity constraints**-train departs a station and enters a line and vice-versa, and follows the pattern

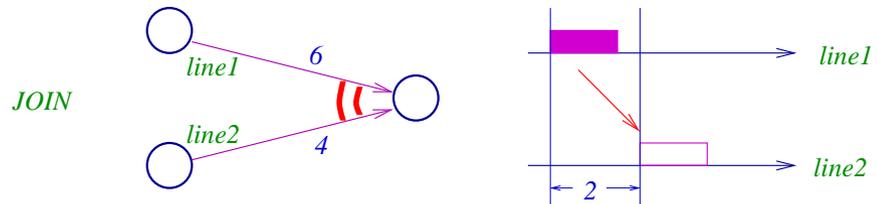


## Other Constraints

- Fork



- Join



## Solvers

### Manual Aids

- Check a TT
- Move services
- Order Services

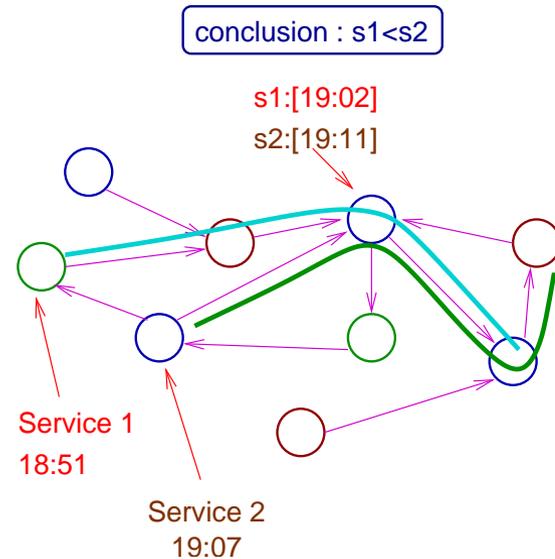
### Automatic

- based on CHIP C++ Constraint Solver. Allows constraints to be posted on variables. Follows clever branch-and-bound
- Partial Order on services  $S$  by *time*  
Partition into clubs  $S_1, S_2, \dots, S_k$
- Solve  $S_i, S_{i+1}$  together. Freeze  $S_i$  and move to  $S_{i+1}, S_{i+2}$

**Compute-Instensive:** Takes 50 minutes for half (UP) service set.

## How to define $S_i$ 's?

- Organize the services in a **temporal partial order**.
- Pick bunch  $S_1$  by peeling off the top few, then  $S_2$  and so on.



- services  $s_i$  and  $s_j$ .
- depart-times  $t_i, t_j$ .
- patterns  $p$  and  $p'$

If  $d_i - d_j \geq T(p, p')$   
then  $s_j < s_i$ .

## Rake-Linking

Once the services have been scheduled, they have to be **provisioned**: assign one of the 64 rakes available with WR.

**Step 1** Form the Service Graph.

- Vertices: Services
- Edges: Possible Successor

CCG 72
BVI 180

*Direct  
Edge*

BVI 192
CCG 304

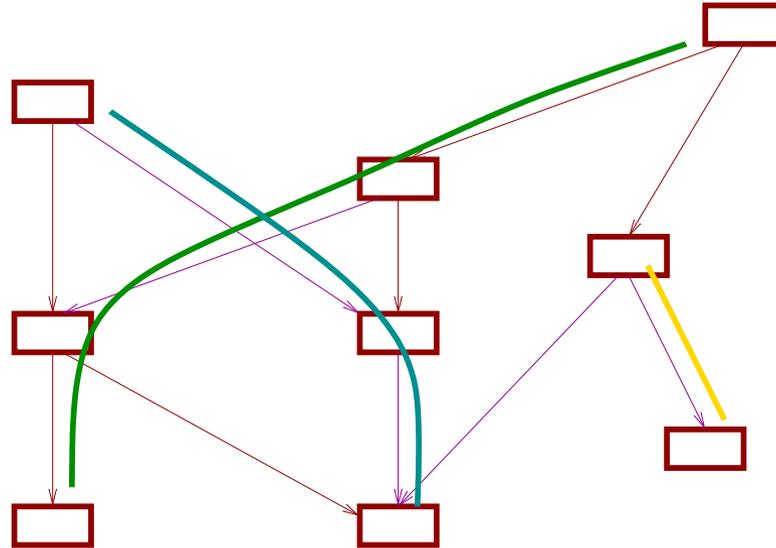
CCG 72
BVI 180

*Indirect  
Edge*

ADH 221
CCG 302

## The Service Graph

Step 2 Compute Chain Decomposition.



- DAG
- Min-Cost-Flow and its variants
- Extremely Fast and provably optimal: **2 minutes**

Home Page

Title Page

Contents



Page 15 of 19

Go Back

Full Screen

Close

Quit

## Platform Allocation

### Inputs

- Service In-Out times
- Service Platform Preferences
- Set of Platforms

Service	In	Out	Platform
Rajdhani	18:56	18:57	4
Virar Local	18:54	19:05	1,2,3,4,5
Dahanu Shuttle	19:01	19:11	2,4

### Output

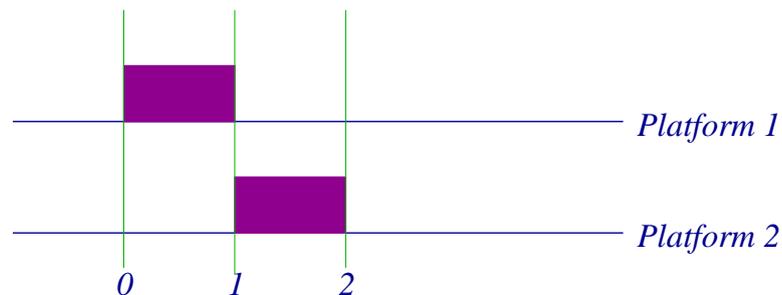
- Platform Allocation for each service
- Clash report if impossible

## Undifferentiated and differentiated

**Theorem:** For the undifferentiated case, if at no point are there more than  $P$  services, then all services can be assigned platforms.

Thus a necessary condition is sufficient. However there is no such theorem in the differentiated case.

Rajdhani	0	1	1
Virar Local	0	2	1,2
Dahanu Shuttle	1	2	2



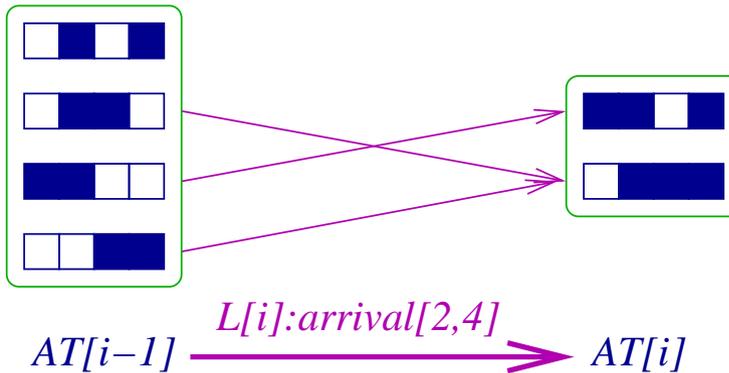
## The Algorithm-undiff

- Let  $A = \{a_1, \dots, a_n\}$  be the set of **arrival instants**. Similarly, let  $D$  be the set of **departure instants**.
- Let  $L = (l_1, l_2, \dots)$  be the list  $A \cup D$  **sorted** by time.
- Maintain **Allotment table**  $at[i]$ .



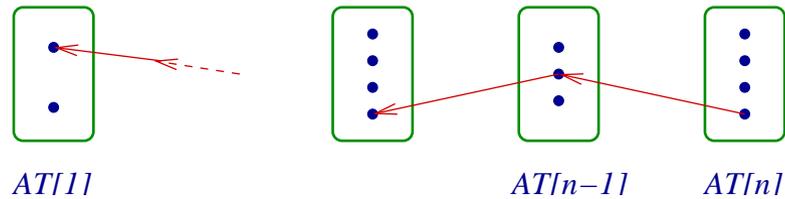
## The Algorithm-diff

- Form  $L$  as before.
- Maintain  $AT[i]$ , the collection of **all possible**  $at[i]$ . This is essentially **Dynamic Programming**.



## Algorithm continued

- If  $AT[i]$  is empty for some  $i$  then **declare infeasible**.
- Otherwise, pick an  $at \in AT[last]$  and **trace back**.



**Complexity:** Good for WR. Virar takes 20 seconds.