
CS228M Surprise Quiz 3 (Spring 2026)**Max marks: 10****Duration: 10 mins**

- *You are required to answer each question only in the sheet provided to you.*
- *Only material written in the sheet will be graded.*
- *The exam is open book and notes. However, you are not allowed to search on the internet or consult others over the internet for your answers.*
- *Be brief, complete and stick to what has been asked.*
- *Unless asked for explicitly, you may cite results/proofs covered in class without reproducing them.*
- *If you need to make any assumptions, state them clearly.*
- **Do not copy solutions from others. Penalty for offenders: FR grade.**

Consider the two first-order logic sentences given below:

$$\varphi_1 \equiv \forall x (P(x) \rightarrow \exists y Q(x, y))$$

$$\varphi_2 \equiv \exists x (P(x) \wedge \forall y Q(x, y))$$

Given below are two sentences with φ_1 and φ_2 as sub-formulas. You are required to indicate whether each of the sentences given below is valid. If you think a sentence is valid, give a natural deduction proof of its validity. If you think a sentence is not valid, give a structure M over the vocabulary $\mathcal{V} = \{P, Q\}$ such that the sentence evaluates to false over M . If you think both sentences are not valid, you can give two separate structures for the two sentences.

1. [5 marks] $\varphi_1 \rightarrow \varphi_2$

(PLEASE TURN OVER)

2. [5 marks] $\varphi_1 \rightarrow \neg\varphi_2$