

Program Analysis: Wrapping Up

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November 2017

Part 1

About These Slides

CS 618

Wrap Up: About These Slides

1/18

Copyright

These slides constitute the lecture notes for CS618 Program Analysis course at IIT Bombay and have been made available as teaching material accompanying the book:

- Uday Khedker, Amitabha Sanyal, and Bageshri Karkare. *Data Flow Analysis: Theory and Practice*. CRC Press (Taylor and Francis Group). 2009.
(Indian edition published by Ane Books in 2013)

Apart from the above book, some slides are based on the material from the following books

- A. V. Aho, M. Lam, R. Sethi, and J. D. Ullman. *Compilers: Principles, Techniques, and Tools*. Addison-Wesley. 2006.
- M. S. Hecht. *Flow Analysis of Computer Programs*. Elsevier North-Holland Inc. 1977.

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Part 2

The Big Picture



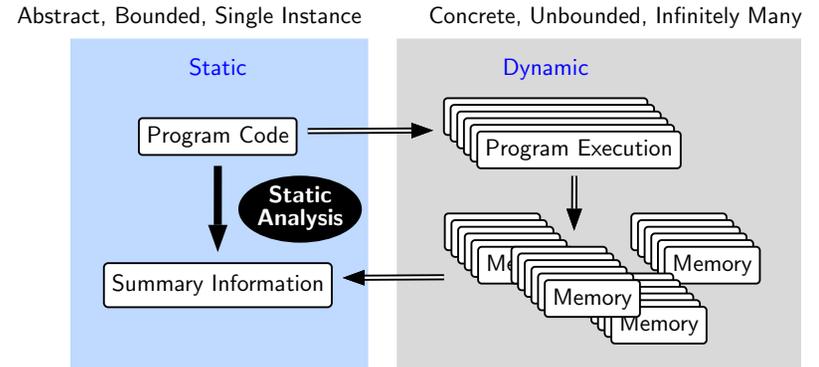
So what have learnt?

Education is what remains after you have forgotten everything that was taught

- Albert Einstein

The Main Theme of the Course

Constructing *suitable abstractions* for *sound & precise modelling* of *runtime behaviour* of programs *efficiently*



Soundness and Precision of Static Analysis

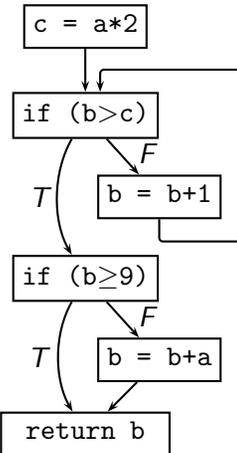
Example Program

```
int a;
int f(int b)
{ int c;
  c = a*2;
  while (b <= c)
    b = b+1;
  if (b < 9)
    b = b+a;
  return b;
}
```

Simplified IR

```
1: c = a*2
2: if (b > c) goto 5
3: b = b + 1
4: goto 2
5: if (b ≥ 9) goto 7
6: b = b+a
7: return b
```

Control Flow Graph



Execution Traces for Concrete Semantics

- A state: (Program Point, Variables ↦ Values)
- A trace: a valid sequence of states starting with a given initial state

	Trace 1	Trace 2
	a b c	a b c
1: c = a*2	0: (1, 2, 3)	0: (5, 10, 7)
2: if (b > c)	1: (1, 2, 2)	1: (5, 10, 10)
goto 5	2: (1, 2, 2)	2: (5, 10, 10)
3: b = b + 1	3: (1, 3, 2)	3: (5, 11, 10)
4: goto 2	4: (1, 3, 2)	4: (5, 11, 10)
5: if (b ≥ 9)	2: (1, 3, 2)	2: (5, 11, 10)
goto 7	5: (1, 3, 2)	5: (5, 11, 10)
6: b = b+a	5: (1, 4, 2)	7: (5, 11, 10)
7: return b	7: (1, 4, 2)	

Execution Traces for Concrete Semantics

- A state: (Program Point, Variables \mapsto Values)
- A trace: a valid sequence of states starting with a given initial state

```

1: c = a*2
2: if (b > c)
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```

Trace 1
a b c
7 : (1, 4, 2)

Trace 2
a b c

• Number of traces is potentially infinite

Execution Traces for Concrete Semantics

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Trace 1
a b c
7 : (1, 4, 2)

Trace 2
a b c

Trace 3
a b c
0 : (-1, 1, 6)
1 : (-1, 1, -2)
2 : (-1, 1, -2)
3 : (-1, 2, -2)
4 : (-1, 2, -2)
2 : (-1, 2, -2)
3 : (-1, 3, -2)
4 : (-1, 3, -2)
2 : (-1, 3, -2)
...

• Number of traces is potentially infinite

• Not all traces may terminate

Execution Traces for Concrete Semantics

- A state: (Program Point, Variables \mapsto Values)
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1: c = a*2
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```

Trace 1
a b c
7 : (1, 4, 2)

Trace 2
a b c

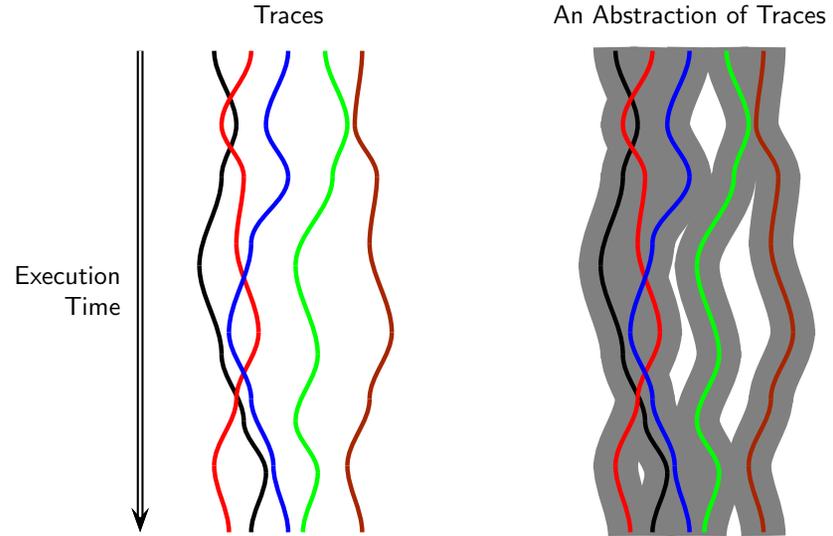
Trace 3
a b c
0 : (-1, 1, 6)
1 : (-1, 1, -2)
2 : (-1, 1, -2)
3 : (-1, 2, -2)
4 : (-1, 2, -2)
2 : (-1, 2, -2)
3 : (-1, 3, -2)
4 : (-1, 3, -2)
2 : (-1, 3, -2)
...

• Number of traces is potentially infinite

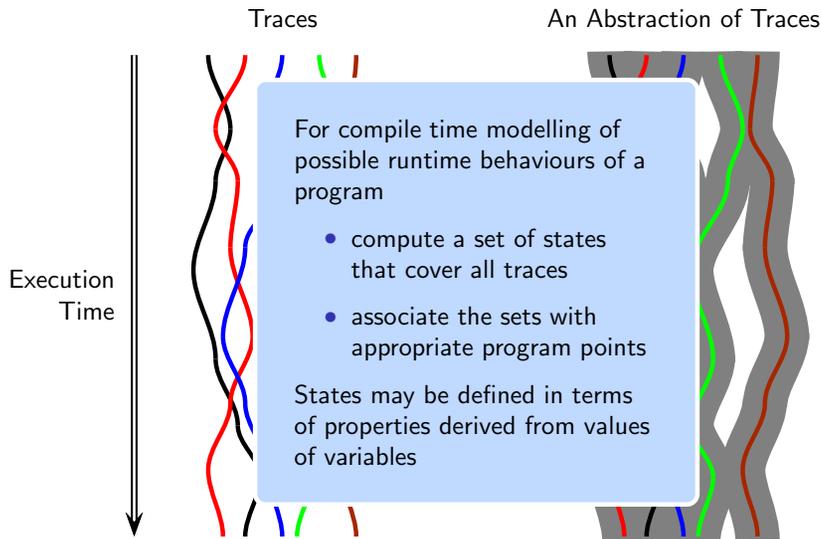
• Not all traces may terminate

• We consider only terminating traces

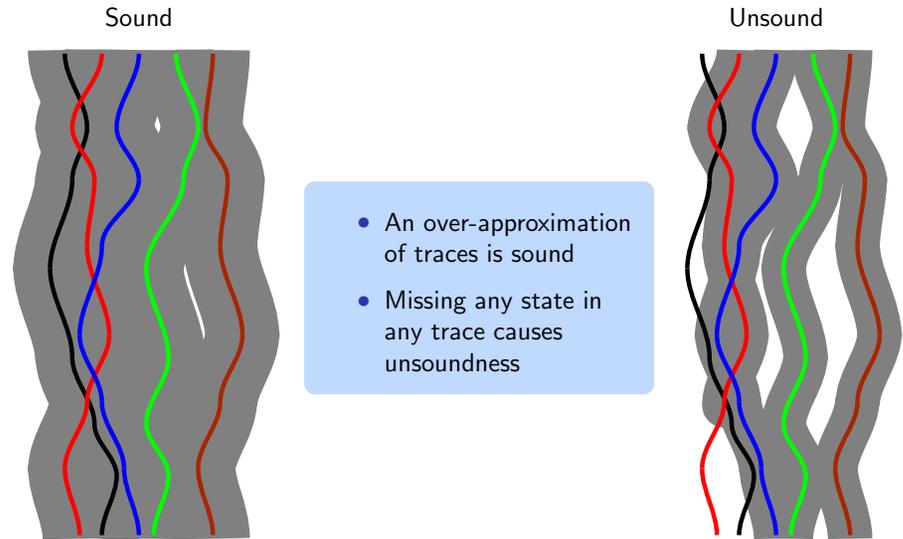
Static Analysis Computes Abstractions of Traces



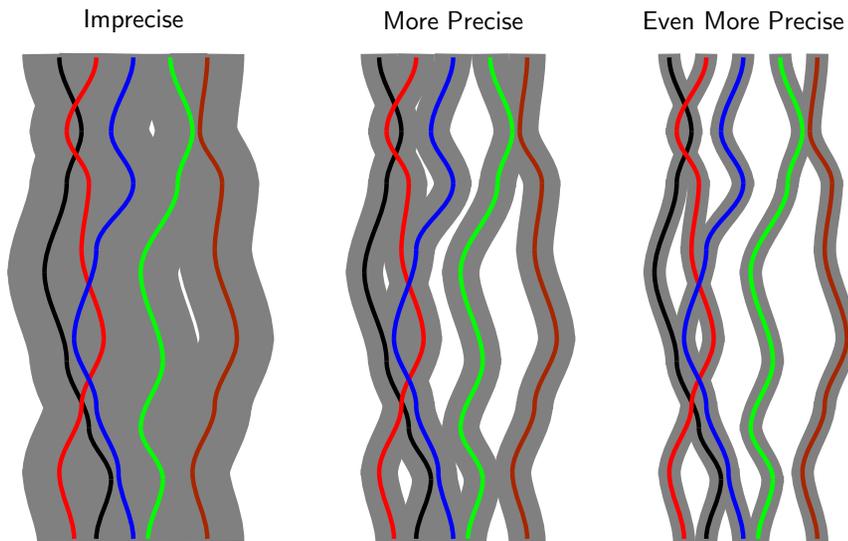
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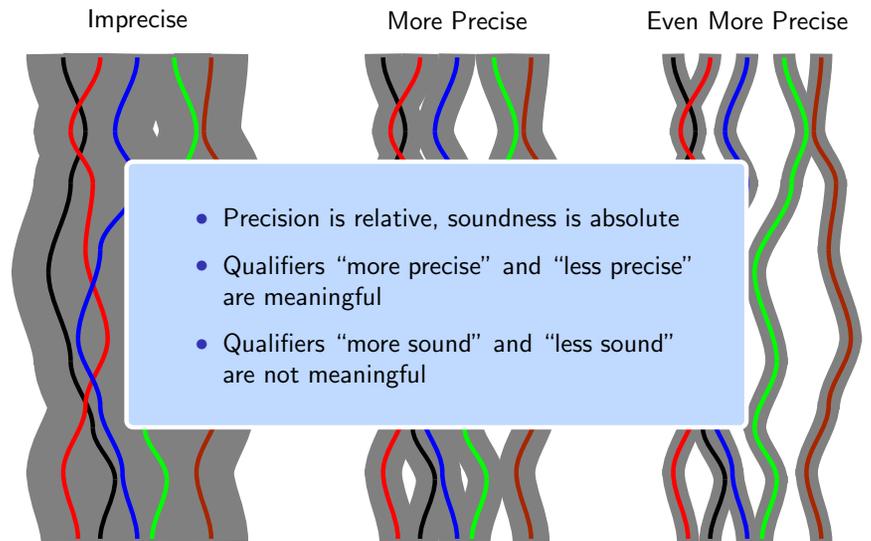
Soundness of Abstractions



Precision of Sound Abstractions

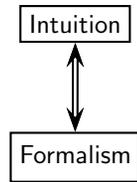


Precision of Sound Abstractions



Motifs Used for Building the Theme

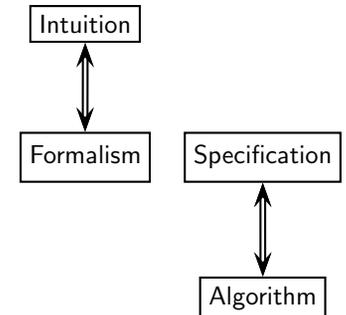
- Intuition-formalism dichotomy



- Intuitions representing abstract view of the run time behaviour
- Systematic formulation amenable to automation and reasoning

Motifs Used for Building the Theme

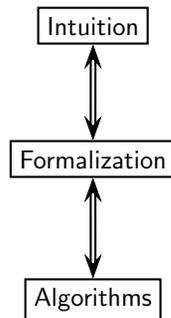
- Intuition-formalism dichotomy
- Specification-implementation dichotomy



- Separate reasoning from the implementation
- Systematize construction of analyzers

Motifs Used for Building the Theme

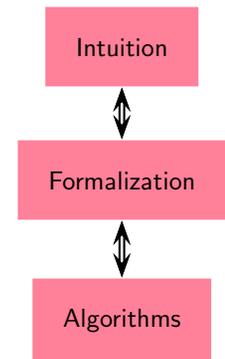
- Intuition-formalism dichotomy
- Specification-implementation dichotomy
- Successive generalizations



- Formalizing underlying concepts rigorously
- Formulating analysis in terms of data flow equations (confluence, initialization, boundary info, flow functions etc.)

Motifs Used for Building the Theme

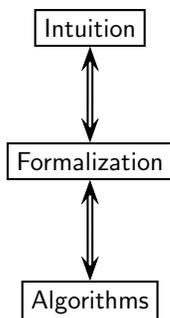
- Intuition-formalism dichotomy
- Specification-implementation dichotomy
- Successive generalizations



- Generalize by relaxing conditions (Previous abstractions should become special cases)
- Generalize the intuitions, specifications, or algorithm

Motifs Used for Building the Theme

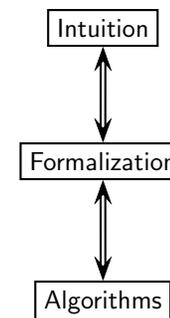
- Intuition-formalism dichotomy
- Specification-implementation dichotomy
- Successive generalizations
- Filtering and distilling ideas



- Ask the right questions
- Separate relevant from irrelevant

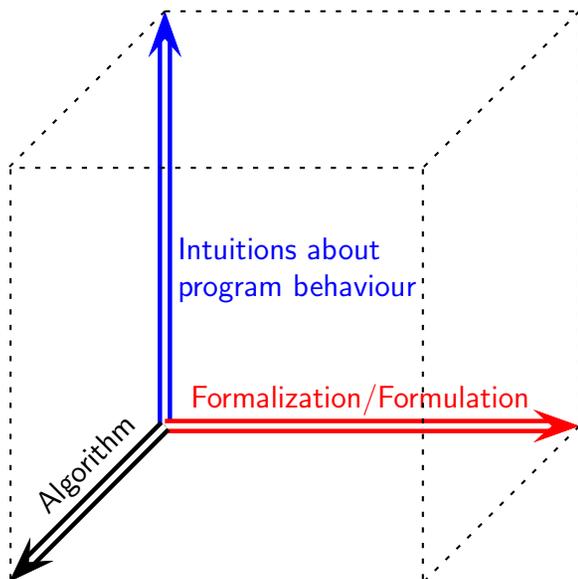
Motifs Used for Building the Theme

- Intuition-formalism dichotomy
- Specification-implementation dichotomy
- Successive generalizations
- Filtering and distilling ideas
- Working from first principles



- First principles: A small set of orthogonal concepts
- Add as few concepts as possible to the set of first principles

Seeking Generalizations



Module 1: Bit Vector Frameworks

Intuitions

- Data flow information at a program point u
 - represents information valid for all execution instances of u
 - depends on some or all paths,
 - starting at, or ending at, or passing through u
 - may be generated, killed, or propagated

Formalization

- Representations
 - programs \equiv control flow graphs
 - data flow values \equiv sets or bit vectors
 - dependence of data flow values \equiv data flow equations

Algorithm

- convergence
- iterative refinement
- initialization
- round robin method

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Module 2: Theoretical Abstractions

Intuitions

- sound approximation of data flow information
- merging data flow values
- direction of flow, relationship with graph traversal
- desired vs. computable solution

Formalization

- lattices, partial order, meet, descending chain condition (DCC)
- monotonicity, distributivity and non-separability of flow functions
- MFP and MoP assignments
- information flow paths, depth and width of a CFG

Algorithm

- conservative initialization
- complexity
- work list based method

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Module 2: Theoretical Abstractions

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- Theme: Generalization in formulations
- Learning outcome: Add the following requirements to the set of first principles
 - Monotonic flow functions and meet
 - semi-lattice satisfying DCC

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Module 3: General Frameworks

Intuitions

- dependence of data flow values across entities
- generation and killing depending upon the incoming information
- flow insensitivity, may and must nature in flow sensitivity
- use of program point in data flow information

Formalization

- Representations for data flow values: Sets, tuples, strings, graphs
- modelling non-separability in flow functions using dependent parts
- flow function operations (e.g. path removal, factorization, extension, relation application)

Algorithm

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Algorithm

- Generalizations in formulation
- Observations:
 - Structure of heap accesses consist of repeating patterns that resemble the program structure
 - Program analysis should be driven by liveness to restrict the information to usable information

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Module 4: Interprocedural Data Flow Analysis

Intuitions

- interprocedural validity of paths and context sensitivity
- constructing summary flow functions Vs. propagating data flow values
- orthogonality of context and data flow information
- partitioning contexts based on data flow values

Formalization

- lattices of flow functions, reducing function compositions and meets
- data flow equations for constructing summary flow functions
- value contexts, their exit values, and transitions

Algorithm

- work list based method
- ordering of nodes in post or reverse post order

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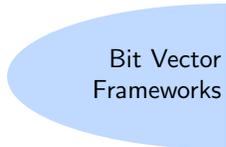
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Algorithm

- work list based method
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- Generalizations in formulation and algorithm
- Observation:
Separating relevant information from irrelevant information can have a significant impact

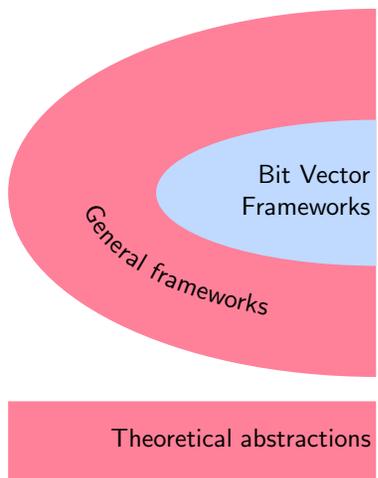
Sequence of Generalizations in the Course Modules



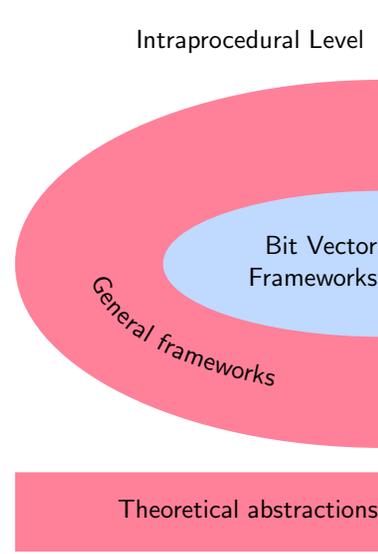
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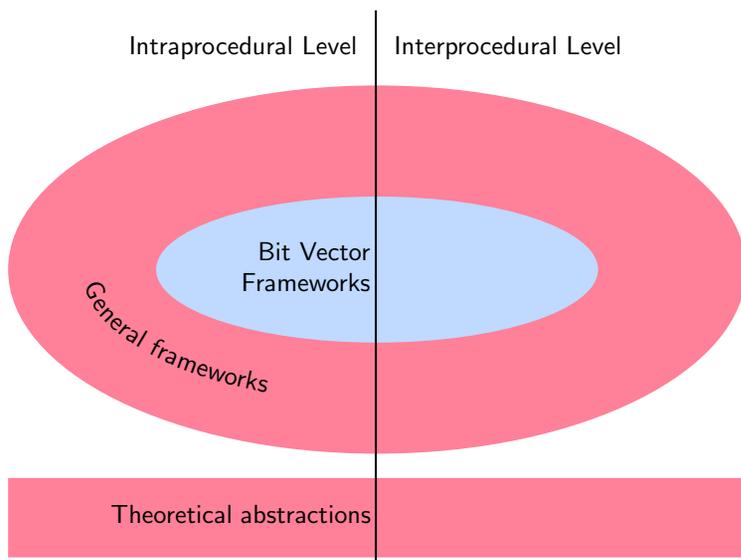
Sequence of Generalizations in the Course Modules



Sequence of Generalizations in the Course Modules



Sequence of Generalizations in the Course Modules



Takeaways of the Course

- Data Flow Analysis:
 - Minimal conditions for devising a data flow framework
 - ▶ Intraprocedural formulation:
 - Meet semilattice satisfying the descending chain condition, and
 - Monotonic flow functions
 - ▶ Extension to interprocedural level: Additional restrictions
 - Value based approach: Finiteness of lattice
 - Functional approach: Distributive primitive entity functions
- General:
 - ▶ Generalization, refinements, distilling the essence
 - ▶ Asking the right questions
 - ▶ Separating relevant information from the irrelevant information

Still Bigger Picture ...

Scope of the course: Generic static analyses for imperative languages

Did not cover

- Influences of other languages features
 - ▶ Concurrency, Object orientation, Coroutines, Exception handling
 - ▶ Declarative paradigms: functional or logic languages
- Influences of other goals
 - ▶ Verification and validation, testing (e.g. analyses for finding bugs does not require exhaustiveness or soundness)
 - ▶ Path sensitive analyses
 - ▶ Shape analysis
 - ▶ Optimization specific analyses
 - ▶ Adhoc techniques of achieving efficiency
 - ▶ Analyses for JIT compilation
 - ▶ Parallelization, Vectorization, Dependence analysis
- Other analysis methods
 - ▶ Abstract interpretation, Type inference, Constraint resolution



Last But Not the Least

Thank You!

